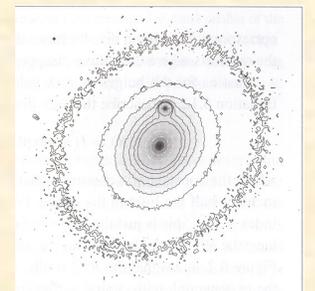
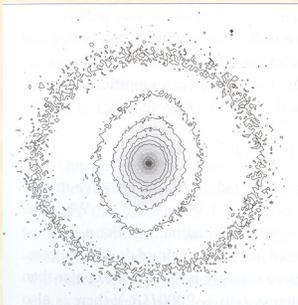
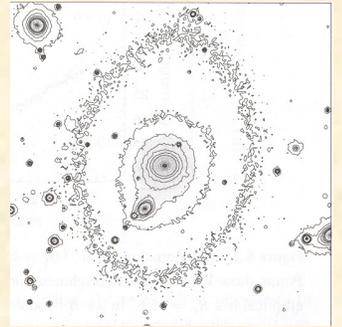


# Photometry of Galaxies

- Basics
- Absolute Magnitudes
- Surface Photometry
- Sky Brightness
- Surface Brightness Profiles
- 3D Shapes
- Luminosity Functions
- Global Correlations



# Basics of Photometry

- Magnitude System: For two stars or two galaxies :

$$m_1 - m_2 = -2.5 \log(F_1/F_2)$$

- For a particular filter band pass, where  $T_\lambda$  is the filter response:

$$m = -2.5 \log \left( \int_0^\infty T_\lambda F_\lambda d\lambda \right) + \text{const.}$$

Ex) To calibrate the V band in the Johnson UBV system, we find that for an A0 V star with apparent magnitude  $V = 0$ :

$$F_\lambda(5500 \text{ \AA}) = 3.75 \times 10^{-9} \text{ ergs s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1} \quad (\text{Allen, AQ, p. 387})$$

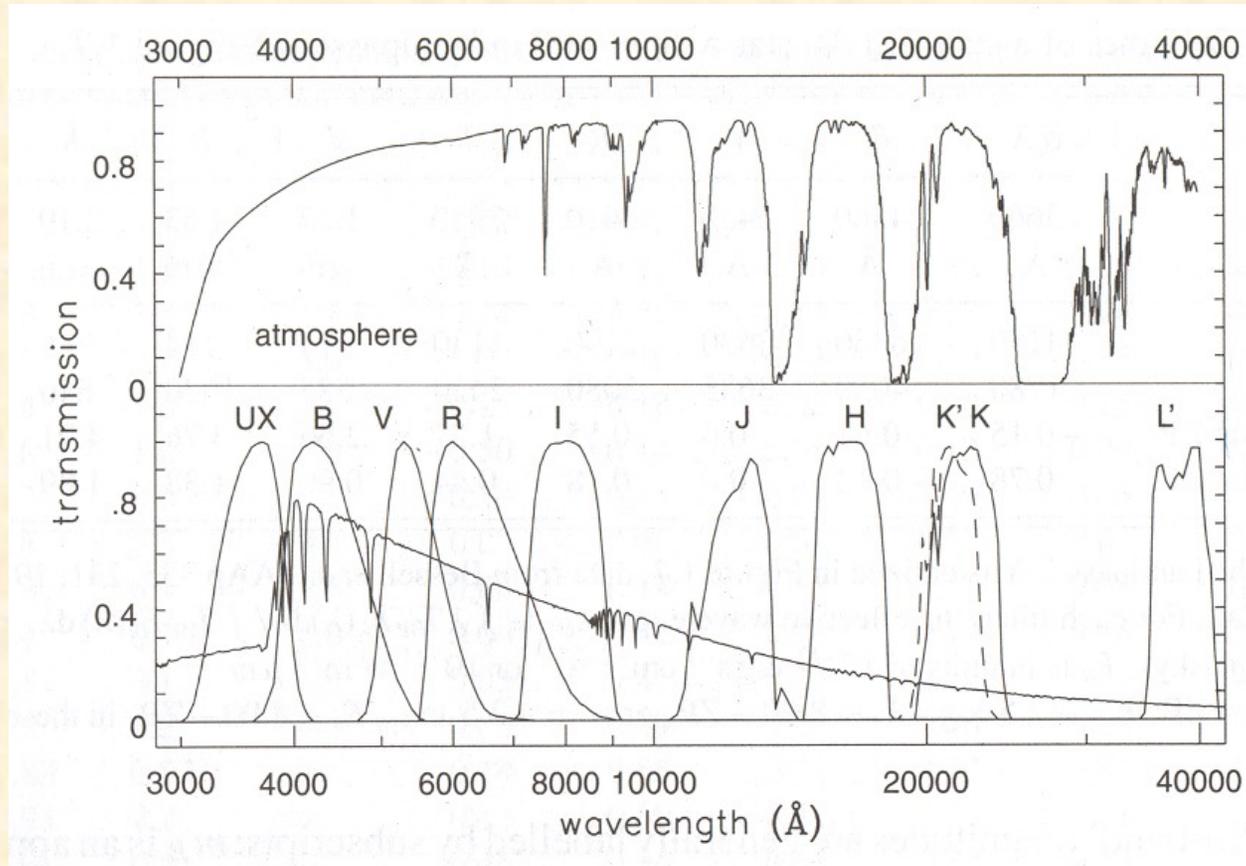
$$\text{So: } V = -2.5 \log [F_\lambda(5500 \text{ \AA})] - 21.065$$

- Colors: one filter magnitude minus another

Ex)  $B - V = 0$  for A0 V star; bluer stars have negative colors

- colors (e.g.,  $J - K$ ) are defined to be zero for an A0 V star

# Filter Bandpasses



(Sparke & Gallagher, p. 20)

$$\text{Effective Wavelength} : \lambda_{\text{eff}} = \frac{\int_0^{\infty} \lambda T_{\lambda} d\lambda}{\int_0^{\infty} T_{\lambda} d\lambda}$$

UX	B	V	R	I	J	H	K	L'
3660Å	4360Å	5450Å	6410Å	7980Å	1.22μ	1.63μ	2.19μ	3.80μ

# Absolute Magnitudes – Galaxies

- Absolute magnitude ( $M$ ): object's apparent magnitude at 10 pc
  - Measure of object's luminosity  $L$  ( $\text{ergs s}^{-1}$ )
- Distance modulus:  $m - M = 5 \log(d) - 5$  ( $d$  is distance in pc)
- Need to correct for extinction  $A$  (strongly  $\lambda$  dependent):
  - Ex)  $V - M_V = 5 \log(d) - 5 + A_V$
- For a high-redshift galaxy, correct for spectral shift in bandpass:
  - Ex)  $V - M_V = 5 \log(d) - 5 + A_V + K_V$
- In general,  $K$  is called the “K-correction”
  - $K = k + 2.5 \log(1+z)$
  - $k$  is a function of galaxy type and  $z$  (tabulated for different bandpasses in Frei & Gunn, 1994, AJ, 108, 1476)
- $M_V$  (Sun) = +4.82       $M_V$  (Galaxy) = -20.6

# Absolute Bolometric Magnitudes

- Measure of luminosity over entire spectrum:

$$M_{\text{bol}} = M = -2.5 \log \left( \int_0^{\infty} L_{\lambda} d\lambda \right) + \text{const.}$$

Bolometric Correction:

$$\text{BC} = M - M_V \quad (\text{depends on object's spectrum})$$

$$\text{BC (Sun)} = -0.08$$

- Some numbers (from Allen's AQ): ( $\odot$  = Sun)
  - $M_{\odot} = +4.74$
  - $L_{\odot} = 3.84 \times 10^{33} \text{ ergs s}^{-1}$
  - $L (\text{Galaxy}) \approx 3.6 \times 10^{10} L_{\odot}$  (bolometric)
  - $L_B (\text{Galaxy}) \approx 2.3 \times 10^{10} L_{\odot}$  (B-band)
  - $L_B (\text{Galactic Disk}) \approx 1.9 \times 10^{10} L_{B\odot}$  (B-band)
  - $Mass (\text{Galactic Disk}) \approx 1 \times 10^{11} M_{\odot}$  (to  $R = 8.5 \text{ kpc}$ )
  - $M/L_B (\text{Disk}) \approx 5 M_{\odot} / L_{B\odot}$

# Surface Photometry

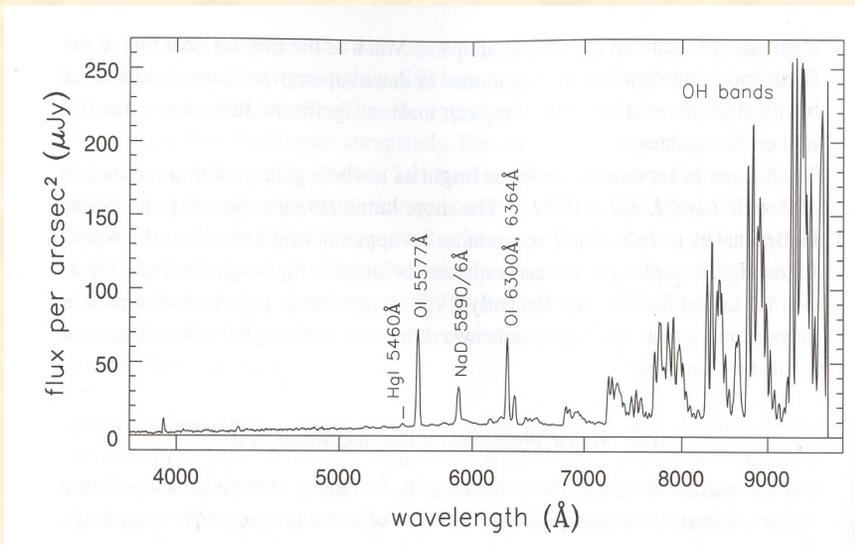
- **Surface brightness:**  $I$  ( $\text{ergs s}^{-1} \text{ cm}^{-2} \text{ arcsec}^{-2}$ ),  $\mu$  ( $\text{mag arcsec}^{-2}$ )
- Independent of distance ( $d$ ) to 1<sup>st</sup> order (neglecting cosmological redshift effects and surface brightness changes)
  - Consider a small patch of a galaxy with uniform brightness, sides of length  $D$ , apparent angular length  $\alpha$ , at a distance  $d$ :
$$I = \frac{F}{\alpha^2} = \frac{L/4\pi d^2}{(D/d)^2} = \frac{L}{4\pi D^2}$$
  - For a flat disk,  $I$  increases as  $1/\cos(i)$  ( $i$  = inclination)
- *Measured*  $I$  depends on resolution of image
- **Surface brightness profile:** change in  $I$  with distance from center along major axis of image
  - Often measured by fitting elliptical isophotes.
  - Strongly affected by subtraction of night sky emission.
  - Core affected by PSF of telescope and “seeing”.

# Sky Brightness

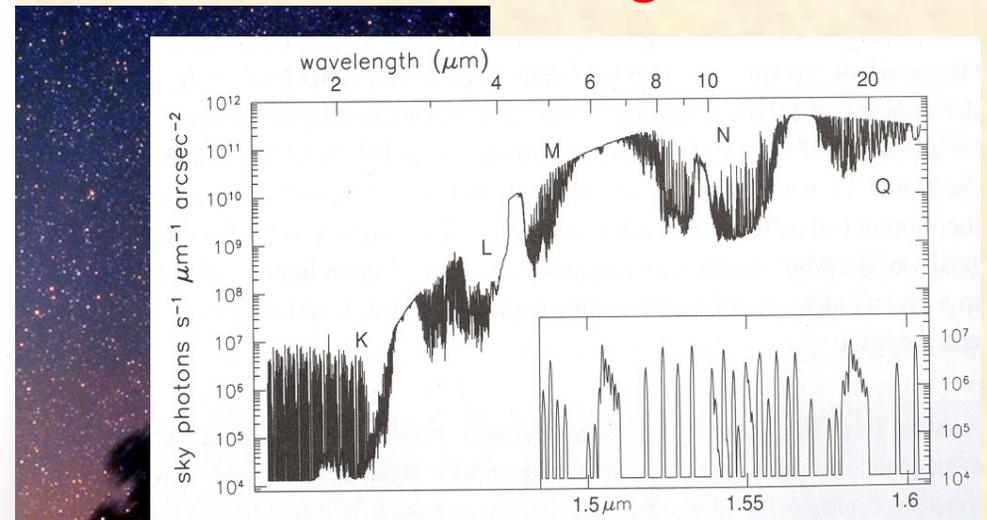
- For a dark sky (from the ground):  $\mu_B \approx 23$ ,  $\mu_R \approx 21$  mag arcsec<sup>-2</sup>
- Contributions (decreasing importance in the optical):
  - 1) Zodiacal light: sunlight scattered off interplanetary dust
  - 2) Airglow: emission lines in the upper atmosphere (O I, NaD: UV ionization and recombination, excited OH: O<sub>3</sub> + H<sub>2</sub>O reaction)
  - 3) Unresolved Galactic starlight
  - 4) Diffuse extragalactic light

Optical Airglow    Zodiacal Light

Infrared Airglow

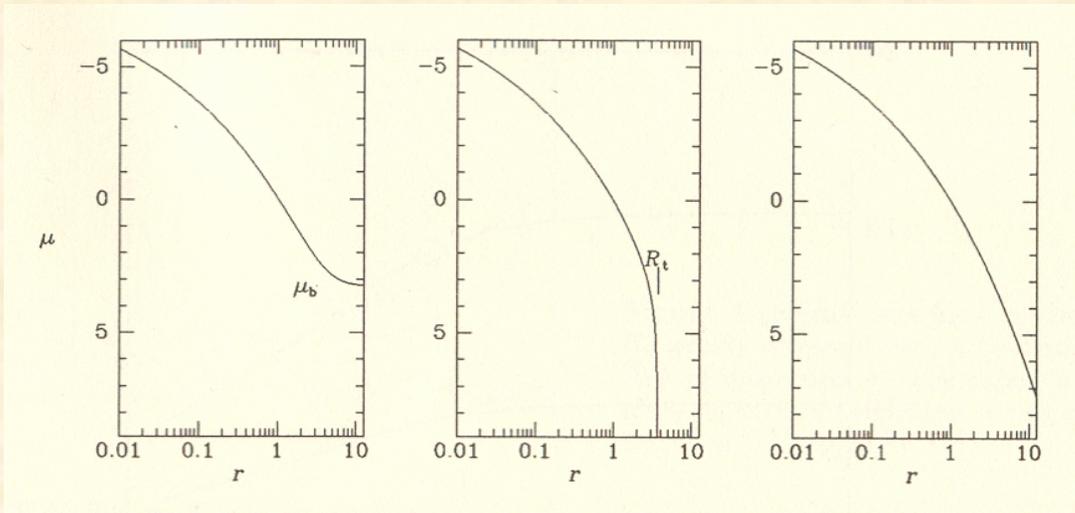


(Sparke & Gallagher, p. 19)



(Sparke & Gallagher, p. 44)

# Effects of error in sky subtraction:



(BM, p. 175)

under

over

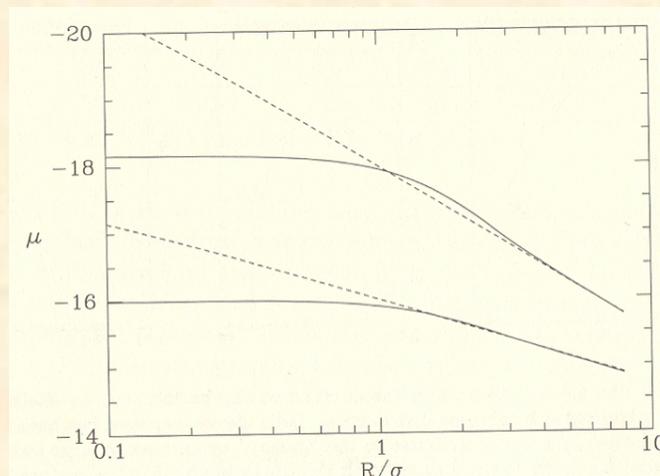
correct

# Effects of PSF due to telescope + seeing:

$\mu \sim R^{-1}$  →

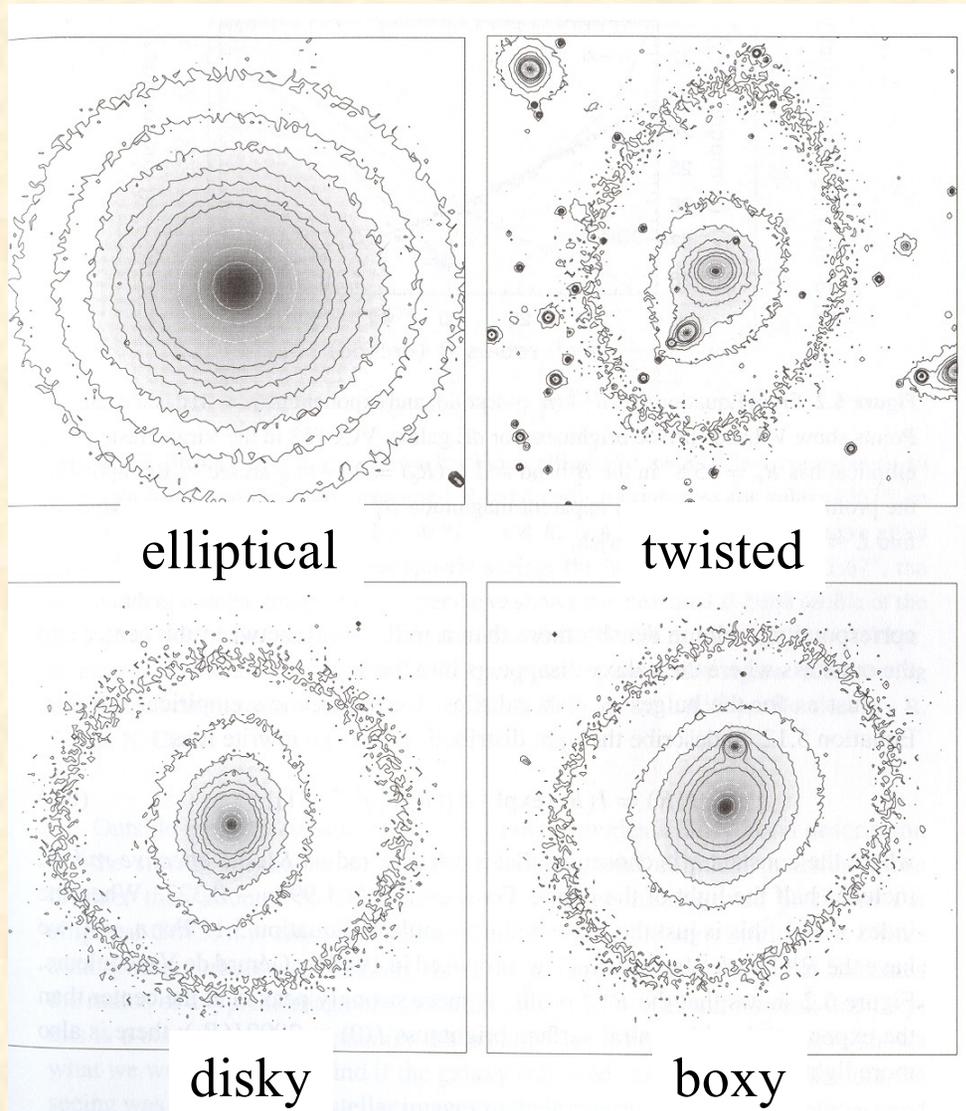
$\mu \sim R^{-0.5}$  →

$\sigma$  = dispersion of Gaussian PSF



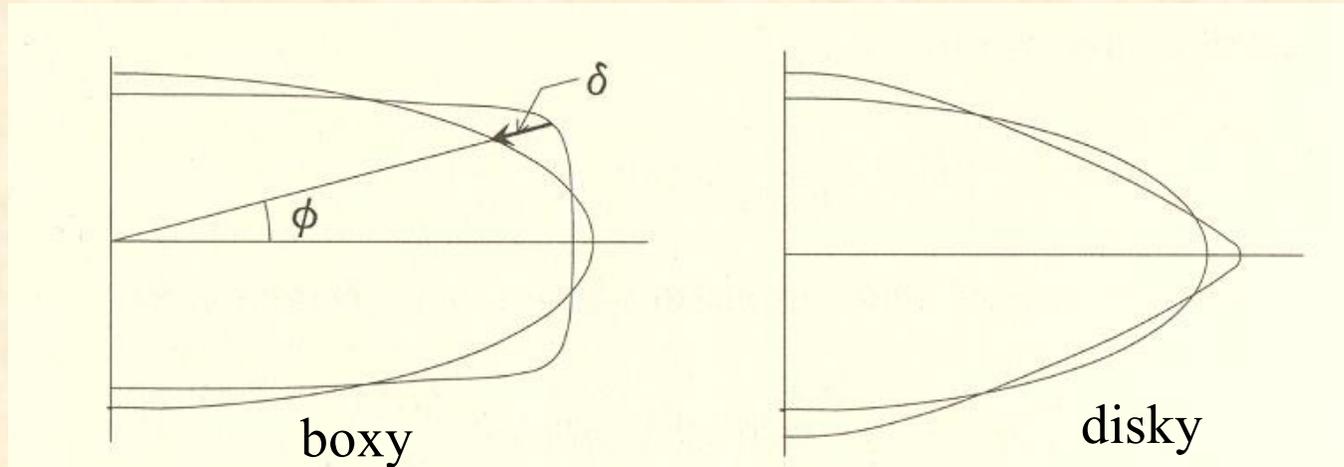
(BM, p. 176)

# Elliptical Galaxy Isophotes (Contours of equal $\mu_R$ )



(Sparke & Gallagher, p. 243)

- Boxy/disky isophotes often characterized by parameter  $a_4$
- Fit elliptical isophotes and then measure  $\delta$  as fct. of  $\Phi$



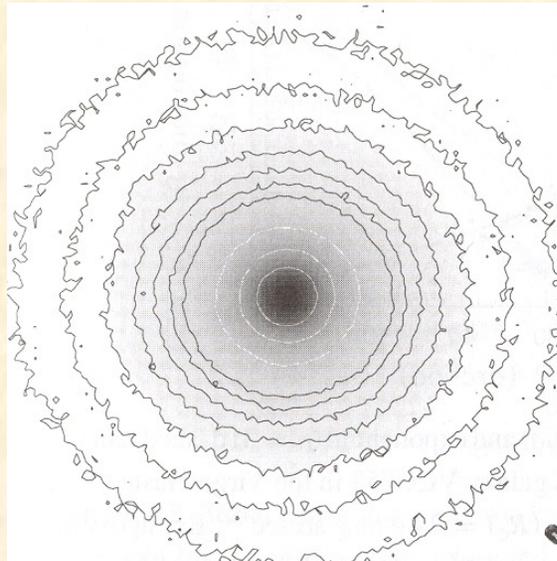
Express  $\delta$  as a Fourier series:

$$\delta(\phi) = \langle \delta \rangle + \sum_{n=1}^{\infty} a_n \cos(n\phi) + \sum_{n=1}^{\infty} b_n \sin(n\phi)$$

- Observational results: most  $a_n$  and  $b_n$  are negligible, except  $a_4$
- $a_4/a < 0 \rightarrow$  boxy,  $a_4/a > 0 \rightarrow$  disk (typical range:  $-0.02 \rightarrow +0.02$ )

# Galaxy Sizes

- Isophotal radius: distance from center at which a particular surface brightness is reached along the semi-major axis
  - De Vaucouleurs radius ( $R_{25}$ ): R at  $\mu_B = 25$
  - Holmberg radius: R at  $\mu_B = 26.5$
- Effective radius ( $R_e$ ): radius inside of which  $\frac{1}{2}$  of the light is emitted (depends on a model fit to brightness profile)

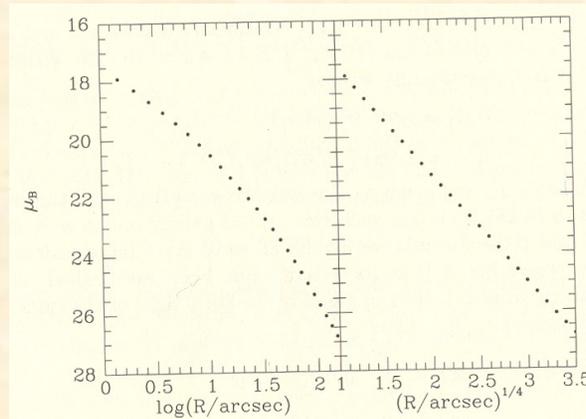


# Ellipticals/Bulges: Surface-Brightness Profiles

- Often fit with the **de Vaucouleurs  $R^{1/4}$  law**:  
$$I(R) = I_e \exp \{-7.67 [(R / R_e)^{1/4} - 1]\}$$
- Note this is of the form:  $\mu = a - bR^{1/4}$  (a and b are consts.)  
→ R = angular distance from the center
- $1/2$  of the light is emitted inside  $R_e$  if the galaxy is circularly symmetric
- Elliptical galaxies typically have values  $a_e$  and  $b_e$   
→  $R_e = (a_e b_e)^{1/2}$  ( $1/2$  light is inside ellipse with area  $\pi R_e^2$ )

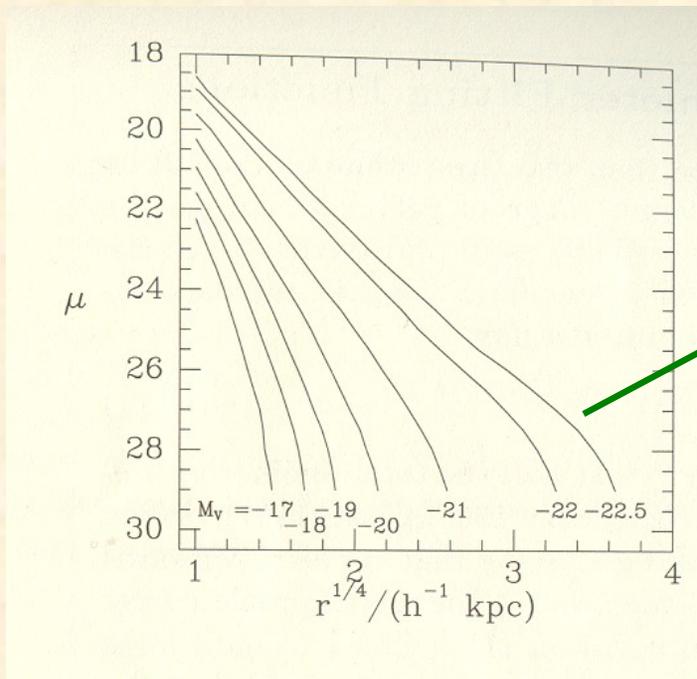
Ex) NGC 1700 (BM, p. 185)

Single power-law:  
( $I \sim R^\alpha$ )  
doesn't fit.



De Vaucouleurs law  
works well.

# Deviations from $R^{1/4}$ in $E'$ s – Function of Luminosity



(BM, p. 175)

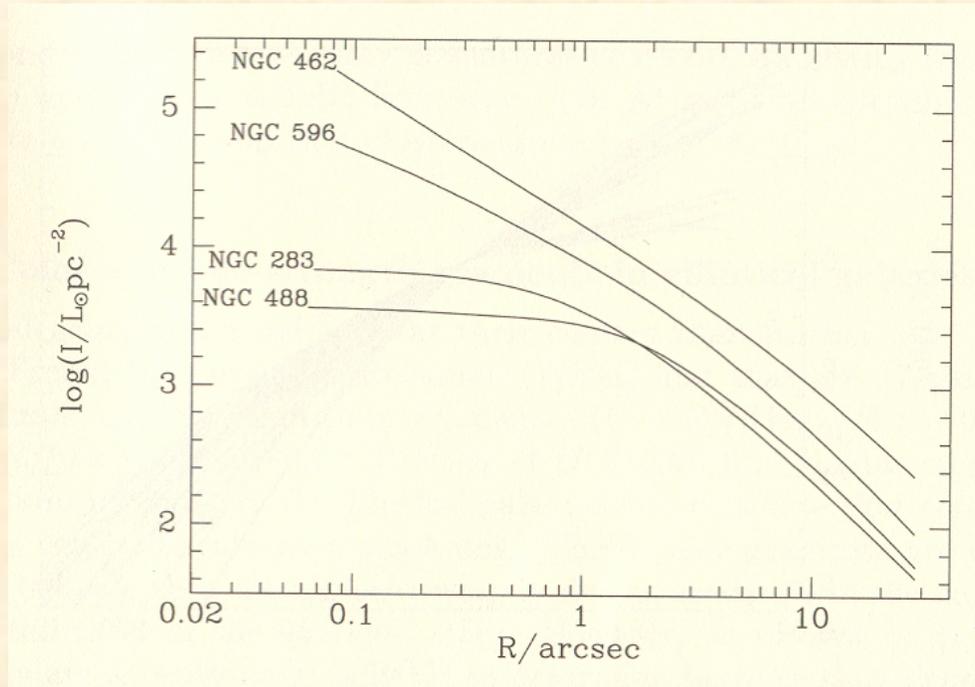


(HST/WFPC2 image of cD NGC 4881 in the Coma cluster, courtesy STScI)

- Two classes of dwarf Ellipticals (Kormendy & Djorgovski 1989):
  - Compact (M32): at low luminosity end of above graph
  - Diffuse: Best fit by **exponential law**:  $I(R) = I_d \exp(-R/R_d)$  (much flatter than  $R^{1/4}$ )

## Centers of Ellipticals (using *HST*)

- Surface brightness shows wide variation inside of 1".



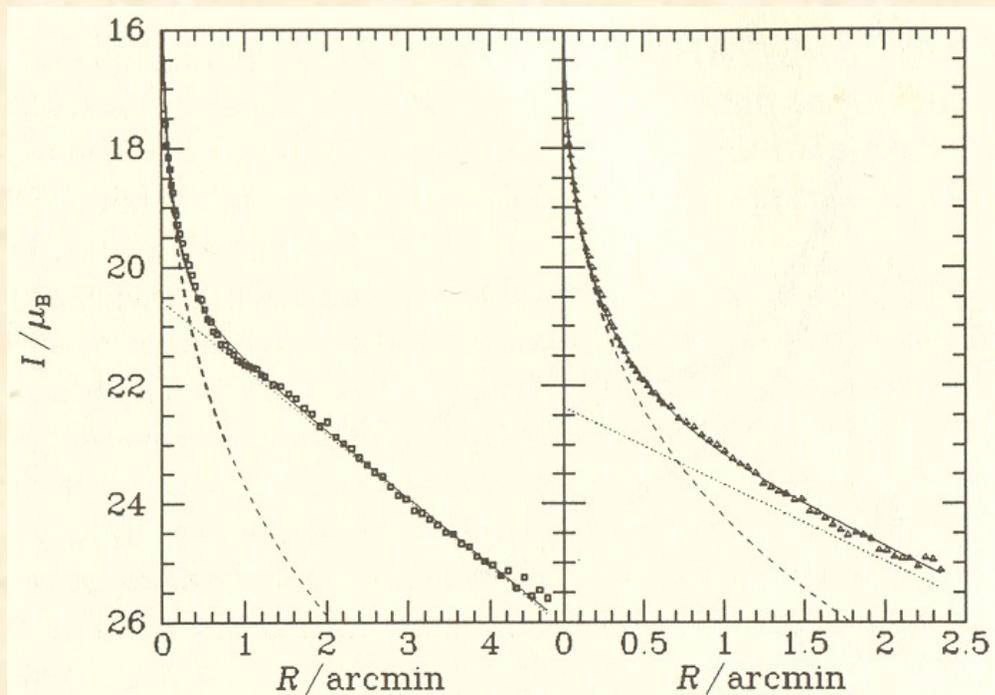
(BM, p. 191)

- Are cuspy profiles evidence for supermassive black holes?
  - Argument: BH's produce cuspy potentials and hence cuspy profiles (Lauer et al. 1991, 1992)

**No - black hole masses from kinematics show no correlation with "cusiness" (Kormendy & Richstone, 1995, ARAA, 33, 585-586)**

# Disks: Surface-Brightness Profiles

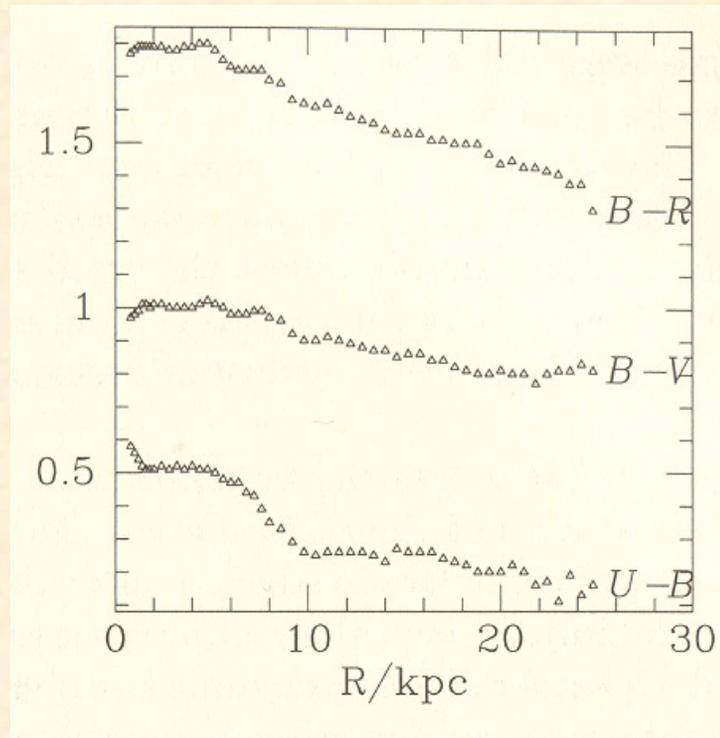
- Disks: Exponential law works:  $I(R) = I_d \exp(-R/R_d)$ 
  - Most disk galaxies have  $R_d$  in the range 1- 10 kpc
- Complications with surface photometry:
  - Bulge overlap, bars, dust lanes, spiral arms, young stars
  - Use red or near-IR if possible.



Combined  
disk/bulge fit

(Binney & Merrifield, p. 216)

# Color Gradients – M31



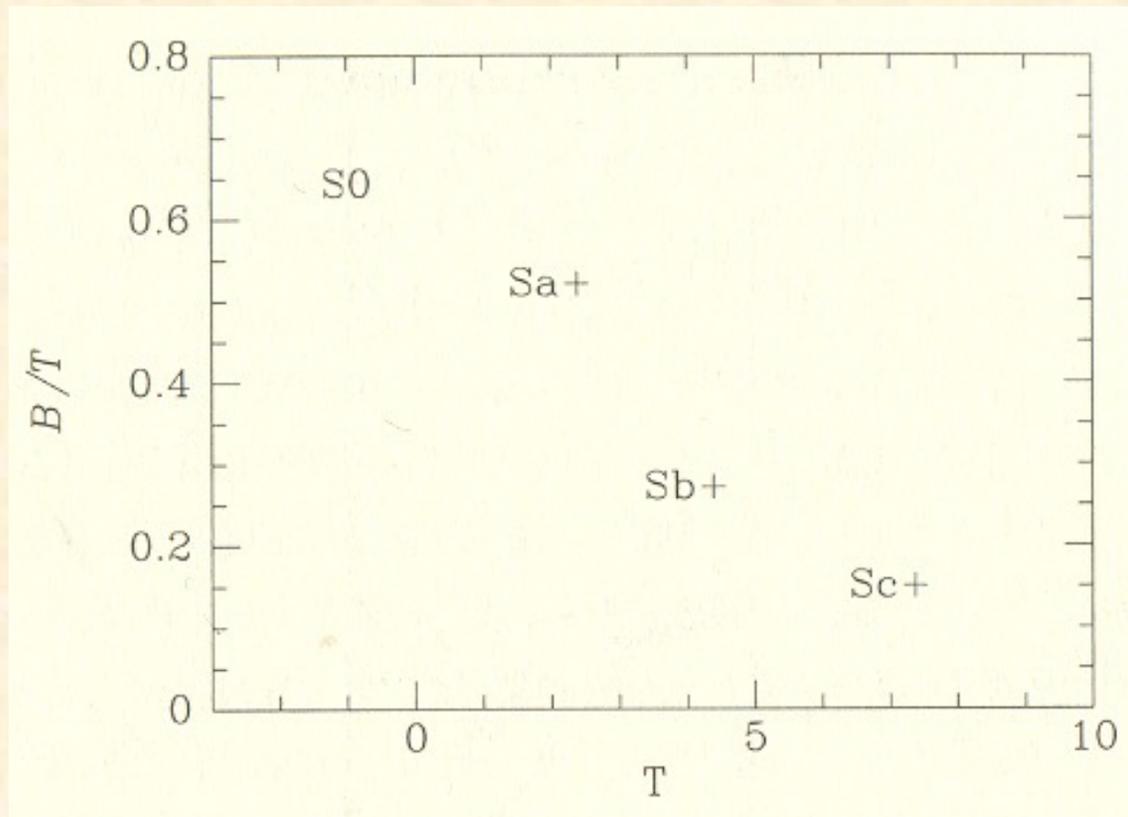
(Binney & Merrifield, p. 224)

- Spirals tend to get bluer with increasing distance from nucleus (as do ellipticals). Some combination of:
  - 1) Increasing # of hot, young stars.
  - 2) Decreasing metallicity.
- Exception: Starburst (“H II”) galaxies have rapid ongoing star formation in their nuclei.

# Bulges: Quantitative Correlation with Spiral Type

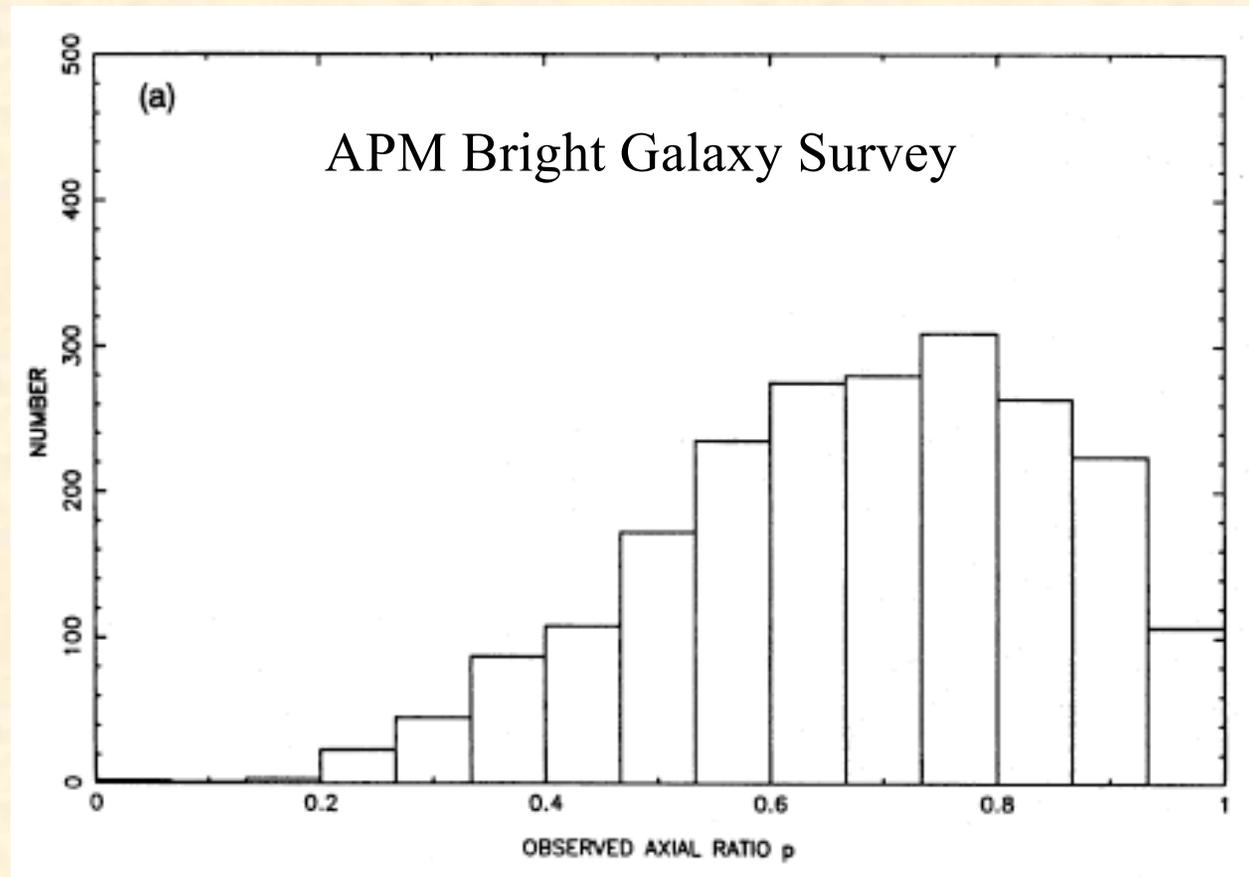
- Ratio of bulge to total luminosity from fits:

$$B / T = \frac{R_e^2 I_e}{R_e^2 I_e + R_d^2 I_d} = \frac{\text{bulge luminosity}}{\text{total luminosity}}$$



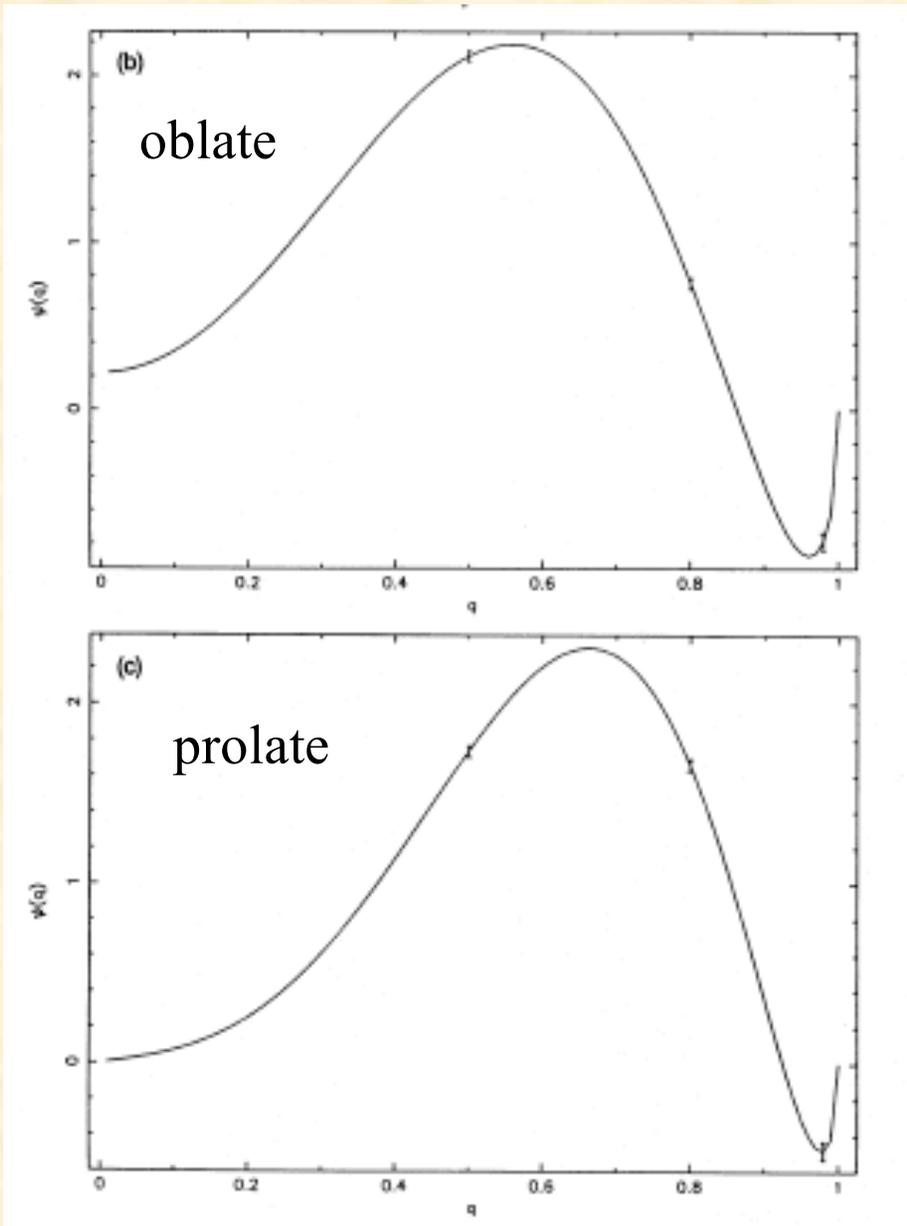
(Binney & Merrifield, p. 220)

# True Shapes - Ellipticals



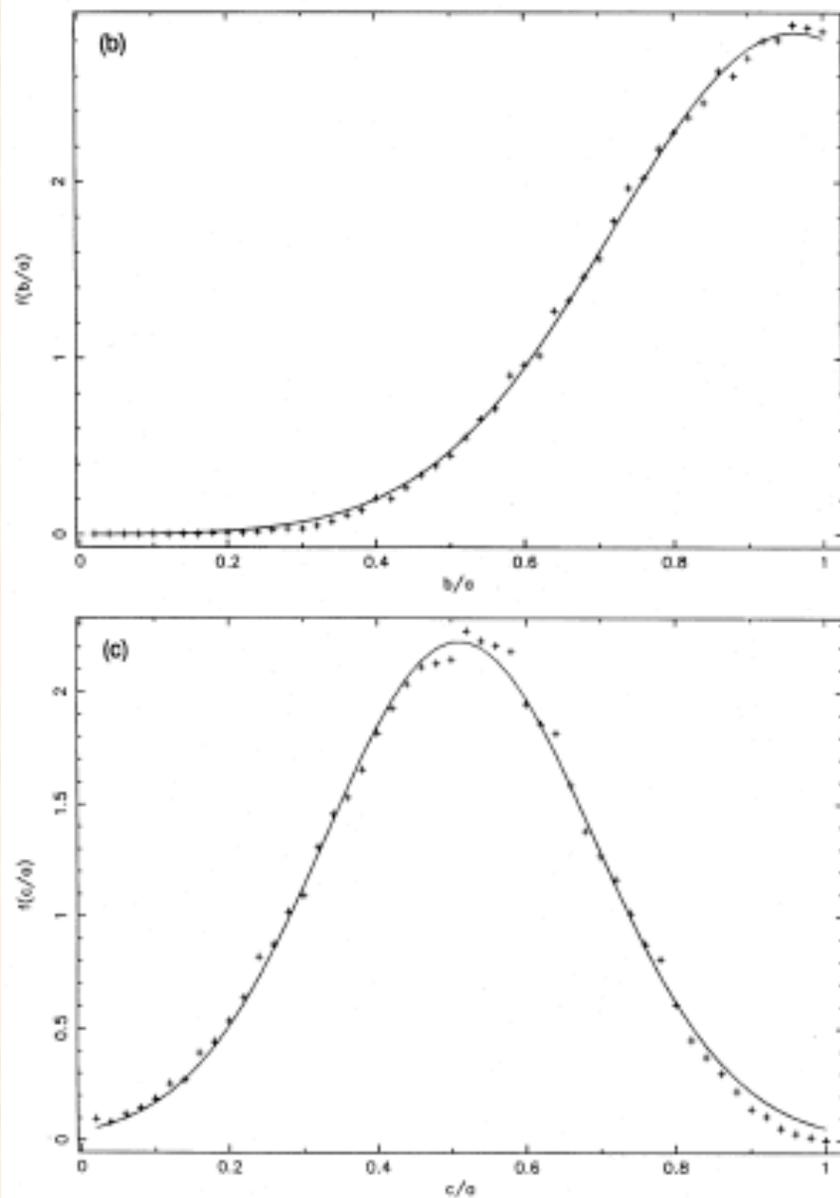
(Lambas et al. 1992, MNRAS, 258, 404)

- Assuming 3 axes of symmetry, are ellipticals oblate ( $a = b, c < a$ ), prolate ( $a = b, c > a$ ), or triaxial ( $a \neq b \neq c$ )?
- Need statistical studies of a large sample and assume that ellipticals are oriented randomly.



- From observed distribution of axial ratios  $\phi(p=b_{\text{obs}}/a_{\text{obs}})$ , one can determine the true distribution for  $\Psi(q = c/a)$  for oblate and prolate spheroids (Fall & Frank, 1993, AJ, 88, 1626)
- Both are unrealistic, since they give negative values at large  $q$  (spheres)
- Many ellipticals are likely *triaxial*.

(Lambas et al. 1992)



(Lambas et al. 1992)

- For triaxials, need to assume an underlying distribution (e.g., Gaussian)
- Ellipticals tend to be more *oblate* rather than *prolate*.
- Luminous E' s tend to be more triaxial (i.e., more asymmetric) than fainter ones (Tremblay & Merritt 1996).

# Bulges

- **Bulges:** “true” ellipticity:  $(\text{major-minor})/\text{major axis} = 0$  to  $0.7$ 
  - Flat bulges rotate more rapidly and have shallower brightness profiles  $\rightarrow$  “pseudobulges”
  - $\sim 25\%$  have boxy or even “peanut” appearance.
  - Would be seen as roughly elliptical from other angles

NGC 5746



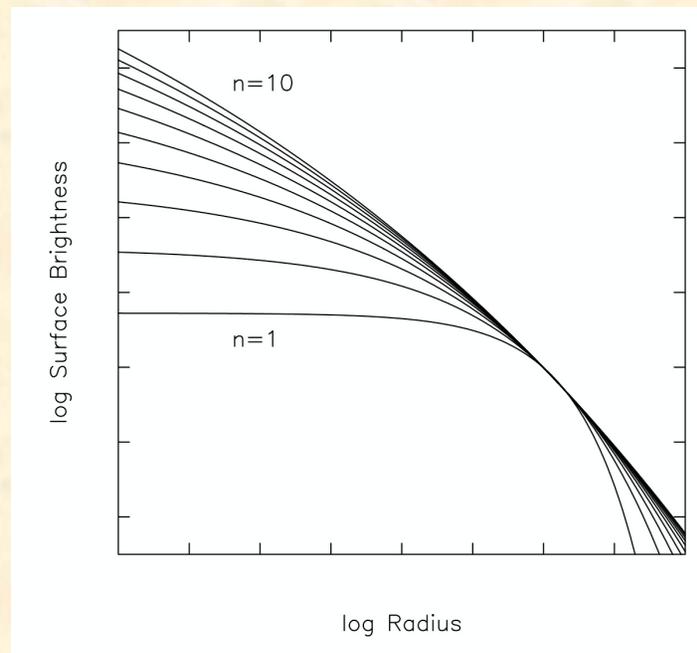
# Disks

- Even “face-on disks” can be slightly elliptical ( $e$  up to  $\sim 0.04$ ).
  - could be real or could be influence of spiral structure
- Surface brightness perpendicular to disk: use edge-on galaxies
  - $I(z) = I(R) \exp(-z/z_0)$  ( $z_0 = 0.01$  to  $0.1R_d$ )
- Luminosity density:
  - $j(r, z) = j_0 \exp(-r / r_d) \exp(-|z|/z_0)$  (double exponential)
- Most disks (like MW) have several components:
  - Ex) Optical and near-IR photometry of IC 2531 (Wainscoat et al. 1989): 3 components
    - 1) Thick disk,  $B - V = 0.78$ ,  $z_0 = r_d/12$
    - 2) Thin disk,  $B - V = -0.04$ ,  $z_0 = r_d/96$
    - 3) Dust disk,  $z_0 = r_d/48$

# Sersic Brightness Profile

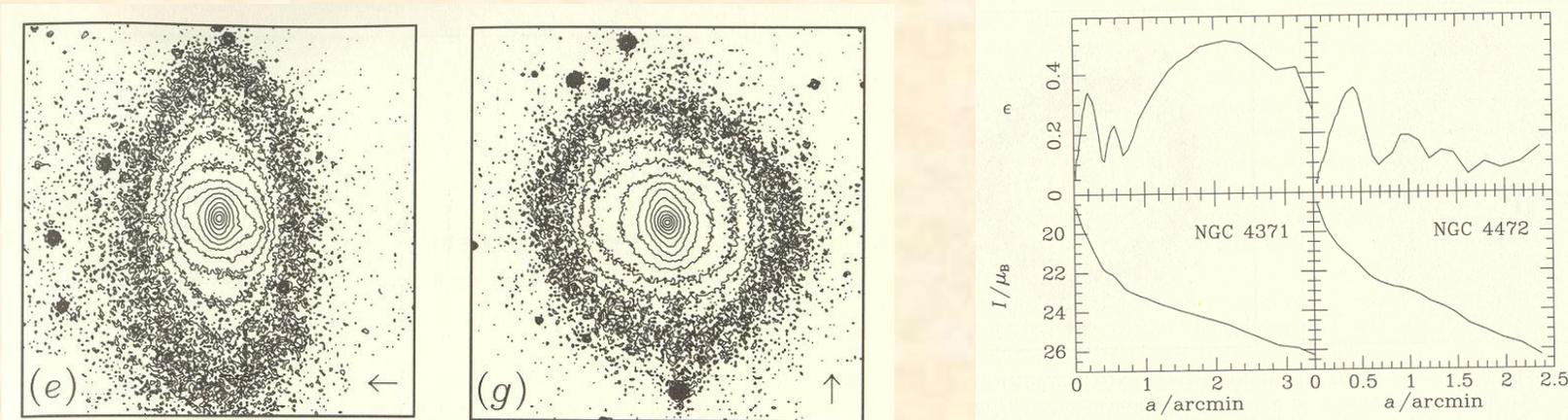
$$I = I_e \exp \left\{ -b_n \left[ \left( R / R_e \right)^{1/n} - 1 \right] \right\}$$

- $b_n$  chosen so that  $\frac{1}{2}$  luminosity inside  $R_e$
- $n = 4 \rightarrow$  de Vaucoulers law,  $n = 1 \rightarrow$  exponential
- pseudobulges – between 1 and 4
- How many free parameters?  $\rightarrow 3$



# Bars

- **Bars**: detected as deviation in ellipticity and bumps in brightness profiles



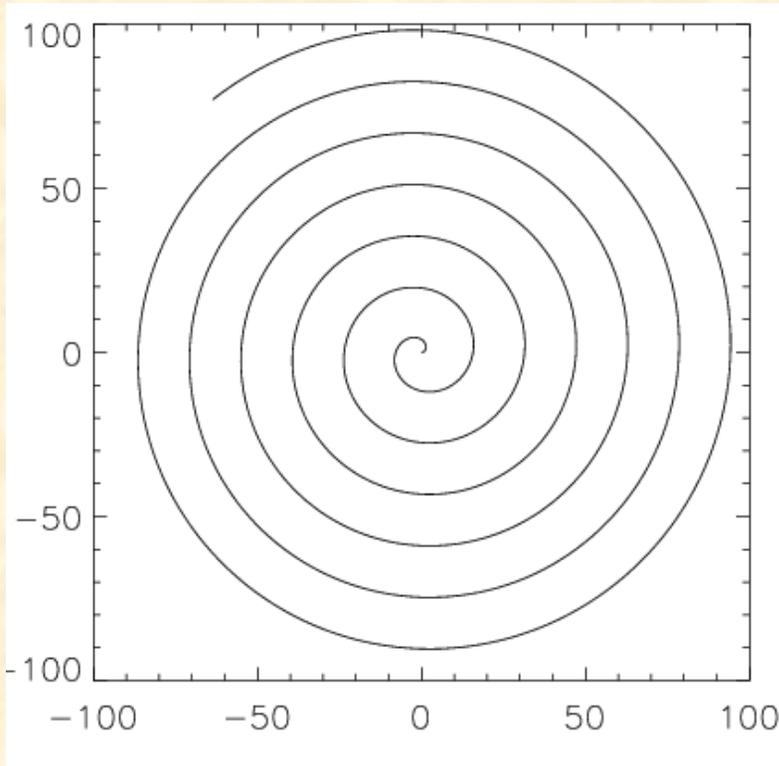
(Binney & Merrifield, p. 229, 230)

- Vertical structure: difficult to know, since bars can't be detected in edge-on galaxies
- Dynamical simulations: thin bars are unstable; tend to form peanut shapes with vertical dimensions similar to thick disk
- 75% of SBs have inner rings → bars, peanut-shaped bulges, and inner rings are somehow dynamically connected

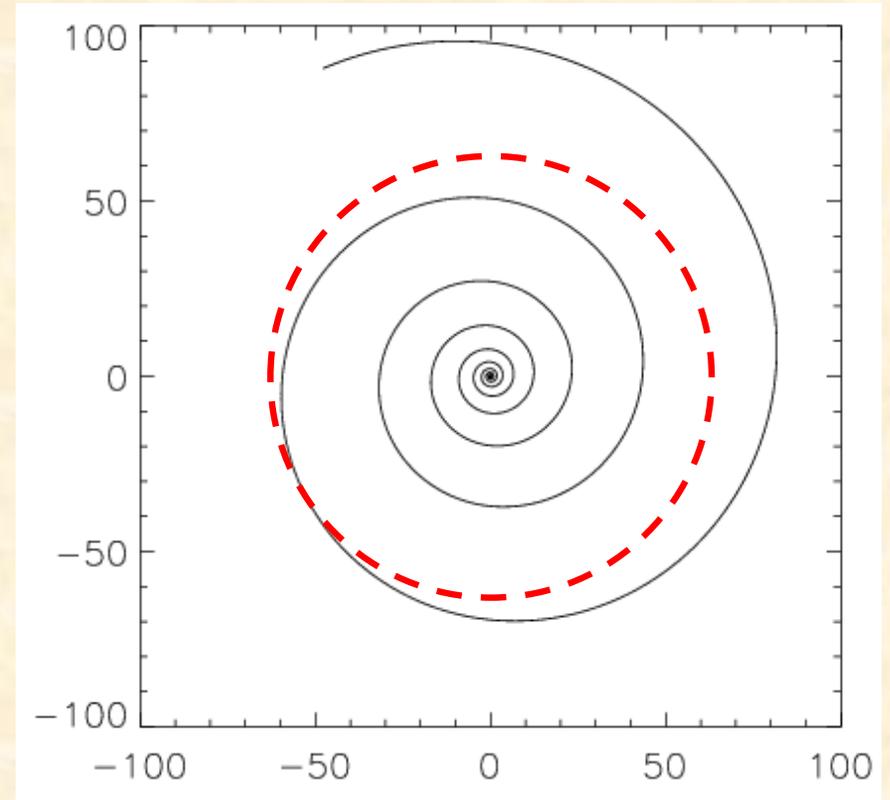
# Spirals

- Tend to be logarithmic in shape:  $\theta \sim \ln(R)$  (polar coords.)

$$\theta \sim R$$



$$\theta \sim \ln(R)$$



Pitch angle ( $\psi$ ) = angle between arm and tangent to circle at R  
- ranges from  $5^\circ$  (Sa) to  $30^\circ$  (Sc to Sd)

# Spirals

- Bluer than surroundings → active star formation
- ~10% are grand design: tend to have a bar and/or outer satellite (M51)
- Kinematics: Spiral arms rotate as if they are “winding up”.

How can you tell which side of a spiral galaxy is closer?

→ Take a spectrum to get radial velocities + spiral arms wind

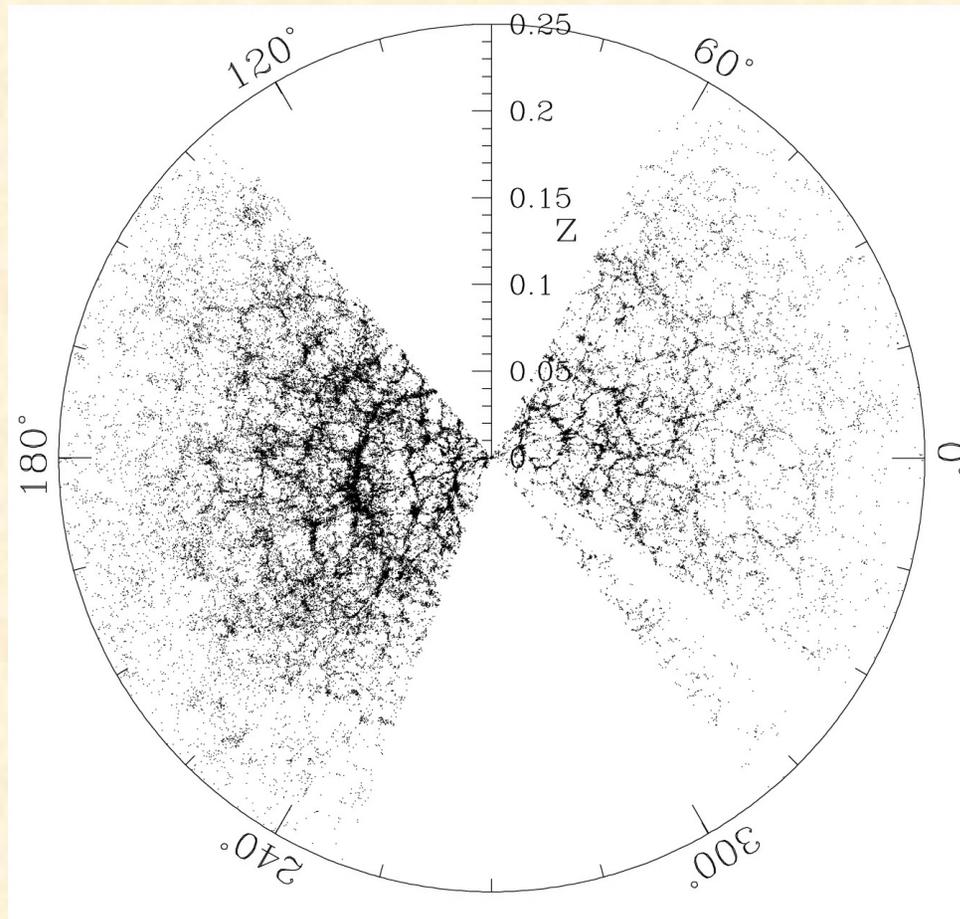


## Another way to tell which side is closer



Near side occults bulge (works for more edge-on spirals)

# Galaxy Luminosity Functions



(SDSS Wedge (Blanton, et al. 2003, ApJ, 592, 819))

- How do we get the # of galaxies at each luminosity?
- Need imaging + spectroscopic surveys (e.g. SDSS, 2DF)
- Integrate surface brightness  $\rightarrow$  flux,  $z \rightarrow$  distance, luminosity

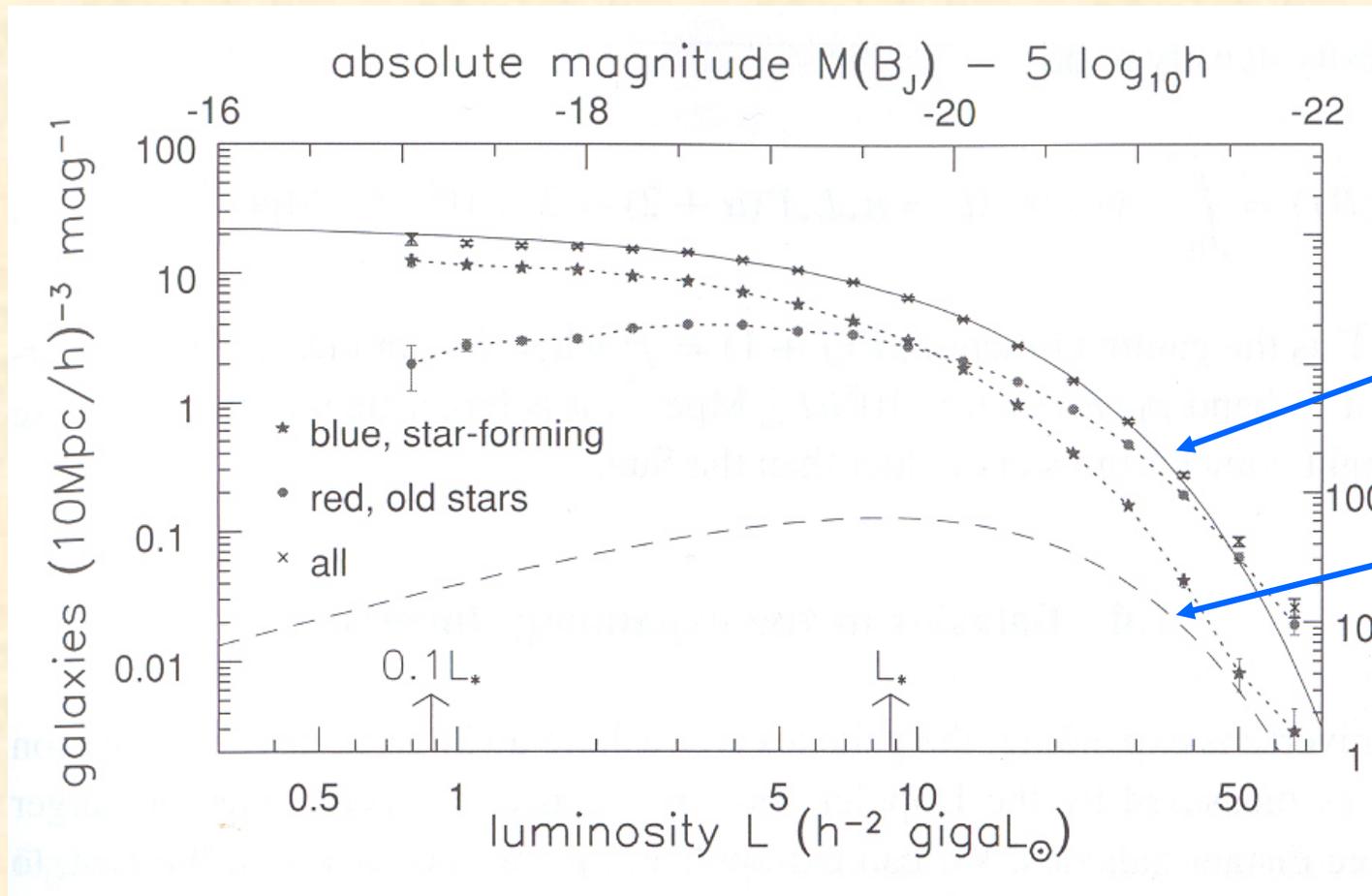
# Galaxy Luminosity Functions

- $\Phi(L) dL$  – # of galaxies with luminosities between  $L$  and  $L + dL$  (or  $M$  and  $M + dM$ ) per  $\text{Mpc}^3$
- Need to correct for Malmquist bias: can only count galaxies to a limiting magnitude (miss distant, faint galaxies)
- $\Phi$  often described by the Schechter Luminosity Function:

$$\Phi(L) = \frac{n^*}{L^*} \left( \frac{L}{L^*} \right)^\alpha \exp\left( \frac{-L}{L^*} \right)$$

- $n^*$  = normalization constant  $\approx 0.02 h^3 \text{ Mpc}^{-3}$   
(where  $h = H_0/100 \text{ km s}^{-1} \text{ Mpc}^{-1} = 0.73$ )
- $L^*$  = turnover luminosity at the high end  $\approx 9 \times 10^9 h^{-2} L_\odot$
- $\alpha$  = slope at low-luminosity end  $\approx -0.4$

# Luminosity Function - Data



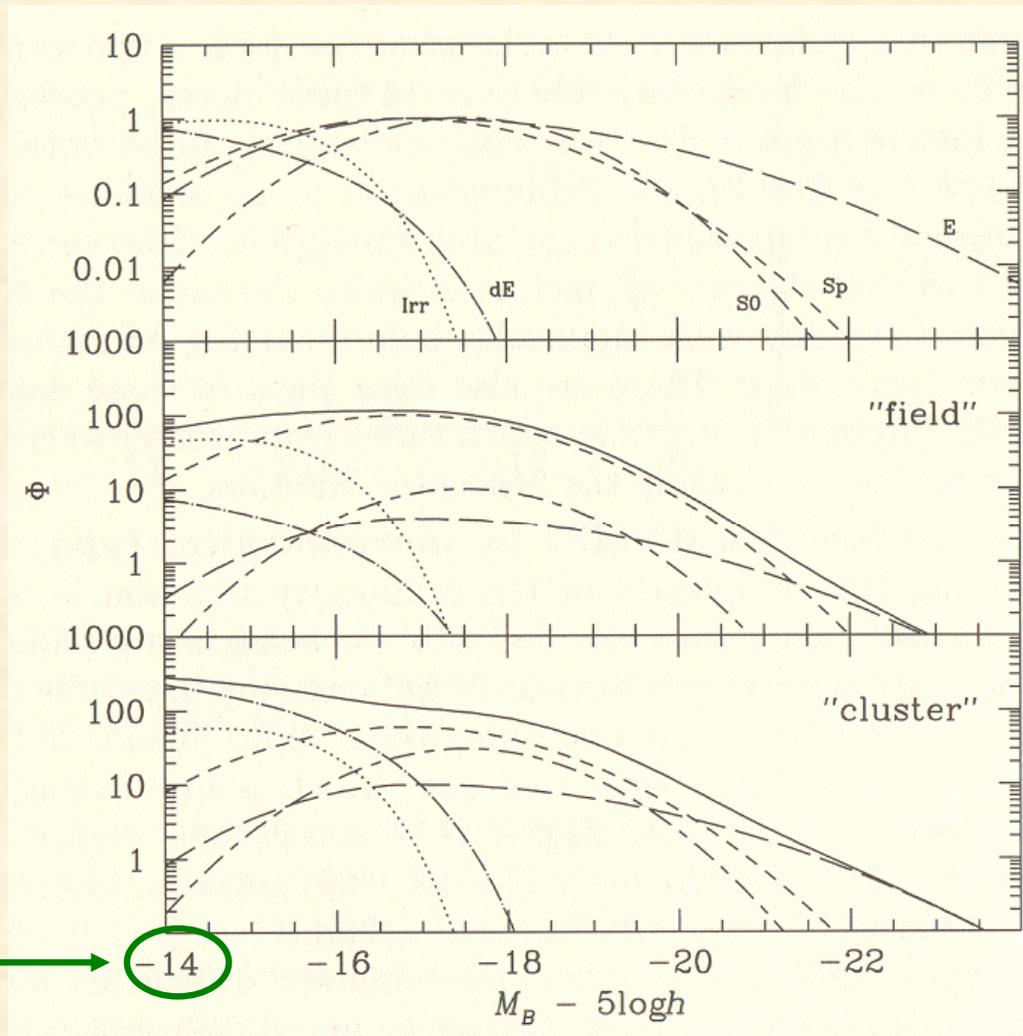
$\Phi$

$\Phi_x (L/L^*)$

(2dF Survey - Sparke & Gallagher, p. 45)

- Giant E's dominate at high end
- Most of the luminosity comes from bright galaxies

# Luminosity Functions by Morphological Type



← arbitrary normalization

← correct relative normalization

(Binney & Merrifield p. 168)

- dE's and Irr's dominate at low luminosities
- Brightest galaxies are giant E's and cD's in centers of clusters
- Spirals are less common in clusters (and their numbers increase with distance from center)

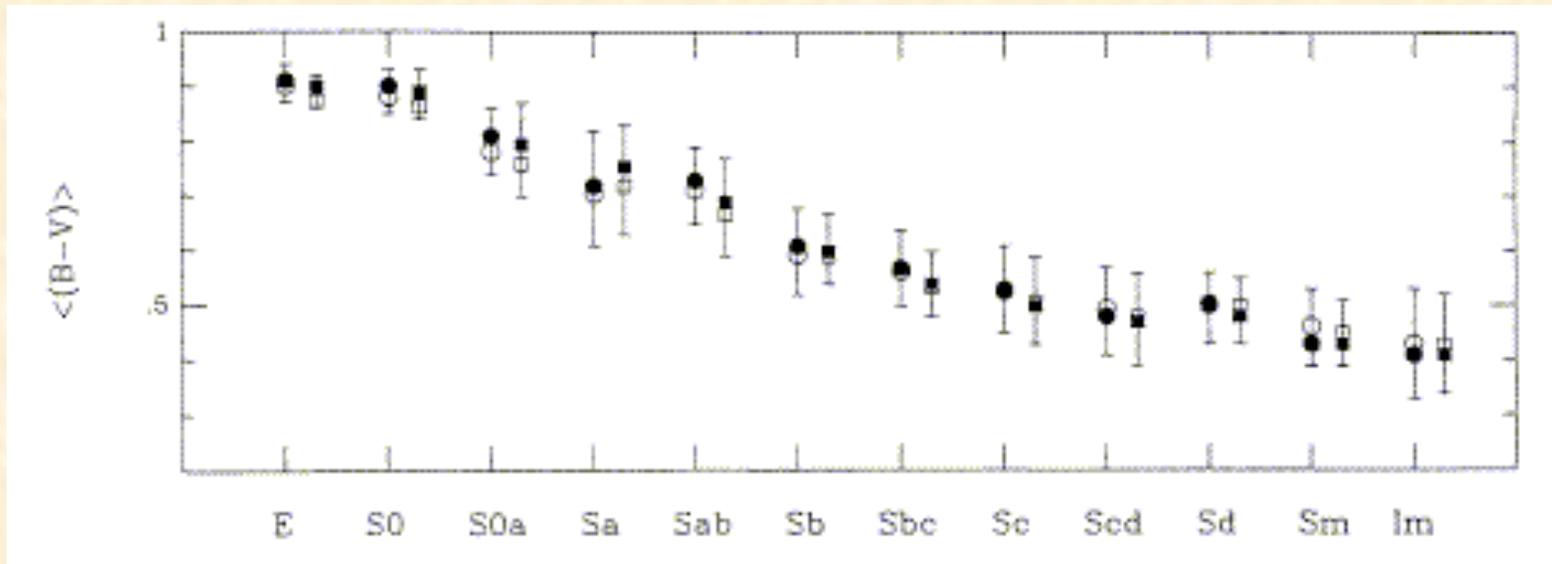
# Local Group

Name	Alternate Name	Coordinates		Type	Distance (kpc)	$M_V$
		RA (1950)	Dec			
M31	NGC 224	00 40.0	+40 59	Sb	725	-21.1
Milky Way	Galaxy	17 42.4	-28 55	Sbc	8	-20.6
M33	NGC 598	01 31.1	+30 24	Sc	795	-18.9
LMC		05 24.0	-69 48	Irr	49	-18.1
IC 10		00 17.7	+59 01	Irr	1250	-17.6
NGC 6822	DDO 209	19 42.1	-14 56	Irr	540	-16.4
M32	NGC 221	00 40.0	+40 36	dE2	725	-16.4
NGC 205		00 37.6	+41 25	dE5	725	-16.3
SMC		00 51.0	-73 06	Irr	58	-16.2
NGC 3109	DDO 236	10 00.8	-25 55	Irr	1260	-15.8
NGC 185		00 36.2	+48 04	dE3	620	-15.3
IC 1613	DDO 8	01 02.2	+01 51	Irr	765	-14.9
NGC 147	DDO 3	00 30.5	+48 14	dE4	589	-14.8
Sextans A	DDO 75	10 08.6	-04 28	Irr	1450	-14.4
Sextans B	DDO 70	09 57.4	+05 34	Irr	1300	-14.3
WLM	DDO 221	23 59.4	-15 45	Irr	940	-14.0
Sagittarius		18 51.9	-30 30	dSph/E7	24	-14.0
Fornax		02 37.8	-34 44	dSph/E3	131	-13.0
Pegasus	DDO 216	23 26.1	+14 28	Irr	759	-12.7
Leo I	DDO 74	10 05.8	+12 33	dSph/E3	270	-12.0
Leo A	DDO 69	09 56.5	+30 59	Irr	692	-11.7
And II		01 13.5	+33 09	dSph/E3	587	-11.7
And I		00 43.0	+37 44	dSph/E0	790	-11.7
SagDIG		19 27.9	-17 47	Irr	1150	-11.0
Antlia		10 01.8	-27 05	dSph/E3	1150	-10.7
Sculptor		00 57.6	-33 58	dSph/E3	78	-10.7
And III		00 32.6	+36 12	dSph/E6	790	-10.2
Leo II	DDO 93	11 10.8	+22 26	dSph/E0	230	-10.2
Sextans		10 10.6	-01 24	dSph/E4	90	-10.0
Phoenix		01 49.0	-44 42	Irr	390	-9.9
LGS 3		01 01.2	+21 37	Irr	760	-9.7
Tucana		22 38.5	-64 41	dSph/E5	900	-9.6
Carina		06 40.4	-50 55	dSph/E4	87	-9.2
Ursa Minor	DDO 199	15 08.2	+67 23	dSph/E5	69	-8.9
Draco	DDO 208	17 19.2	+57 58	dSph/E3	76	-8.6

(Binney & Merrifield p. 168)

- Many galaxies with low luminosities and low surface brightnesses
- A 3D view can be found at <http://www.atlasoftheuniverse.com/localgr.html>

# Global Correlations: Color vs. Type



(Roberts and Haynes, 1994 ARA&A 32, 115)

Trends:

Ellipticals  $\rightarrow$  bulges  $\rightarrow$  disks

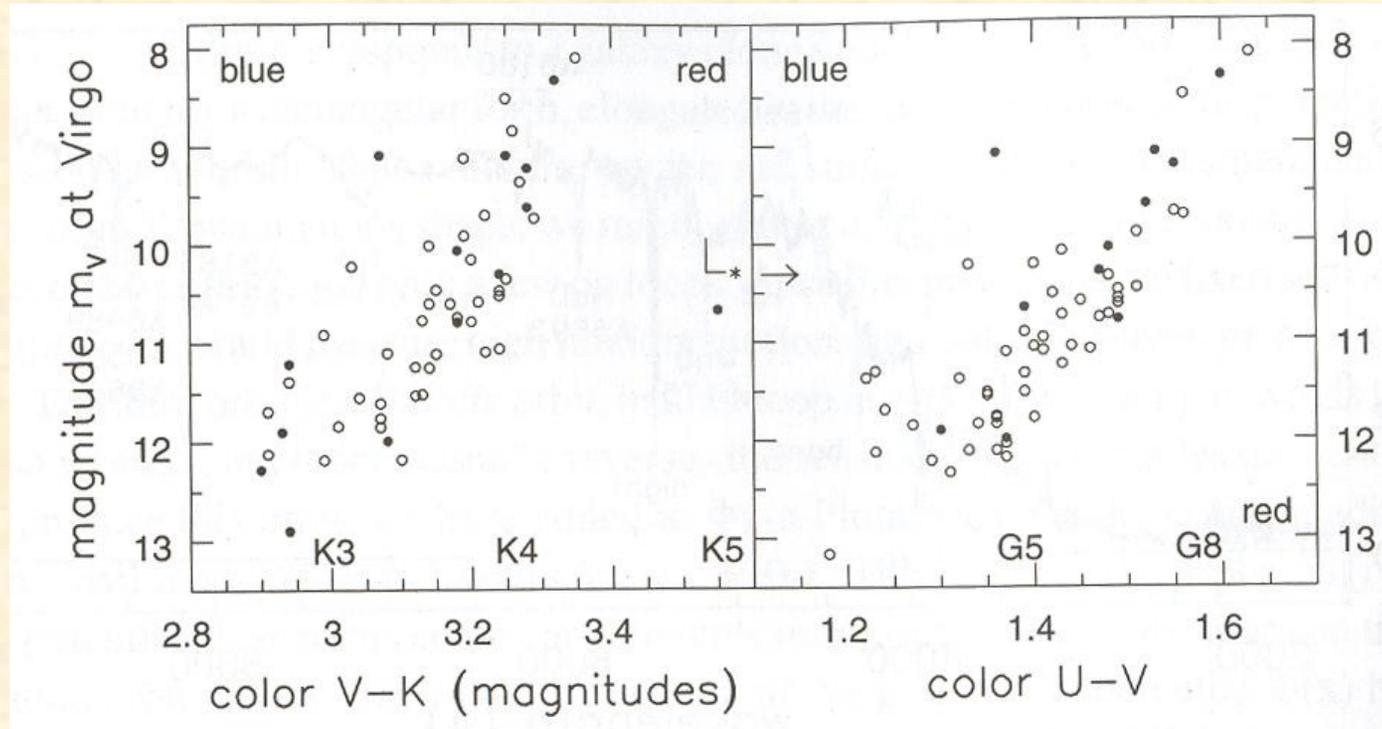
red  $\rightarrow$  blue

old average population  $\rightarrow$  young

low metallicity  $\rightarrow$  high

- Oversimplification; e.g., metallicity in the Galactic bulge decreases with radius (from above solar to below)
- Difficult to separate effects of stellar populations, metallicity, and dust  $\rightarrow$  use spectroscopy

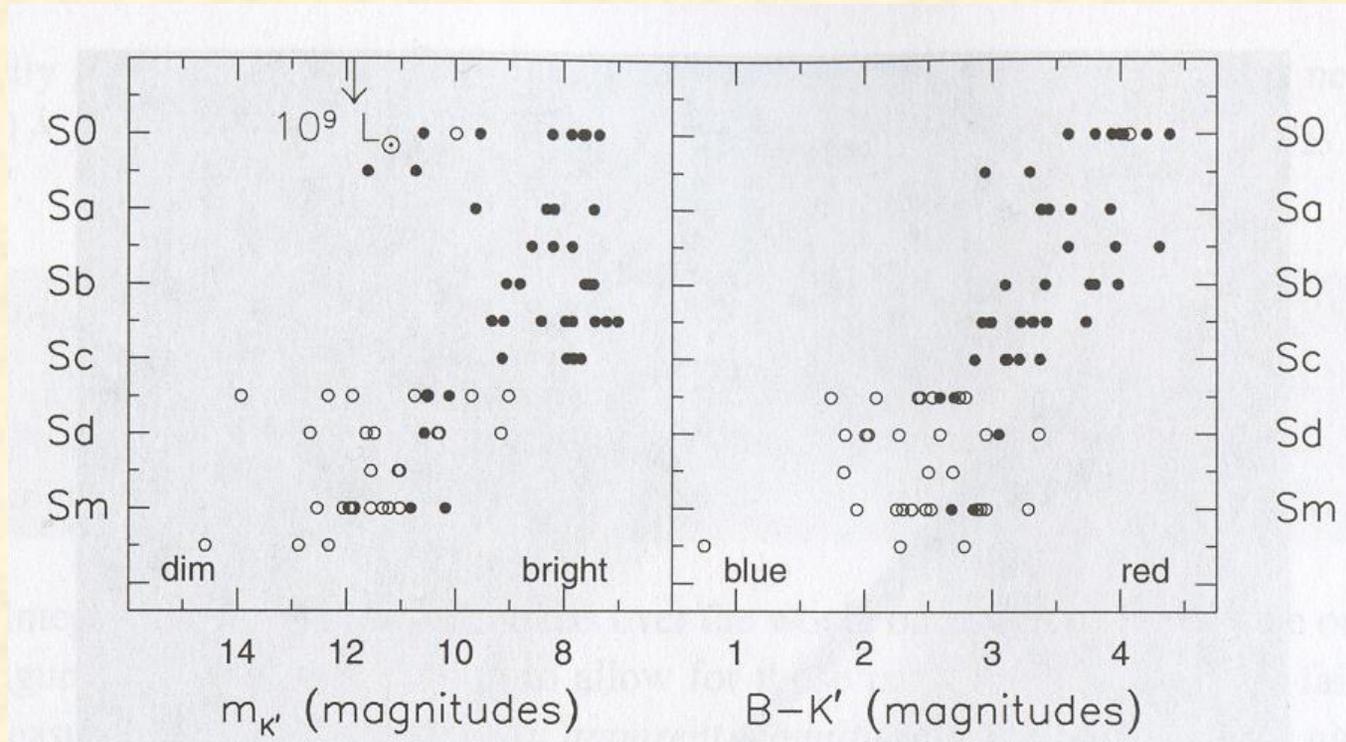
# Ellipticals: Color vs. Luminosity



(Sparke & Gallagher, p. 269)

- Brighter ellipticals are redder
  - higher metallicities, rather than older stellar populations (confirmed from spectra of Fe, Mg absorption lines)

# Global Correlations (Spirals)



(Galaxies in Ursa Major Group; Sparke & Gallagher, p. 201)

- Earlier types have **1) higher luminosities**, **2) higher  $I_R$** , **3) redder colors**, **4) lower H I mass**, **5) less star formation**, and **6) fewer H II regions**
  - Due in part to prominence of bulge. (1, 2, 3)
  - Also, less gas available for star formation in the disk at present epoch (3, 4, 5, 6)