ASTRONOMY 8400 – Spring 2024 Homework Set 1 – "Answers"

1. a)
$$1+z = \sqrt{\frac{1+\beta}{1-\beta}} \rightarrow (1+z)^2 = \frac{1+\beta}{1-\beta}$$
$$(1+\beta) = (1+z)^2 (1-\beta) = (1+z)^2 - (1+z)^2 \beta$$
$$\beta + \beta (1+z)^2 = (1+z)^2 - 1$$
$$\beta = \frac{(1+z)^2 - 1}{(1+z)^2 + 1}$$

b) You can solve this algebraically or graphically. For a 1% error:

$$\frac{z-\beta}{z} = 0.01 \quad \text{so} \quad \frac{\beta}{z} = 0.99$$

$$\frac{1}{z} \frac{(1+z)^2 - 1}{(1+z)^2 + 1} = 0.99$$

$$\frac{z^2 + 2z}{z^2 + 2z + 2} = 0.99z$$

$$0.99z^3 + 2(0.99)z^2 + (2)(0.99)z = z^2 + 2z$$

$$0.99z^2 + 1.98z + 1.98 = z + 2$$

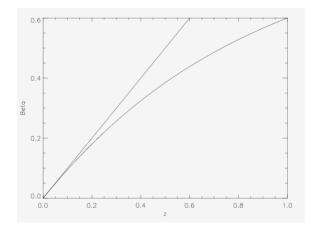
$$0.99z^2 + 0.98z - 0.02 = 0$$

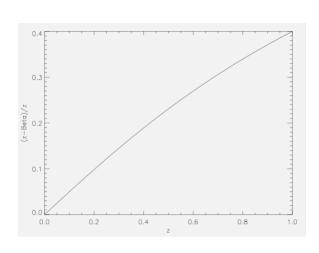
Using the quadratic equation:

$$z = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

z = 0.02 (the other solution is -1.01, which is not valid)

For a 10% error, use the same formalism to get: z = 0.2 (the other solution is -1.09, which is not valid)





- c) The Hubble flow velocity would have to be $\sim 6000 \text{ km s}^{-1}$. z = v/c = 0.02, Galaxies with z < 0.02 are affected most severely.
- 2. a) NGC 4151: RA = 12h10m32.6s + 39d24m21s (J2000)
 - from "Optical Positions of Seyfert Galaxies", Clements, E.D. 1981, MNRAS, 197, 829.
 - b) z = 0.003319, cz = 995 km/s (heliocentric)
 - from H I 21-cm emission from host galaxy, Third Reference Catalog of Bright Galaxies (RC3), deVaucouleurs et al. (1991)
 - c) Distance from z: $D = cz/H_0 = 13.6$ Mpc, where $H_0 = 73$ km/sec/Mpc Corrected z to CMB frame: D = 17.0 Mpc

Distance from other techniques (average) = 14.1 Mpc

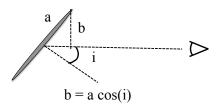
- huge variation depending on technique!
- d) R'SAB(rs)ab Spiral galaxy with weak bar, outer pseudo-ring, inner ring/spiral, early type (deVaucouleurs et al. 1991) Seyfert 1.5

e)
$$\theta = \frac{r}{D} = \frac{1 \text{ kpc}}{13.6 \times 10^3 \text{ kpc}} = 7.35 \times 10^{-5} \text{ rad} \left(\frac{206,265 \text{ arcsec}}{1 \text{ rad}}\right) = 15 \text{ arcsec}$$
Scale = 15 arcsec/kpc

From

NED: Scale = 12 arcsec/kpc (using CMB correction)

- f) Major, minor axes = 6.3×4.5 arcmin, 31×22 kpc (from POSS)
- g) Inc = $\cos^{-1}(a/b) = 44^{\circ}$



- h) E(B-V) = 0.028 mag (from Schlegel et al. maps of IR emission from Galactic dust)
- 3. a) Assume you are looking at a torus from different inclination angles along a hemisphere. At a given distance (r), the probability of viewing at angle θ is proportional to the solid angle determined by an annulus perpendicular to the disk with width $d\theta$. So: $dP(\theta) = \sin(\theta)d\theta$ (probability increases with increasing θ)

The probability of observing between angles θ_1 and θ_2 is:

$$P = \int_{\theta_1}^{\theta_2} \sin\theta \ d\theta / \int_{0}^{\pi/2} \sin\theta \ d\theta$$

$$P = \cos(\theta_1) - \cos(\theta_2)$$

The probability of observing a certain ratio of Seyfert 2s to Seyfert 1s is:

$$x = \frac{\text{\# Seyfert 2s}}{\text{\# Seyfert 1s}} = \frac{N_2}{N_1}$$

$$P = \frac{N_2}{N_1 + N_2} \rightarrow P = \frac{x}{x+1}$$

$$P = \cos(\theta_{\min}) - \cos(90) = \cos(\theta_{\min})$$

$$\theta_{\min} = \cos^{-1}(P) = \cos^{-1}\left(\frac{x}{x+1}\right)$$

For
$$x = 1$$
, $\theta_{min} = 60^{\circ}$

For
$$x = 2$$
, $\theta_{min} = 48^{\circ}$

For
$$x = 3$$
, $\theta_{min} = 41^{\circ}$

