

# Interferometry & Asteroseismology of Delta Scuti Stars: 44 Tau and 29 Cyg



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# Asteroseismology of Eclipsing Binaries

- **Gamma Dor stars**

Guo, Gies, & Matson 2017, ApJ, in press.

- **Post-mass transfer Delta Scuti stars**

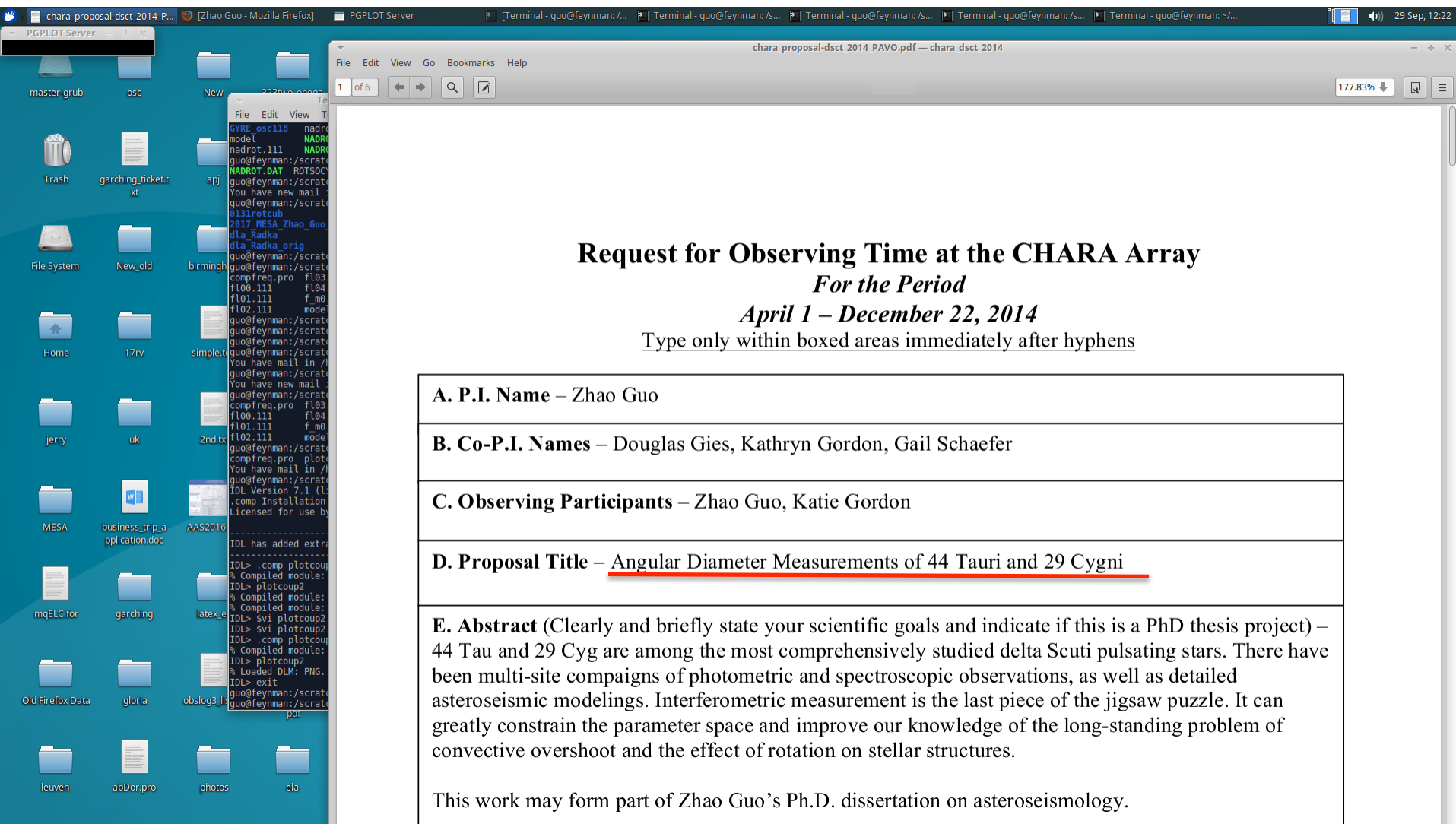
Guo, Gies, Matson, et al. 2017, ApJ, 834, 59

- **Normal Delta Scuti stars**

Guo, Gies, Matson, Garcia Hernandez. 2016, ApJ, 826, 69

- **Heartbeat stars with tidally excited oscillations**

Guo, Gies, & Fuller 2017, ApJ, 837, 114



# 44 Tau

Spectroscopy,  
mode ID: Zima 07

Multi-site photometry:  
Rodler 03, Antoci 07



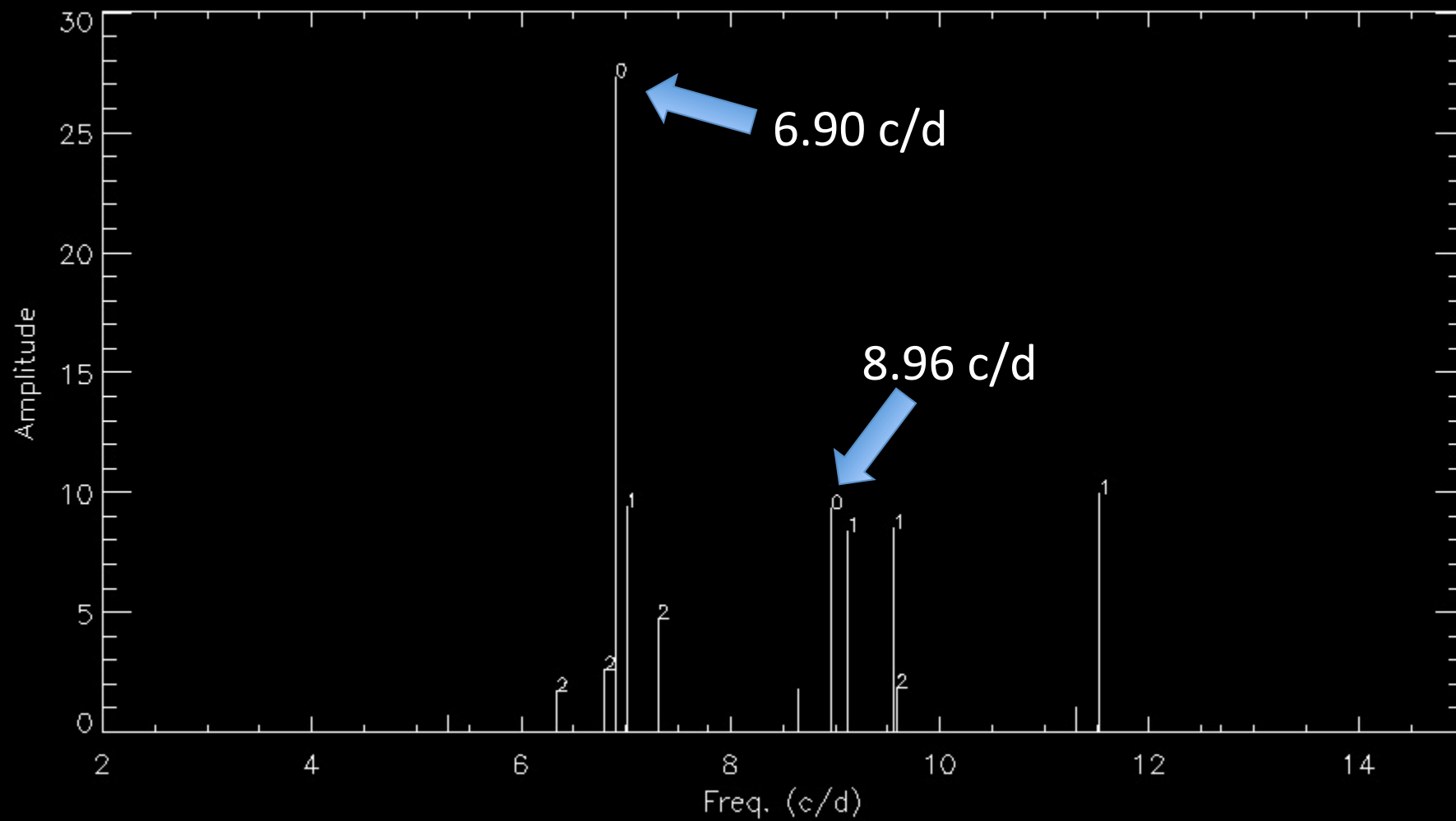
Seismic modeling:  
Lenz 08,10

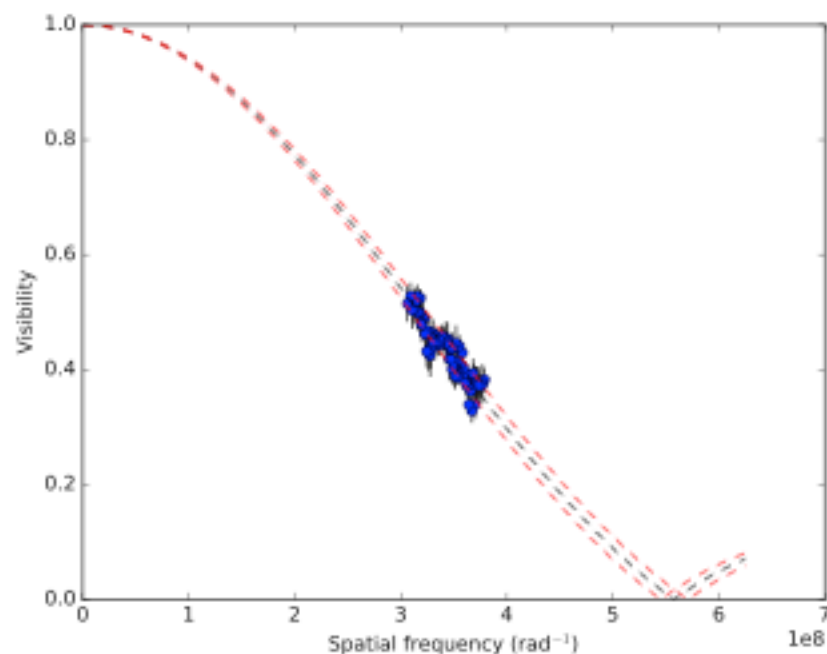
*Interferometry*

- > evolved
- > Intrinsic slow rotator:  $V_{eq} \leq 5 \text{ km/s}$     -> Non-rotating models OK
- > Solar metallicity
- $T_{\text{eff}} = 6900 \pm 100 \text{ K}$ ,  $\log g = 3.6 \pm 0.1$
- > 15 frequencies, most with mode identification



# 44 Tau FT

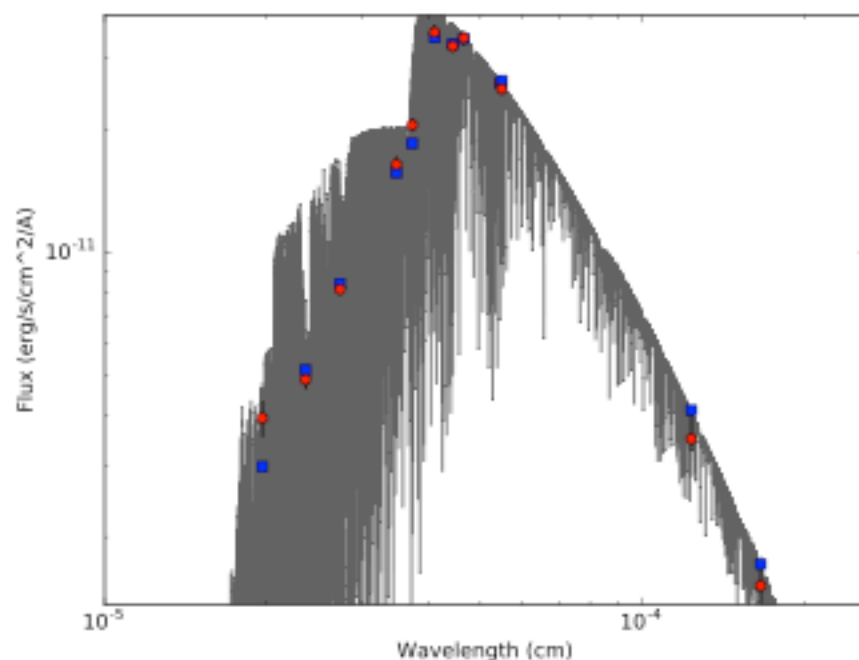




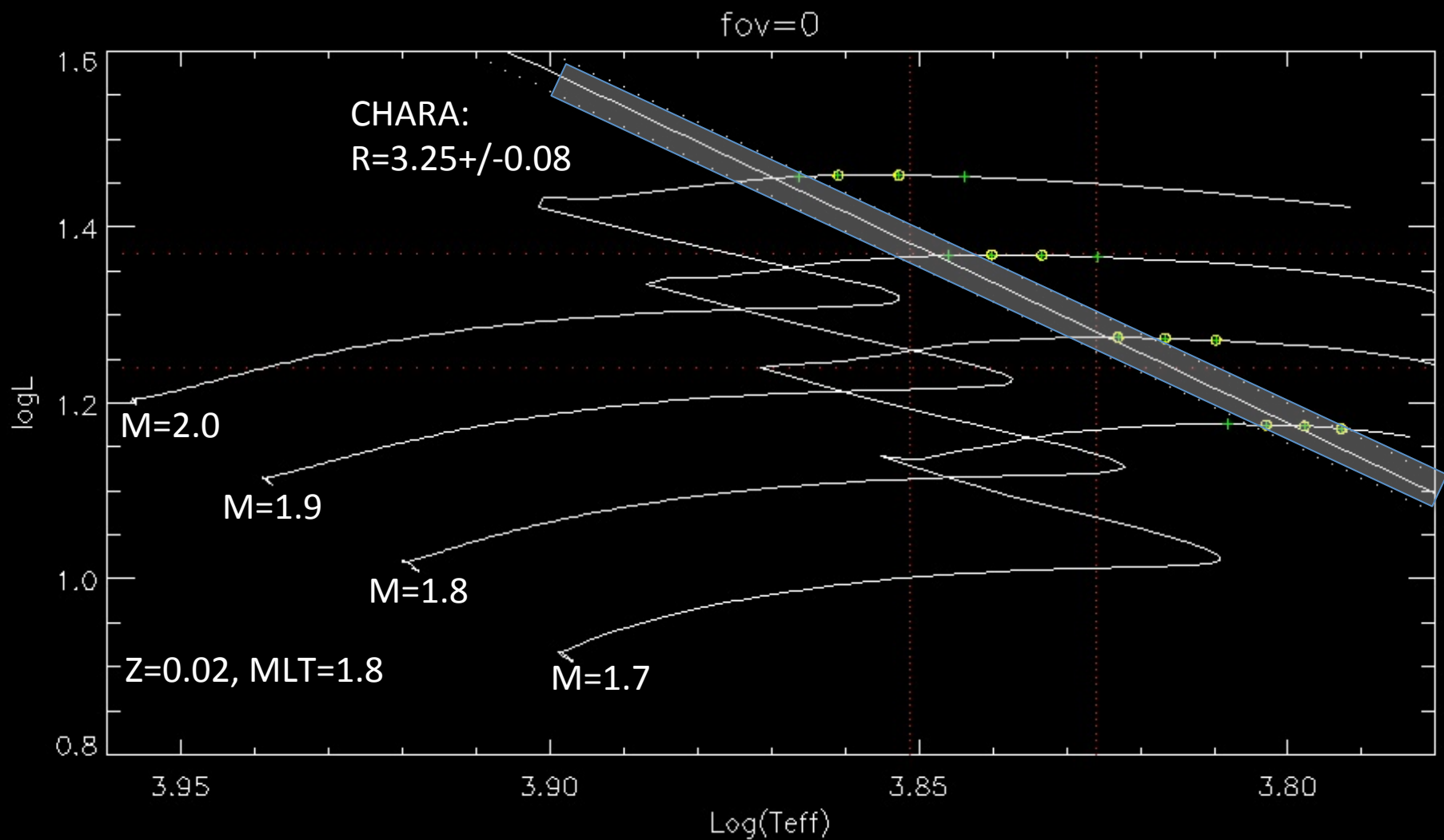
PAVO/CHARA K-band

Angular Diameter =  
 $0.480 \pm 0.011$  mas

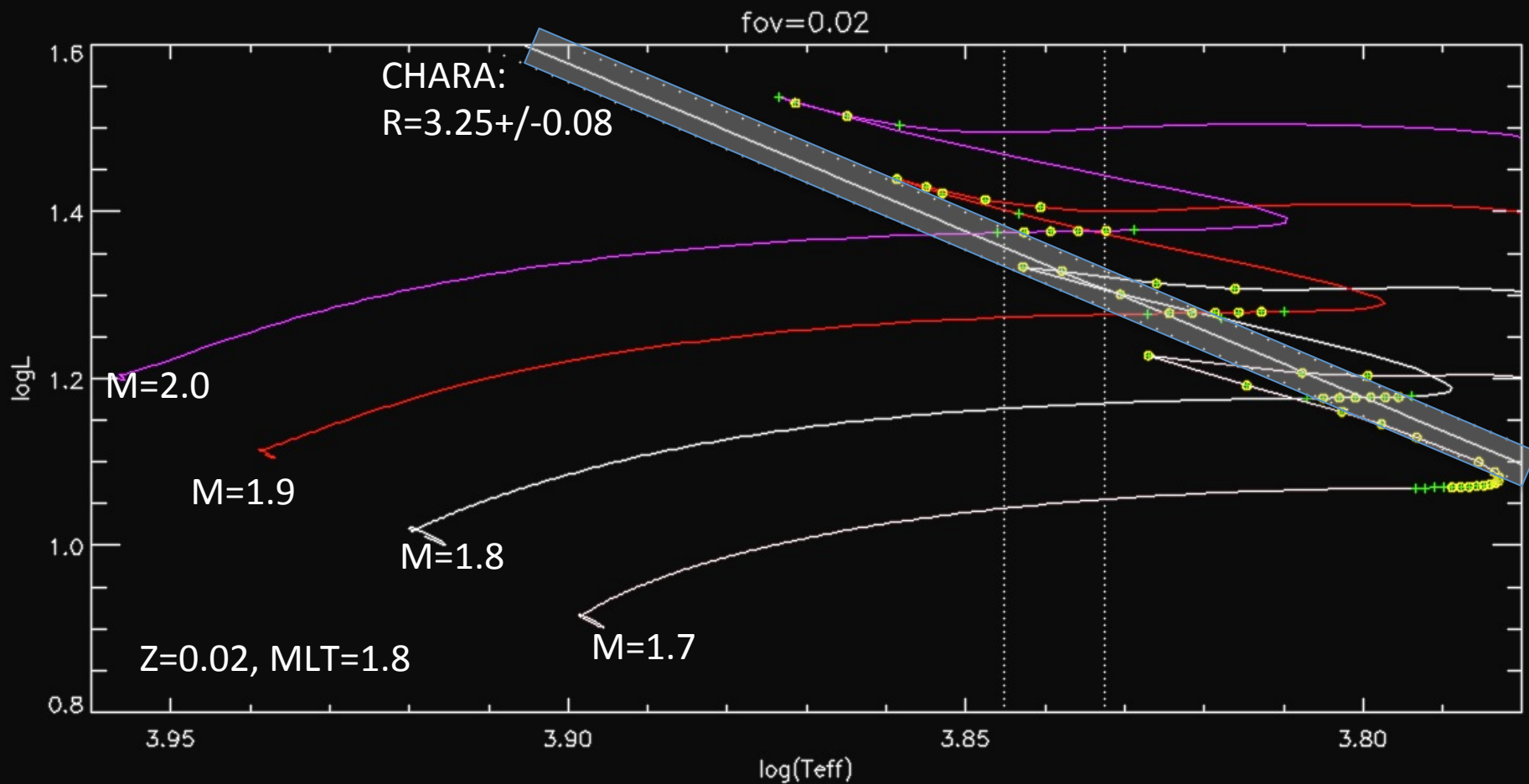
$R = 3.251 \pm 0.083$



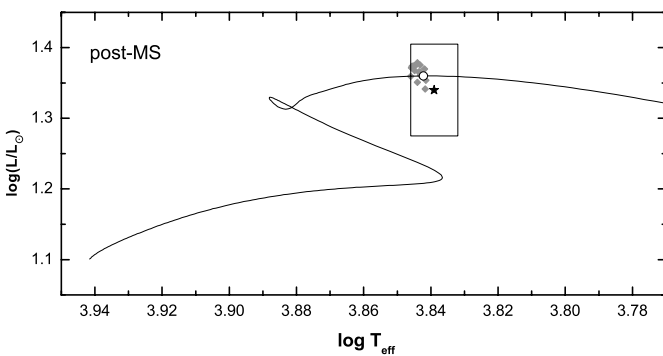
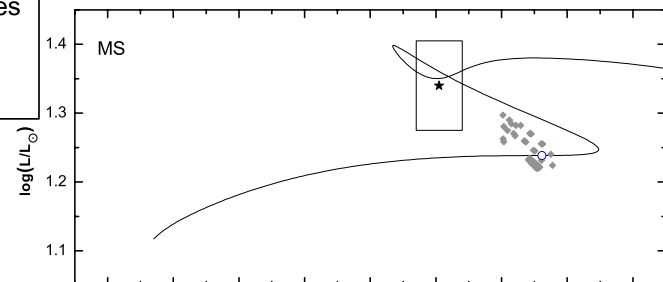
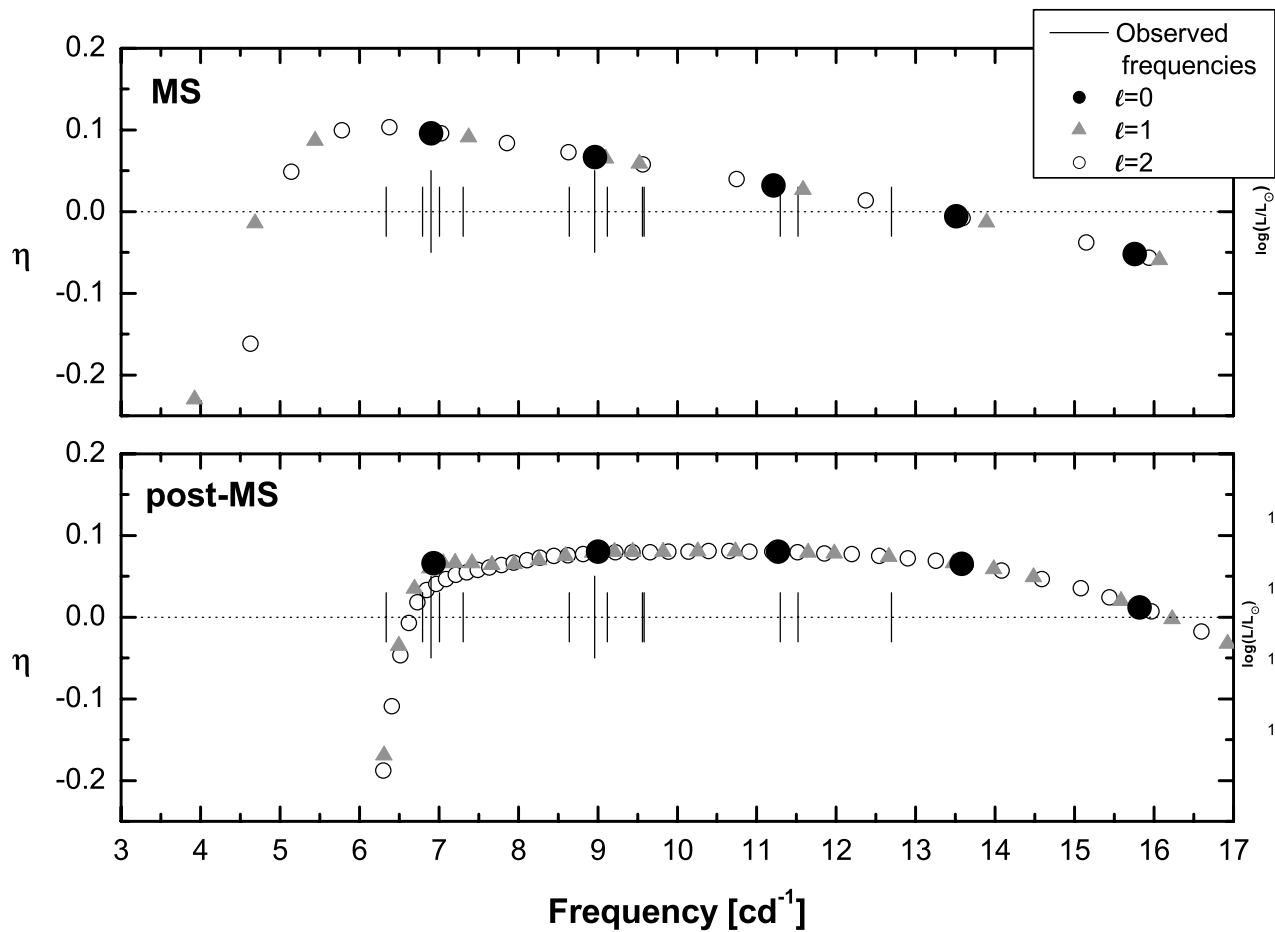
$T_{\text{eff}} = 6768 \pm 94$  K



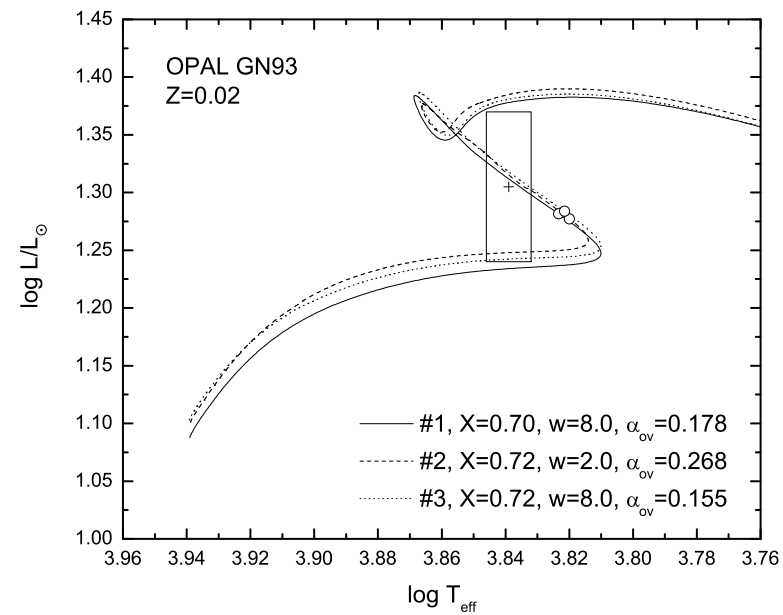
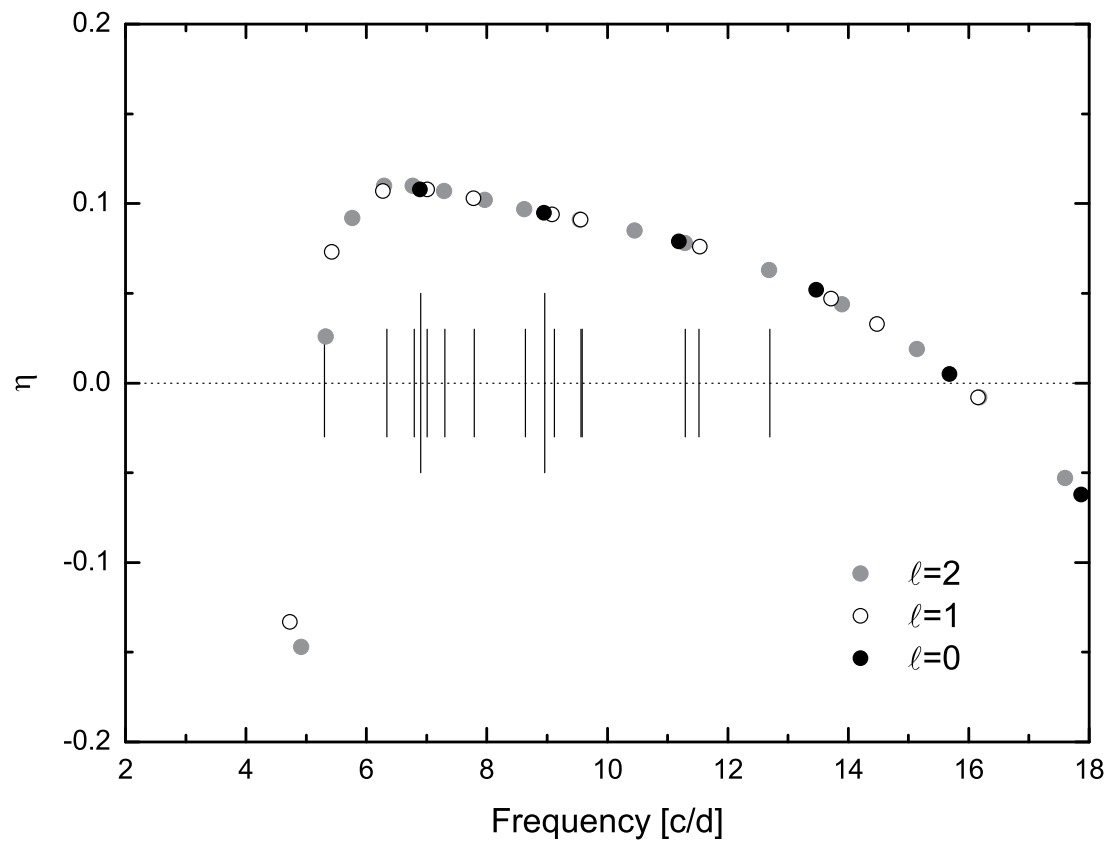
Fundamental radial mode= 6.90  $\pm$  0.10 (c/d)  
1st overtone radial = 8.96  $\pm$  0.10 (c/d)



Fundamental radial mode= 6.90 +/- 0.10 (c/d)  
1st overtone radial = 8.96 +/- 0.10 (c/d)



Lenz, Pamyatnykh et al. 2008

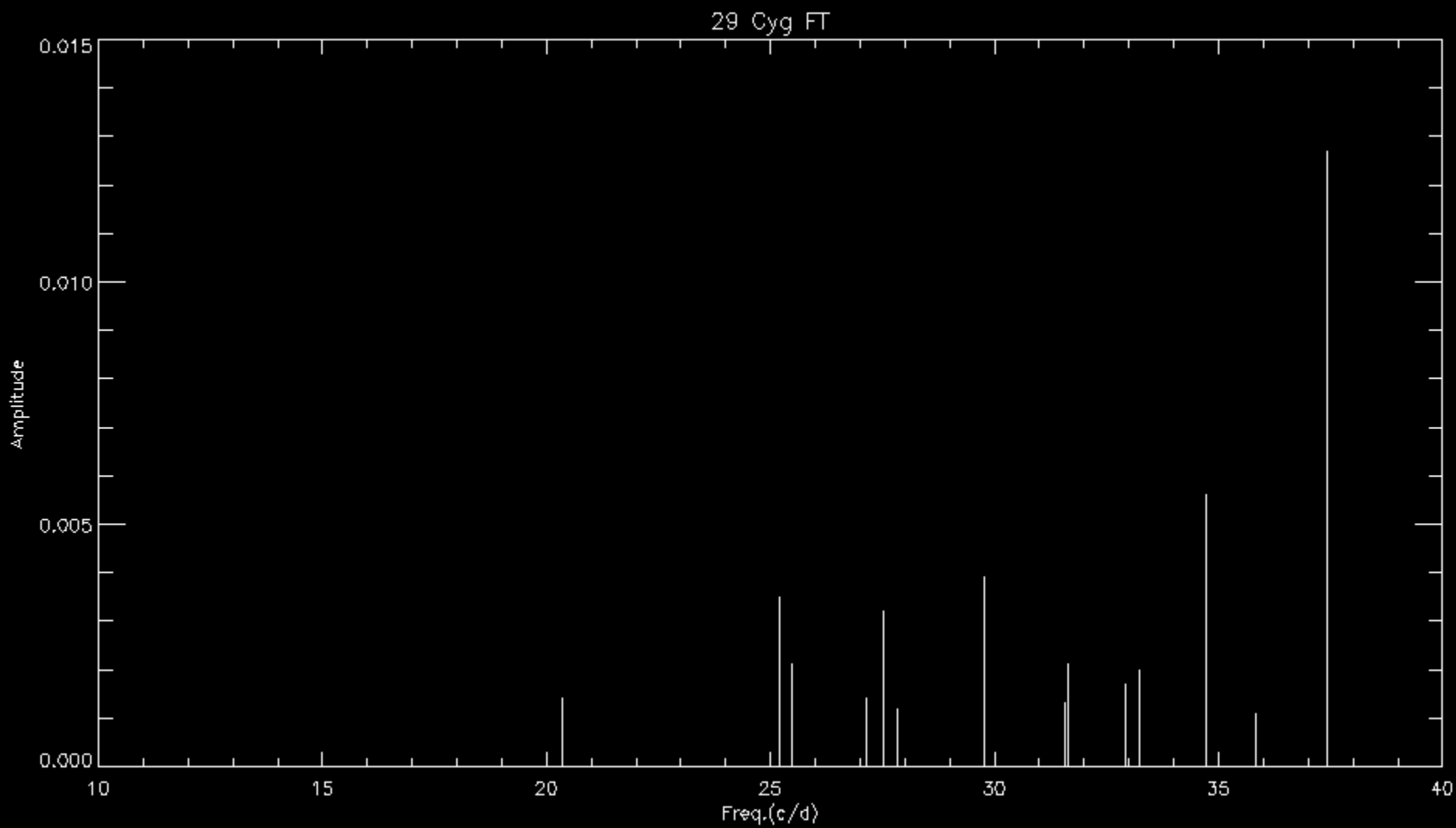


Lenz, Pamyatnykh et al. 2010

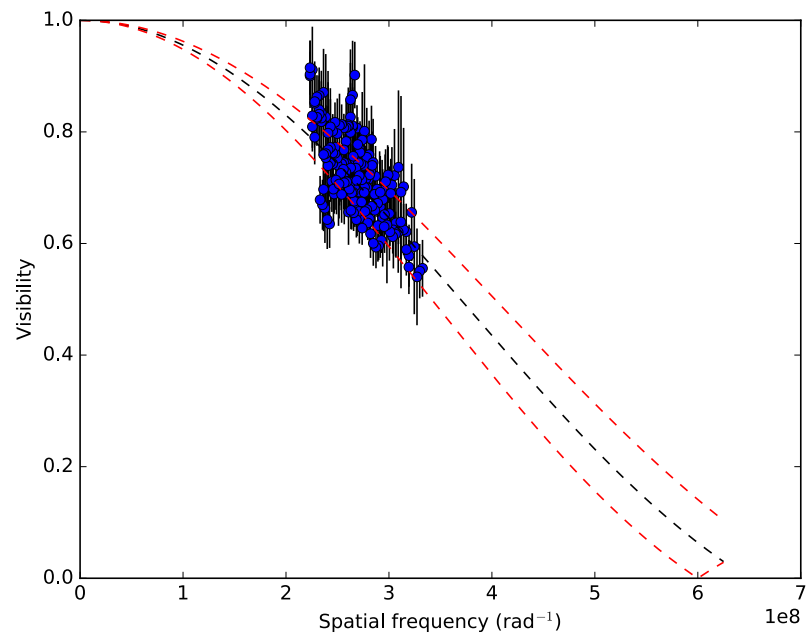
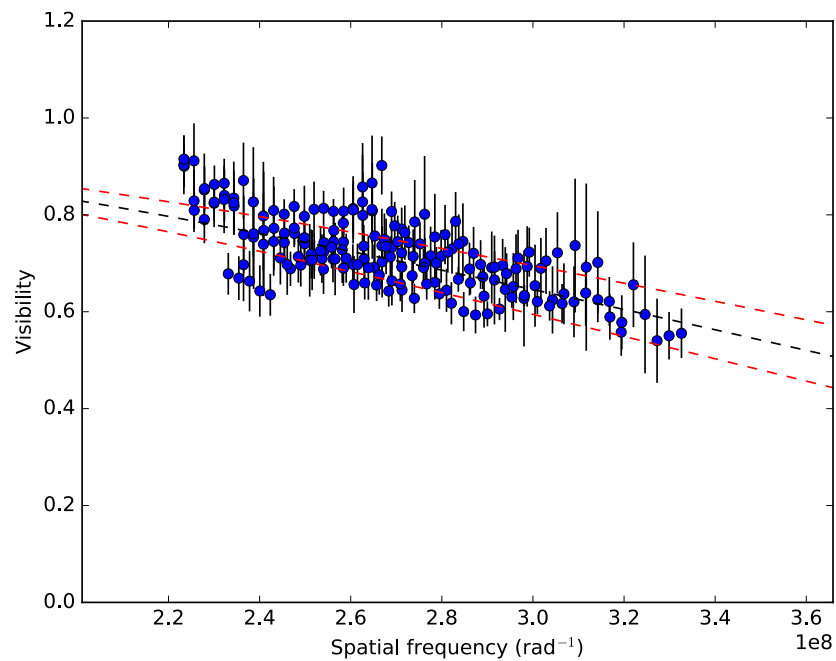
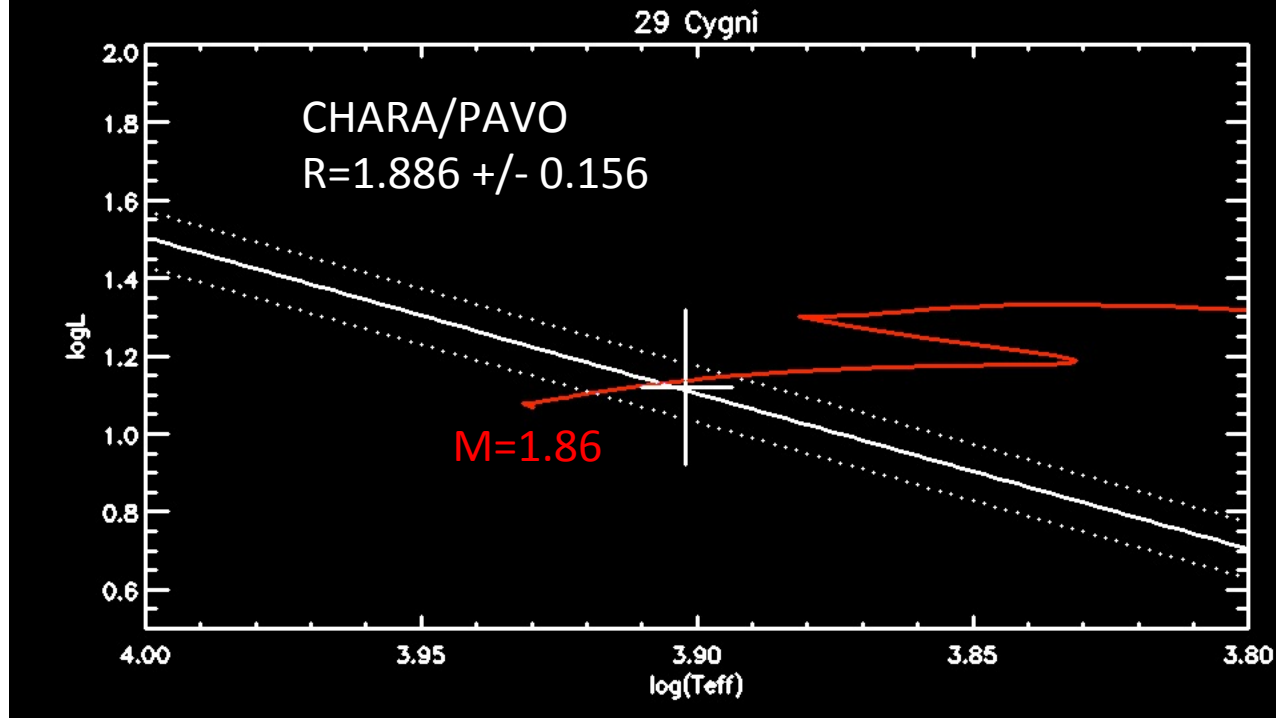
# 29 Cygni

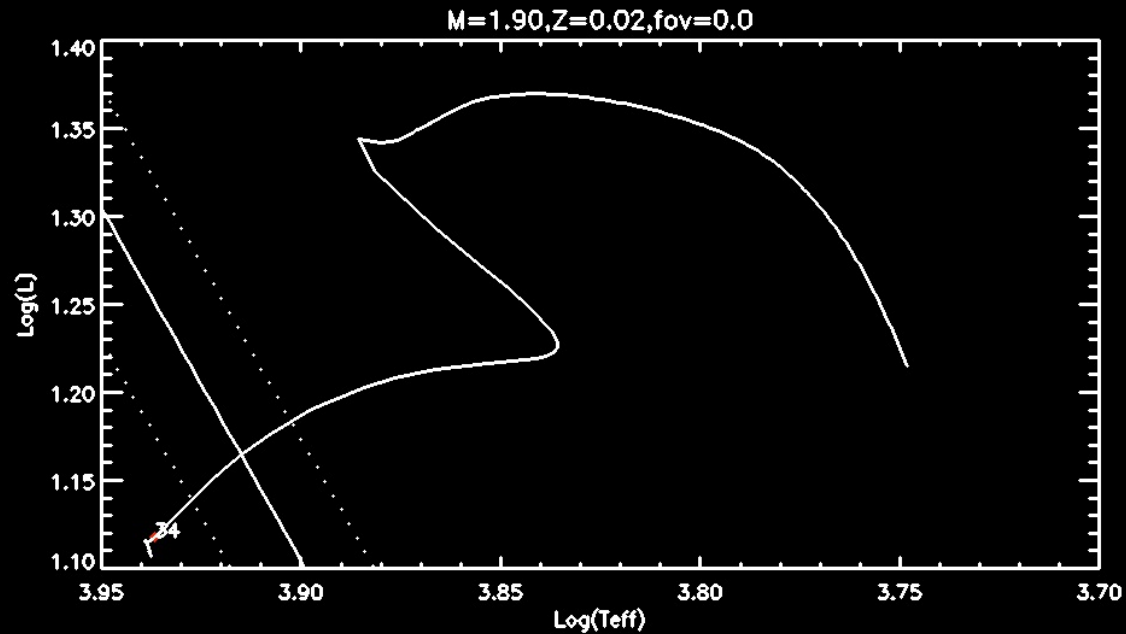
- $V_{\text{ini}} \leq 80 \text{ km/s}$
- Main sequence, slightly evolved
- $\log T_{\text{eff}} = 3.902 \pm 0.009$ ,  $\log g = 4.12 \pm 0.25$
- Lambda Boo star  
(unusually weak lines of iron-peak elements, whereas C,N,O and S have solar abundance)
- 14 frequencies, multi-color photometry mode  
ID. & seismic modeling, Casas 09

# 29 Cygni



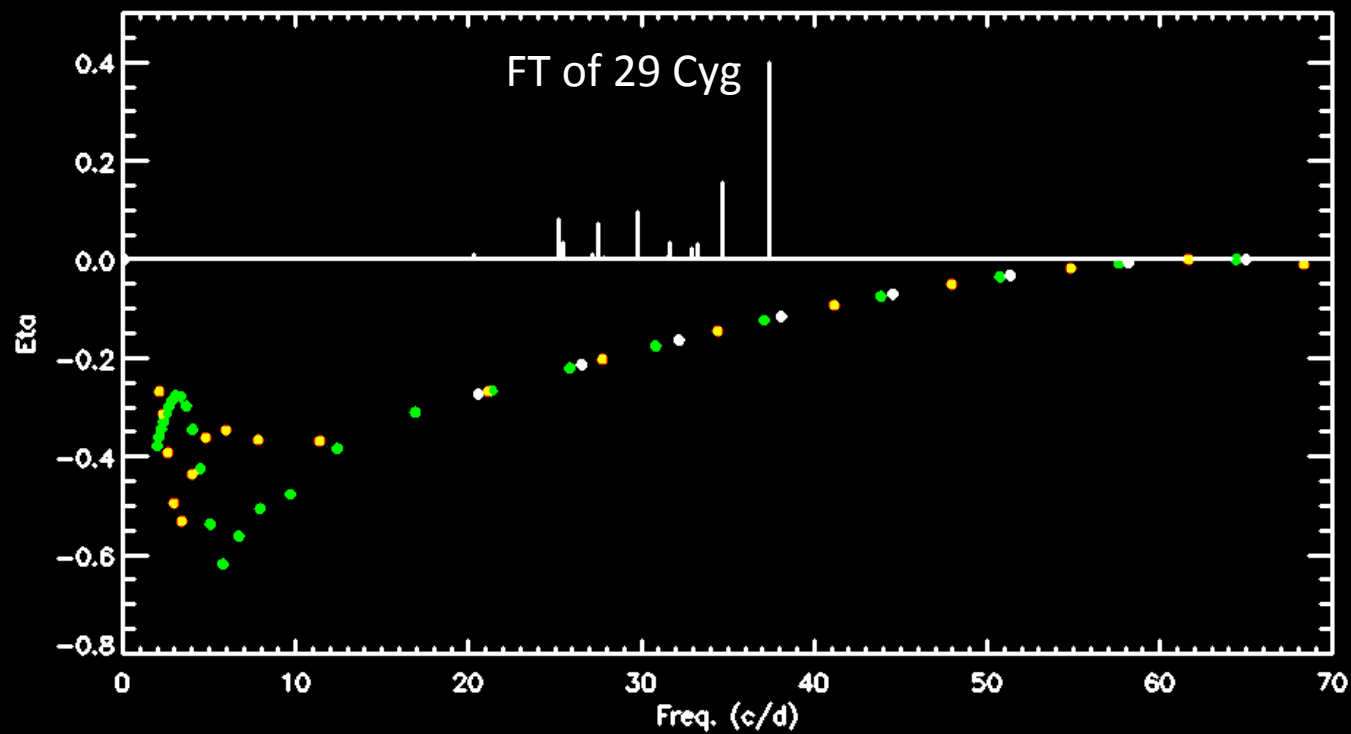


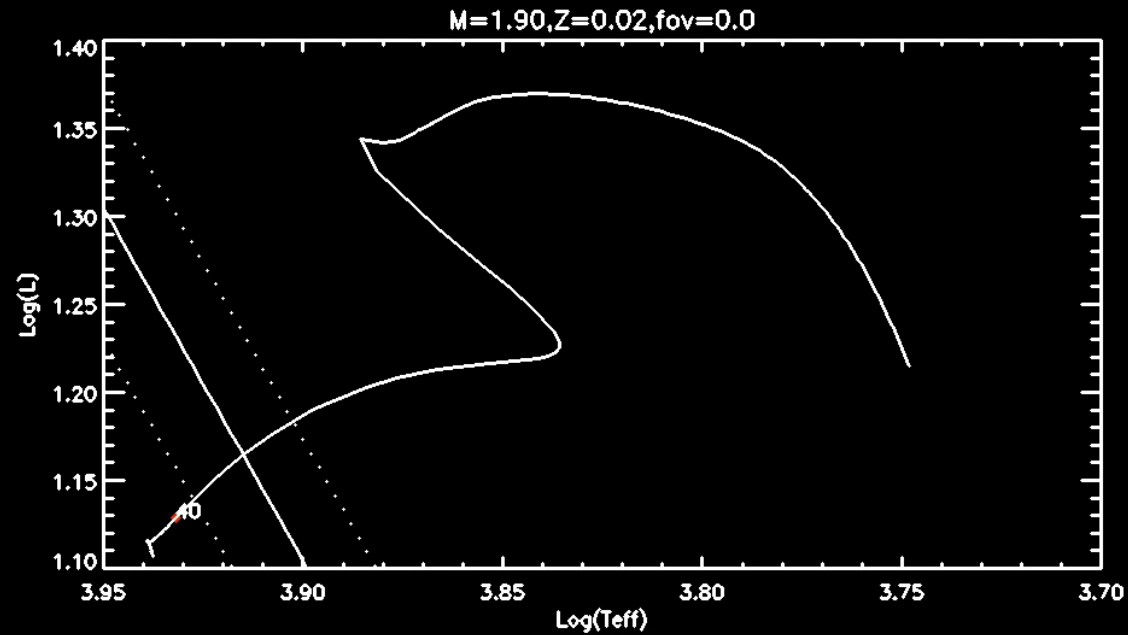




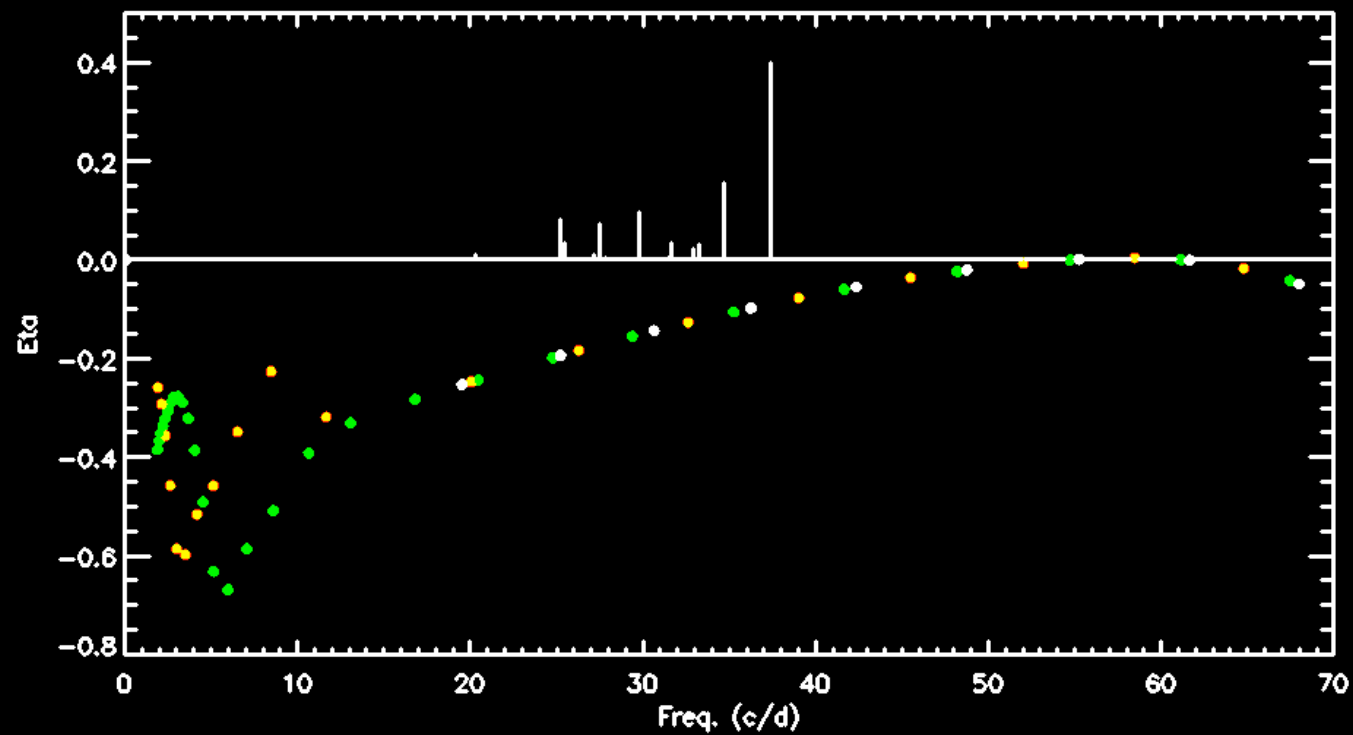
Evolution of  
frequencies and  
mode excitation

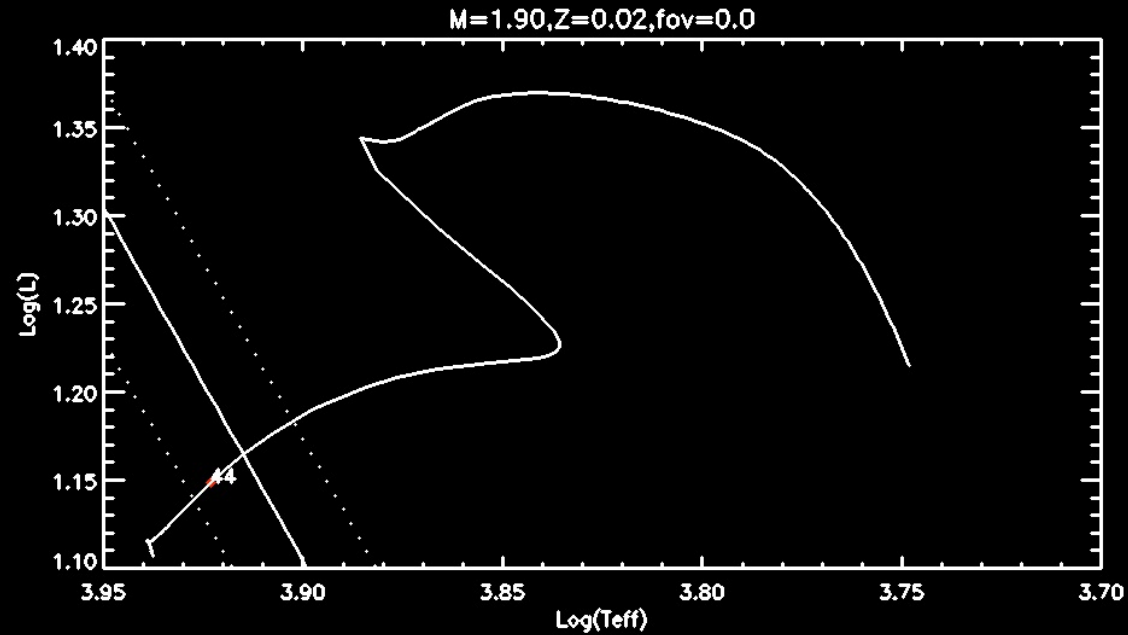
- L=0
- L=1
- L=2



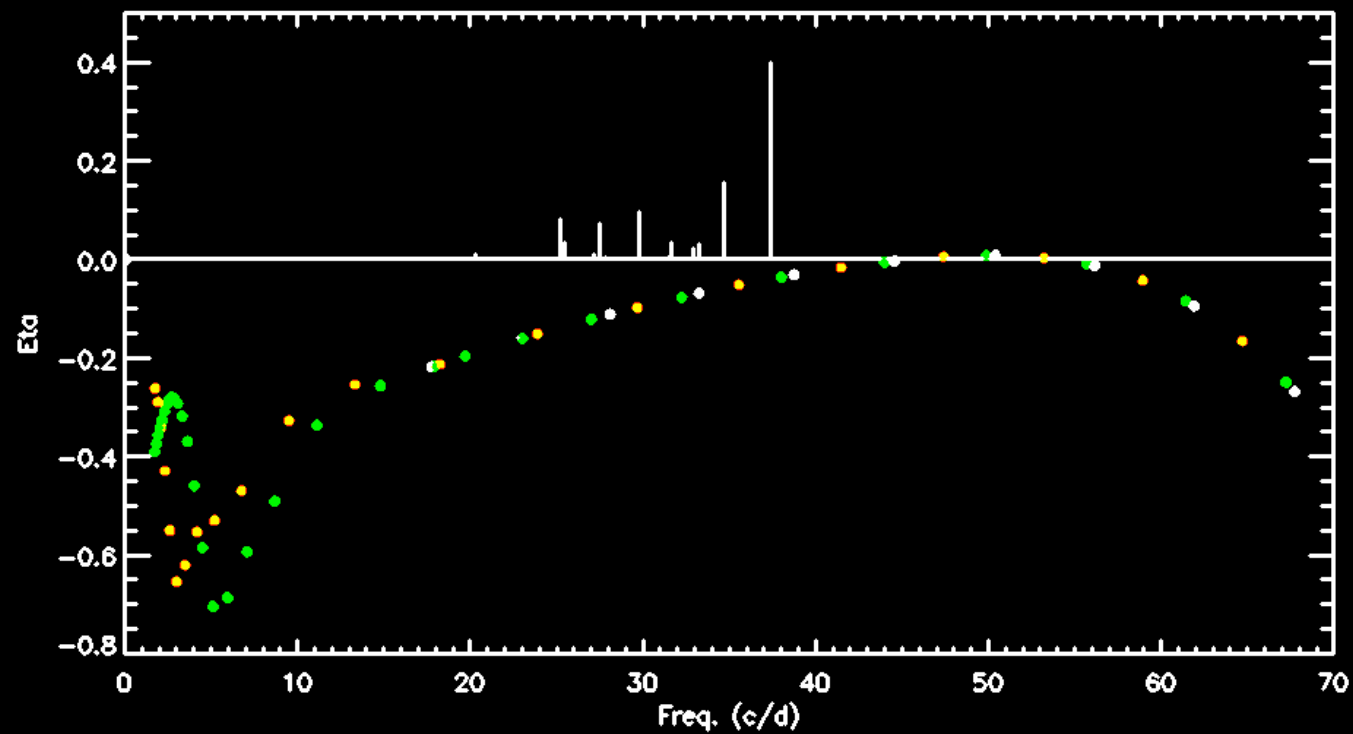


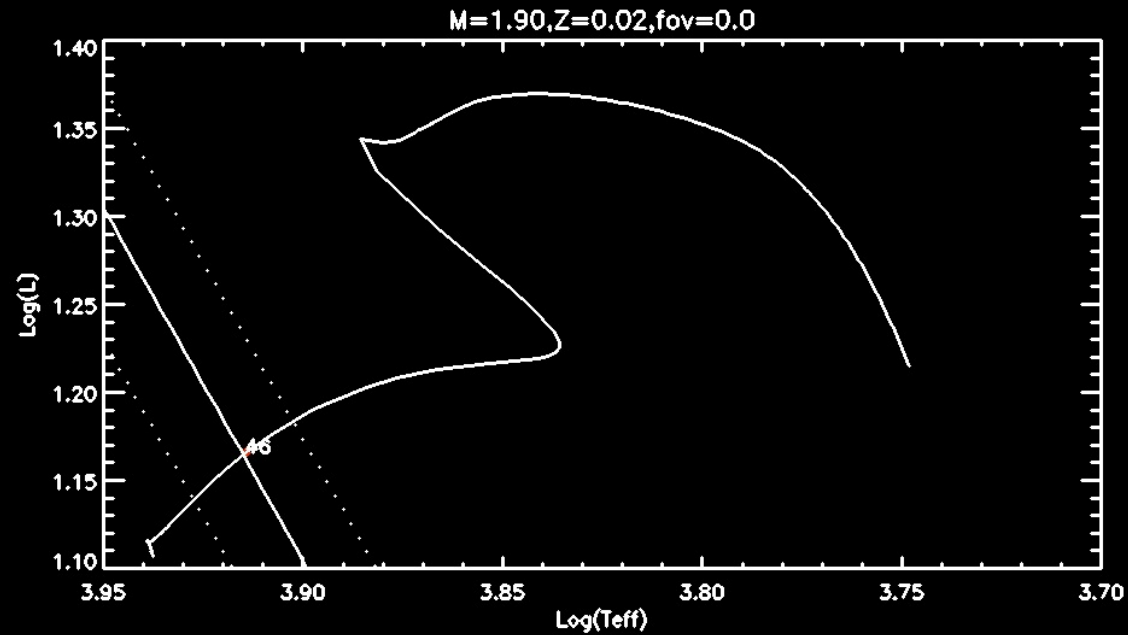
- $L=0$
- $L=1$
- $L=2$



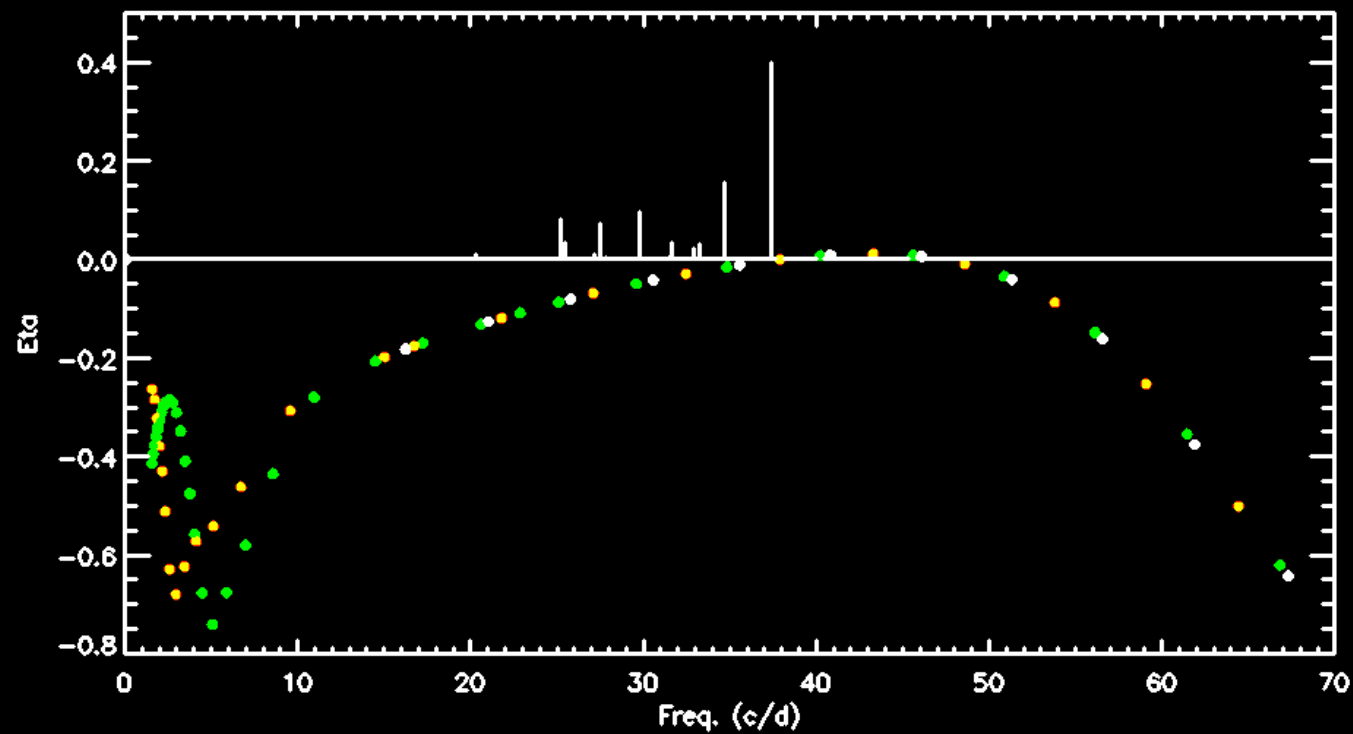


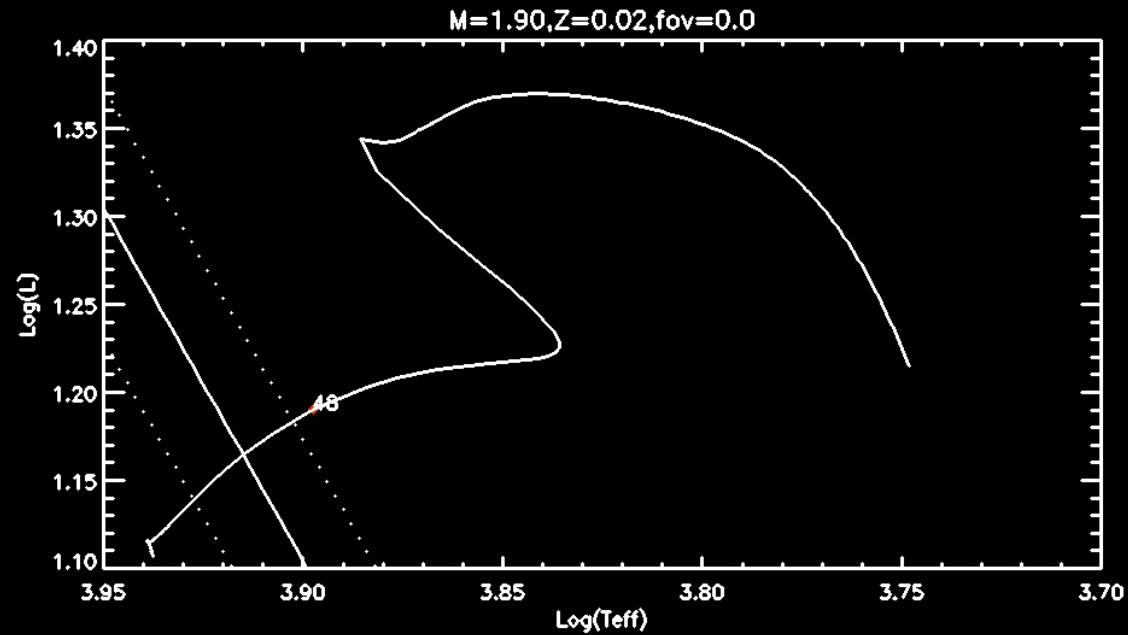
●  $L=0$   
●  $L=1$   
●  $L=2$



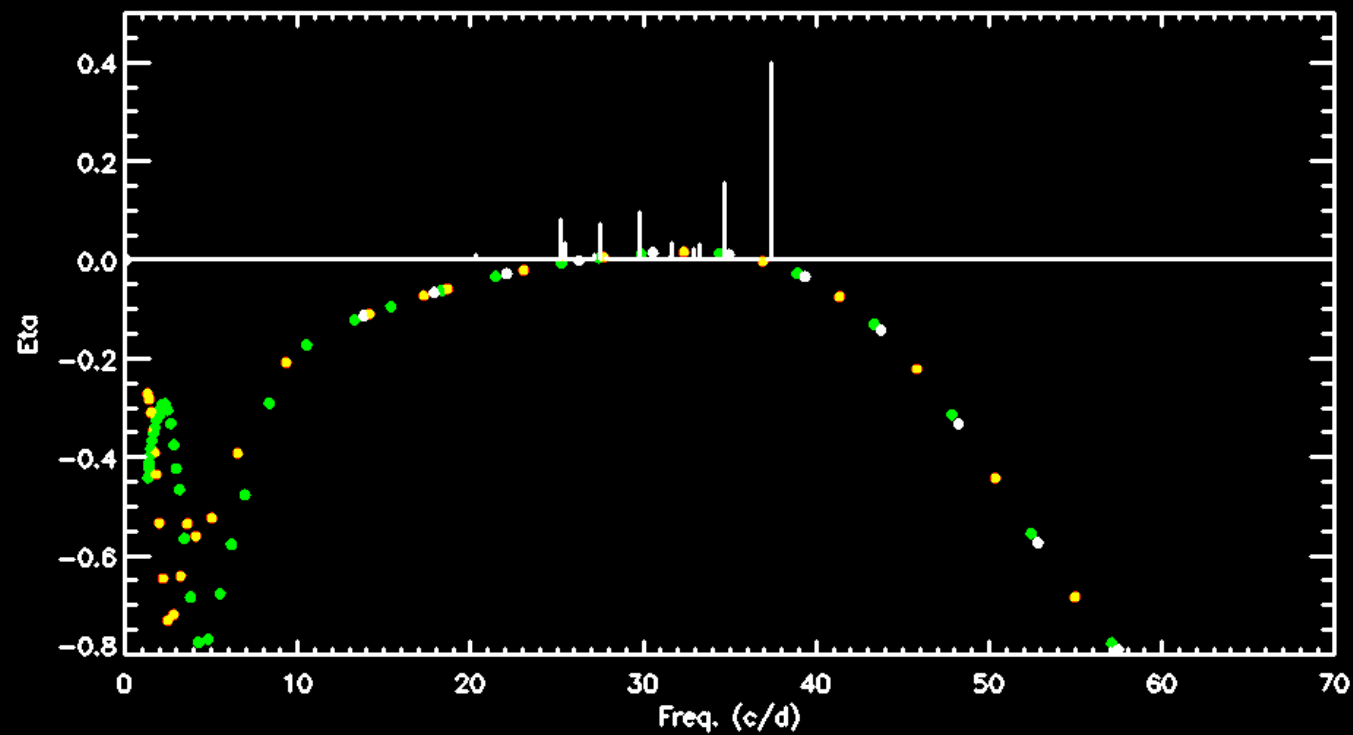


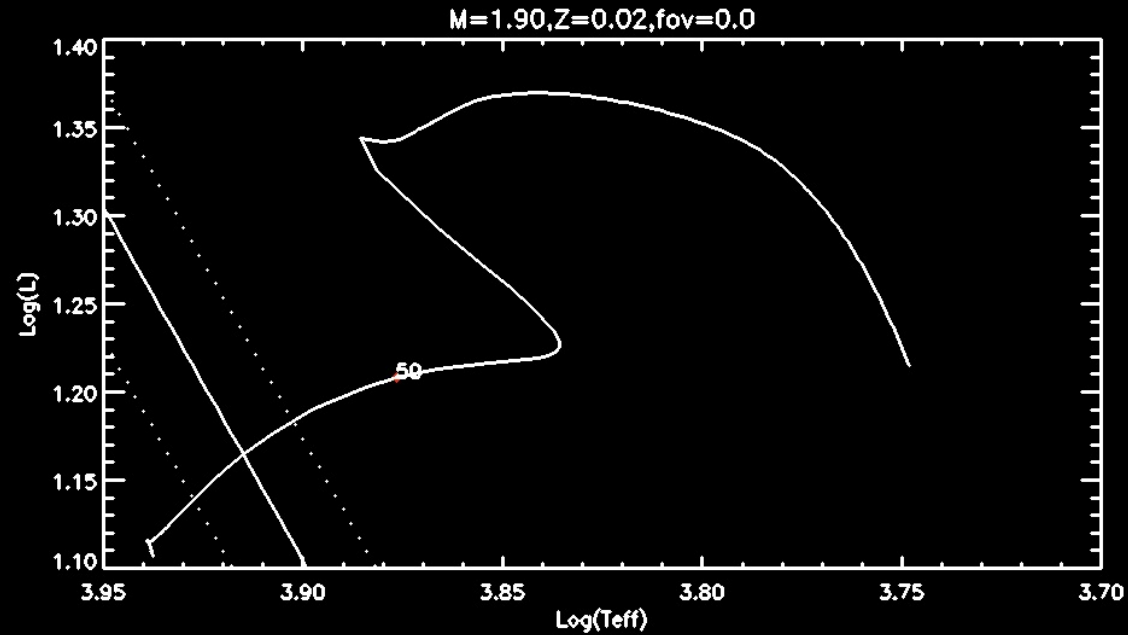
●  $L=0$   
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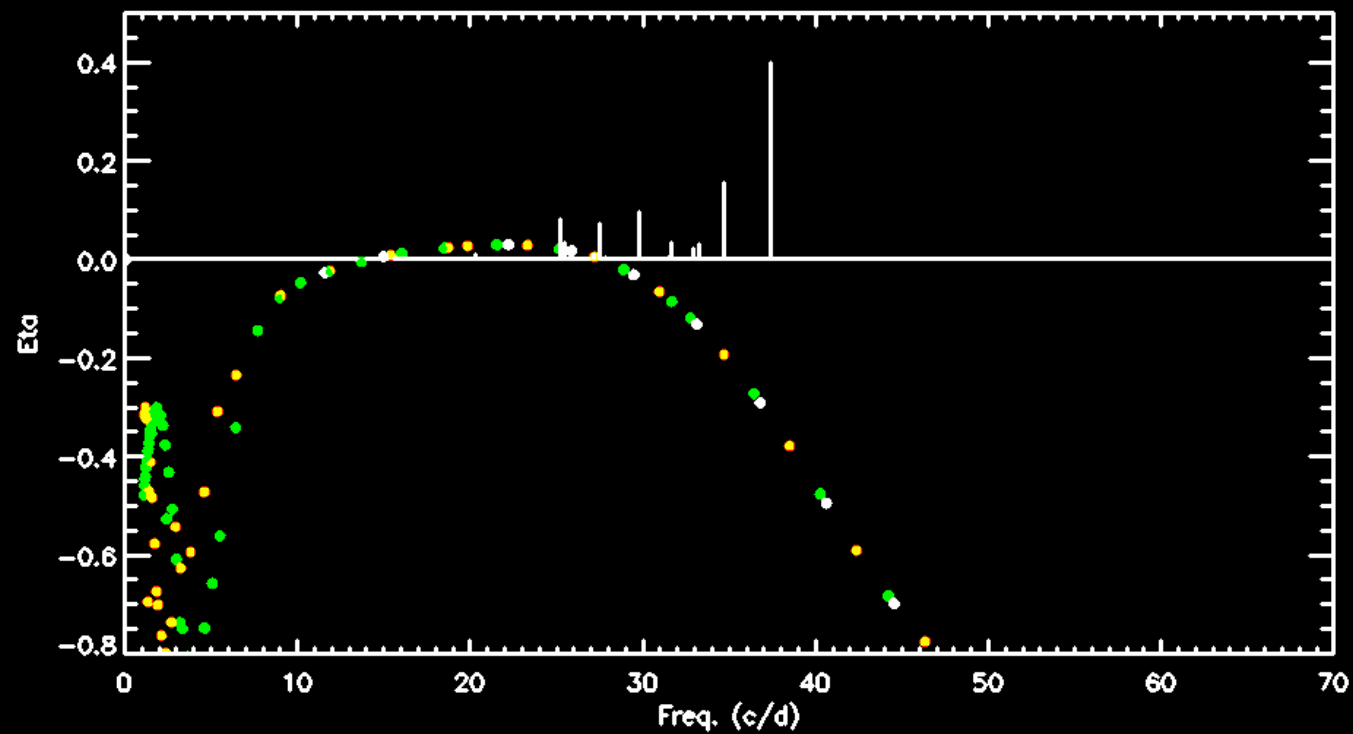


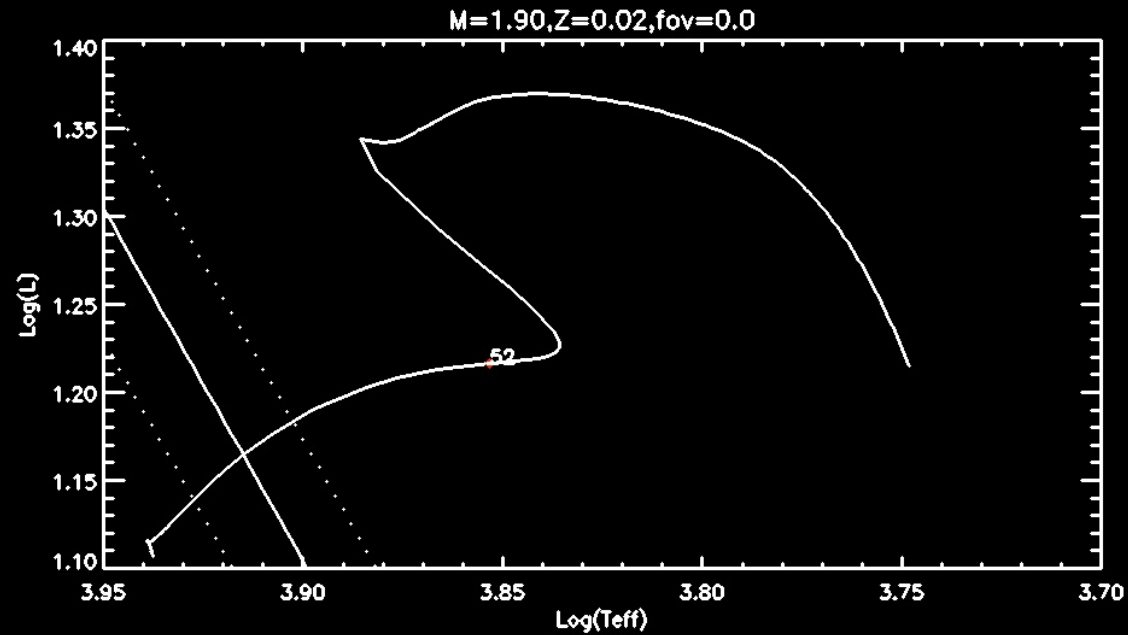
● L=0  
● L=1  
● L=2



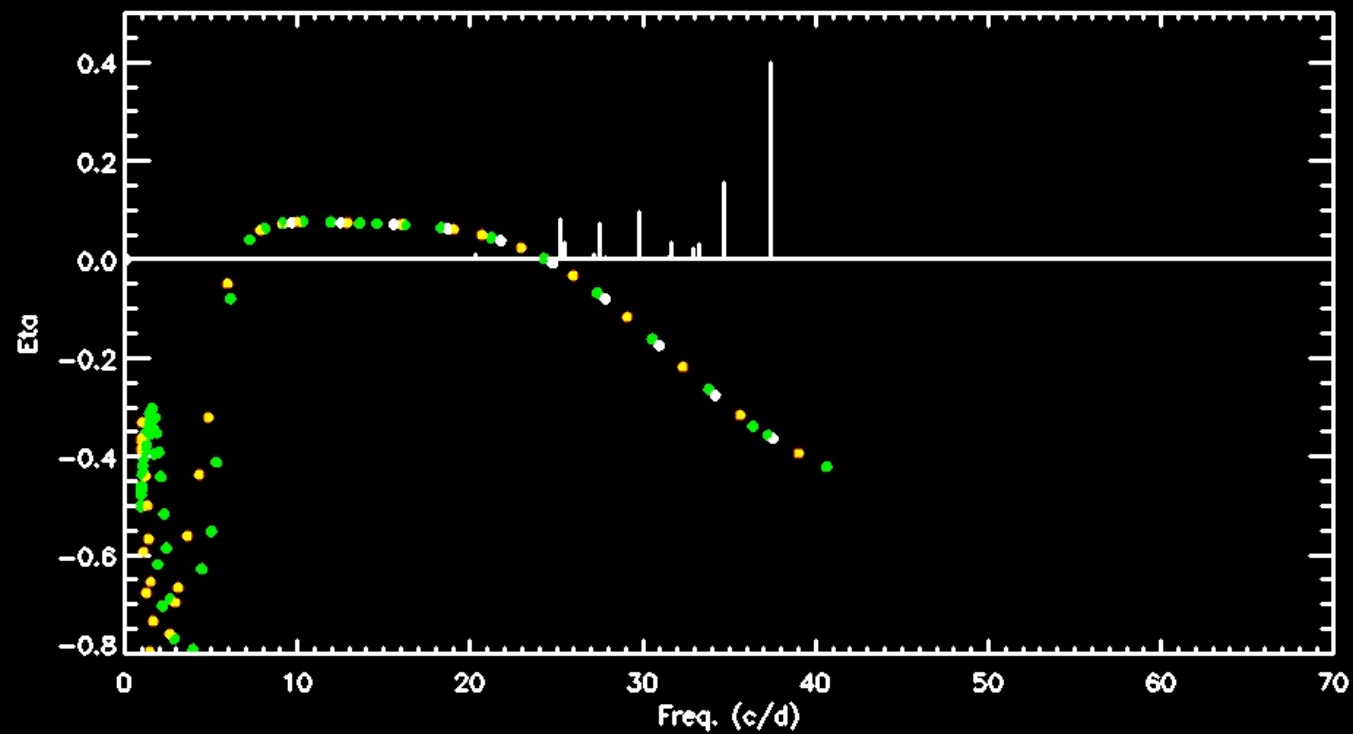


●  $L=0$   
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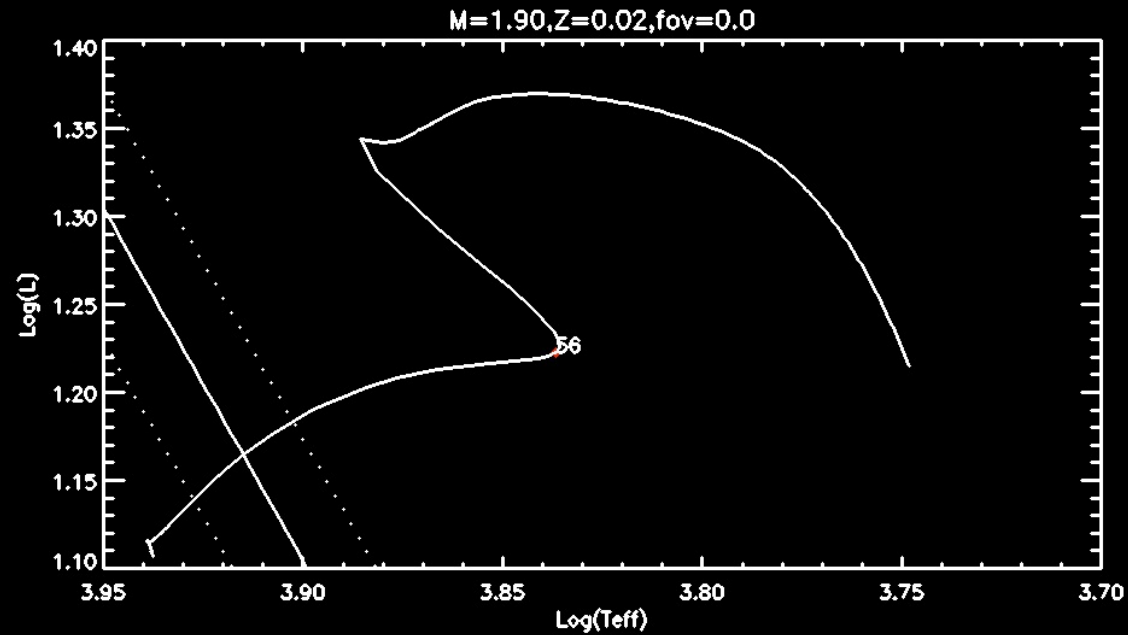




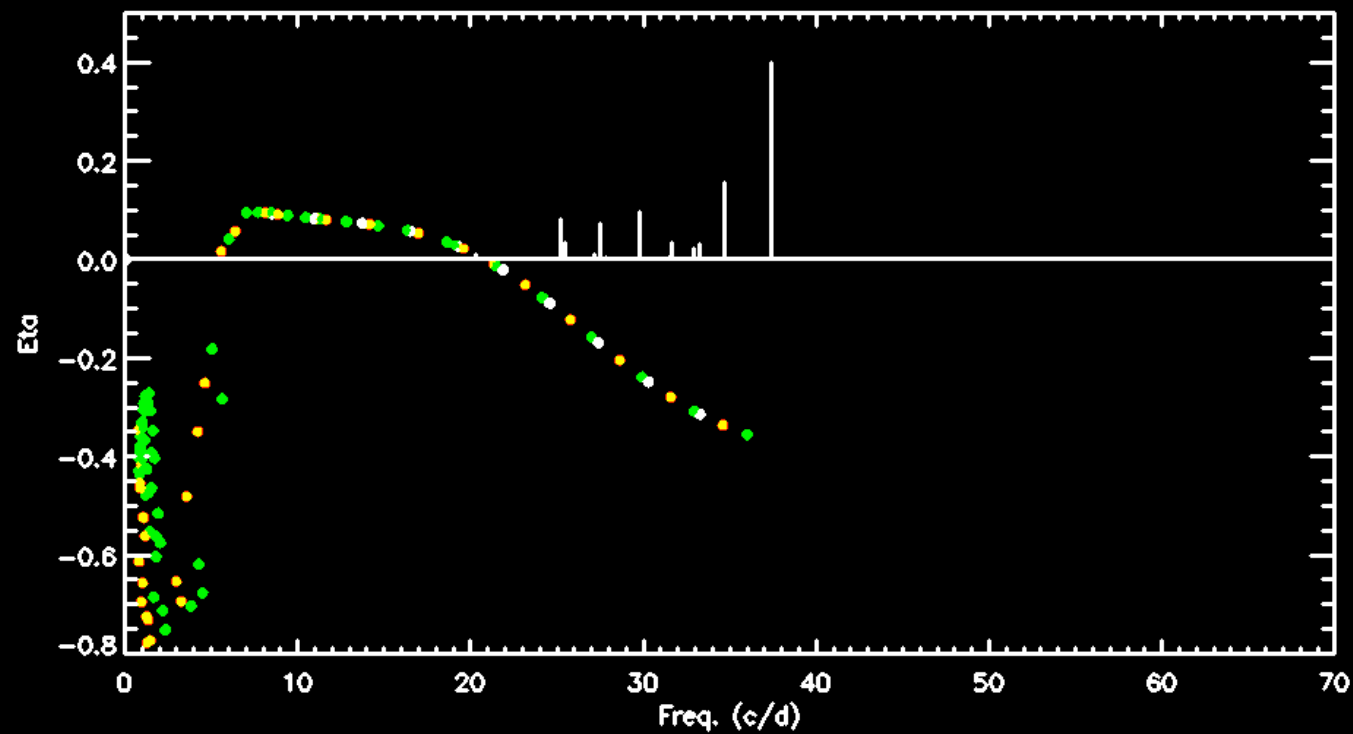
- $L=0$
- $L=1$
- $L=2$

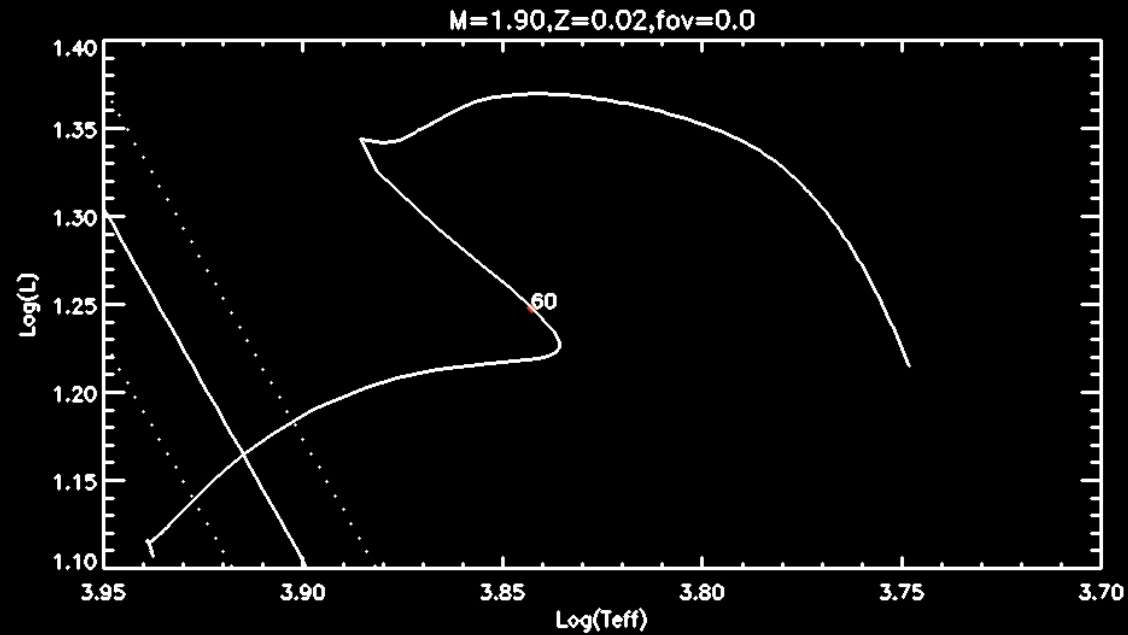




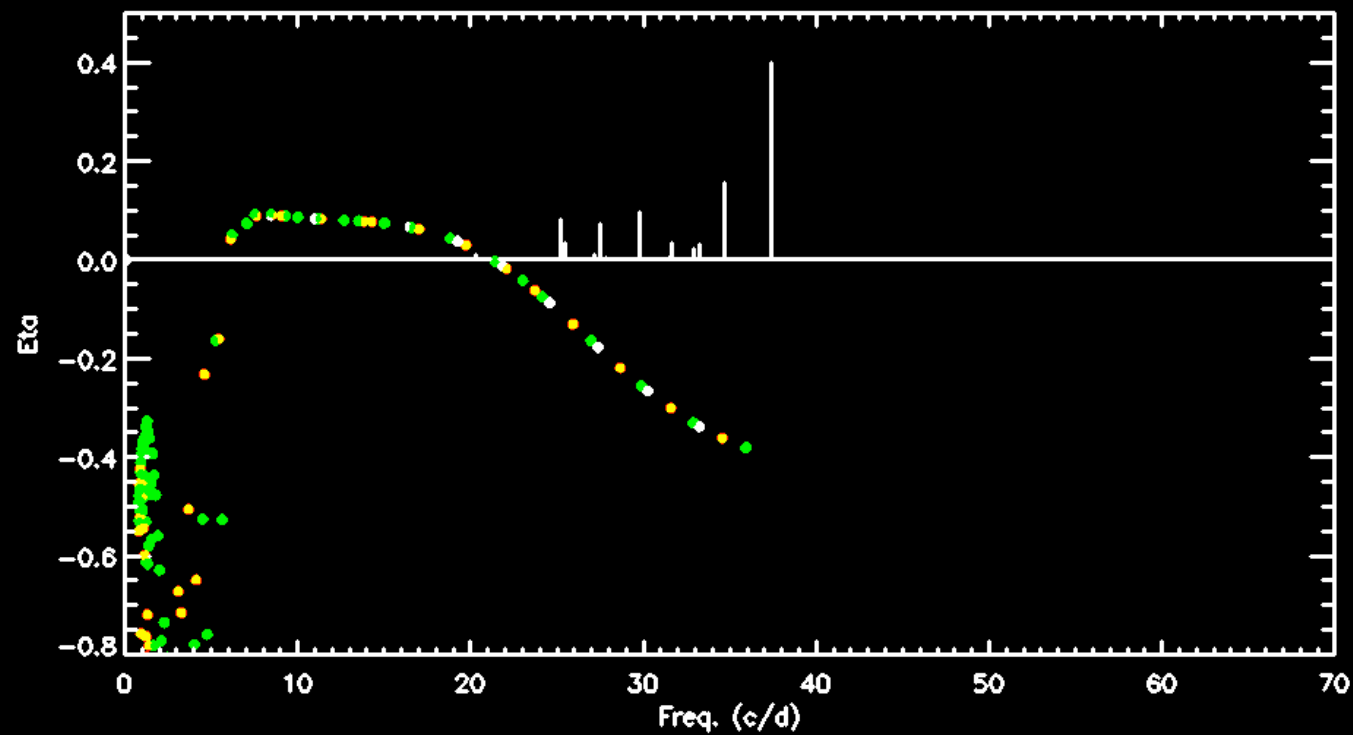


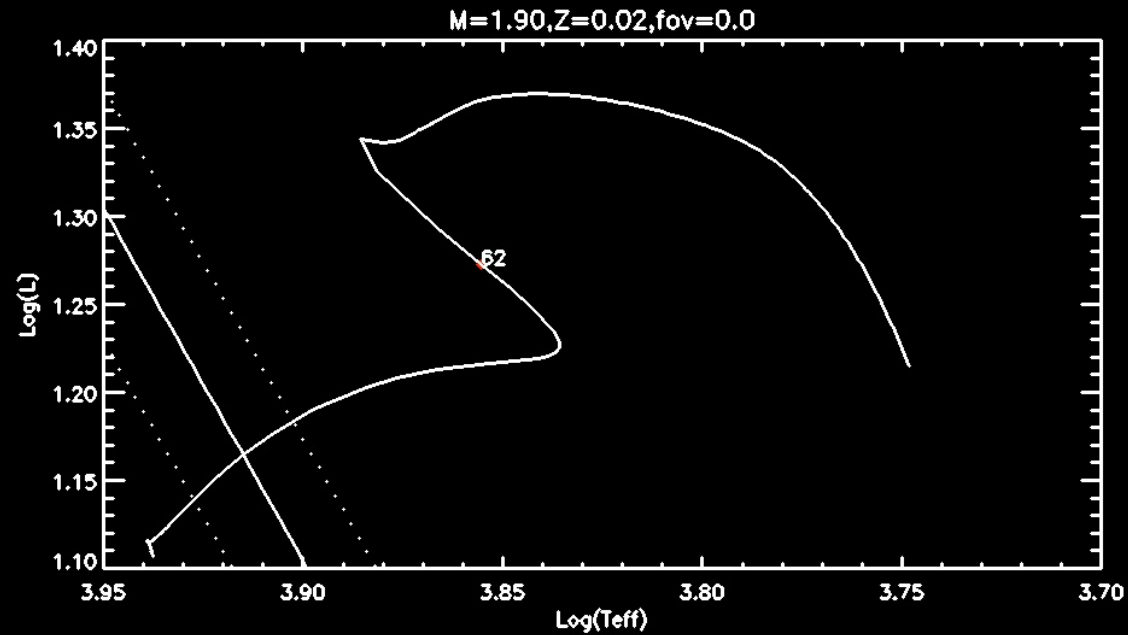
●  $L=0$   
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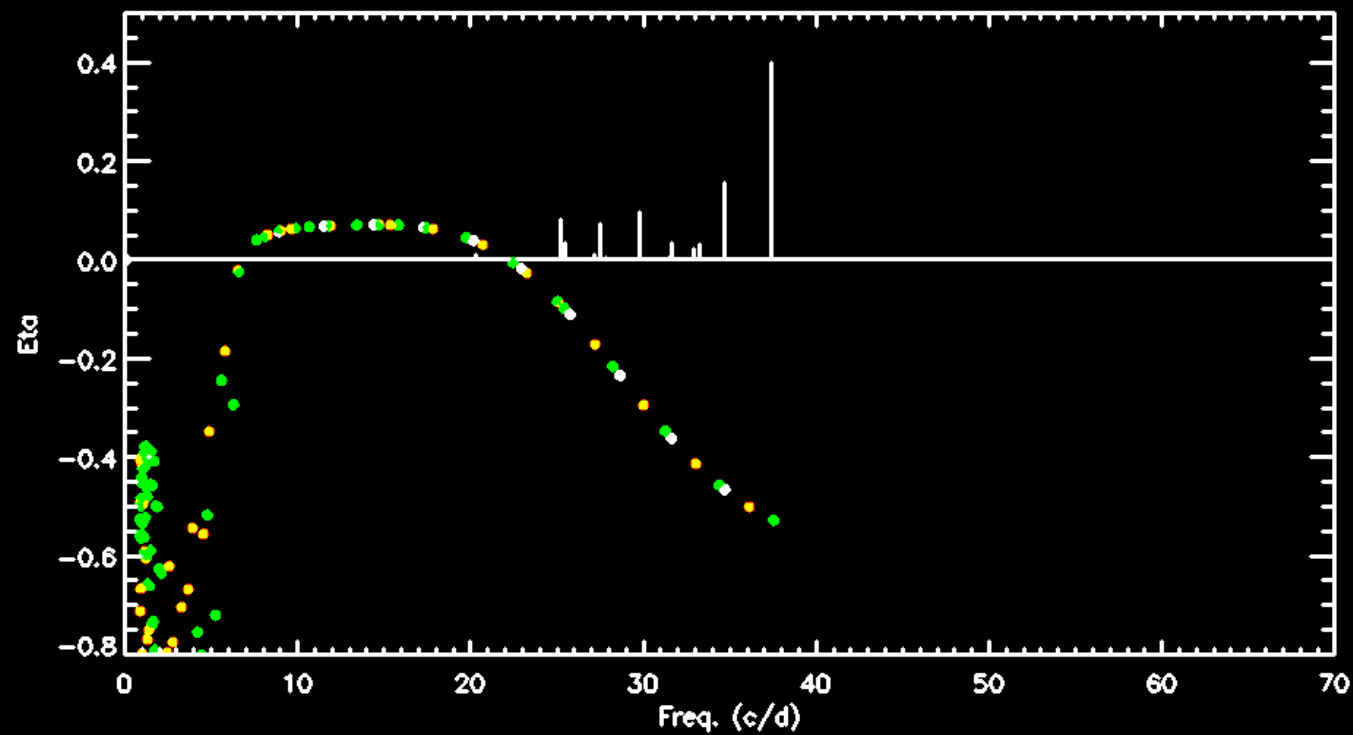


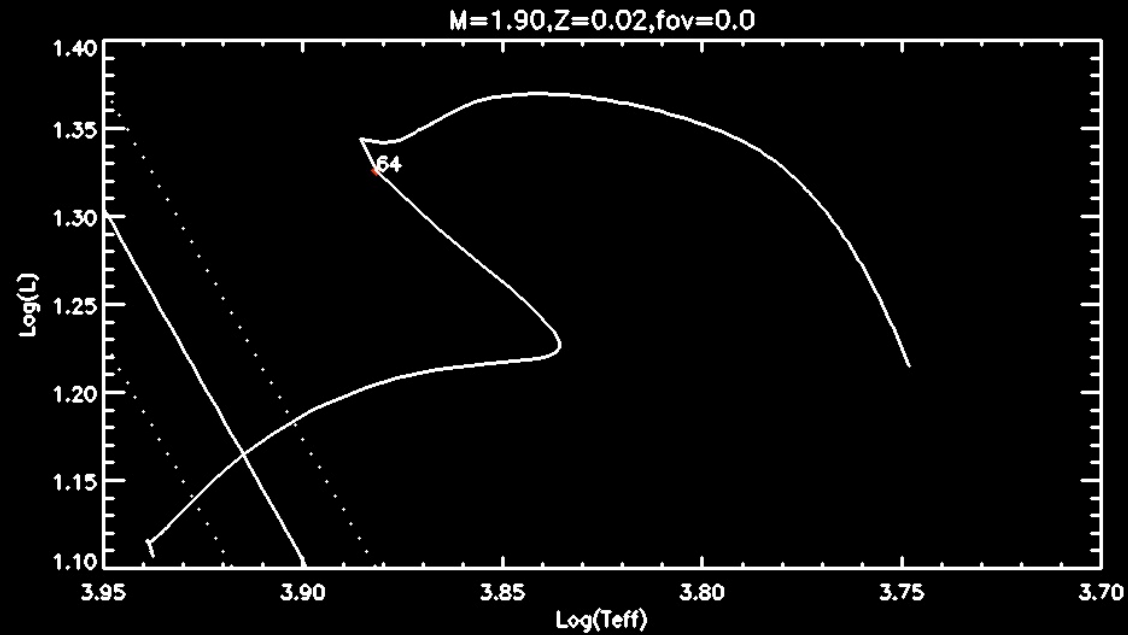
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●  $L=2$



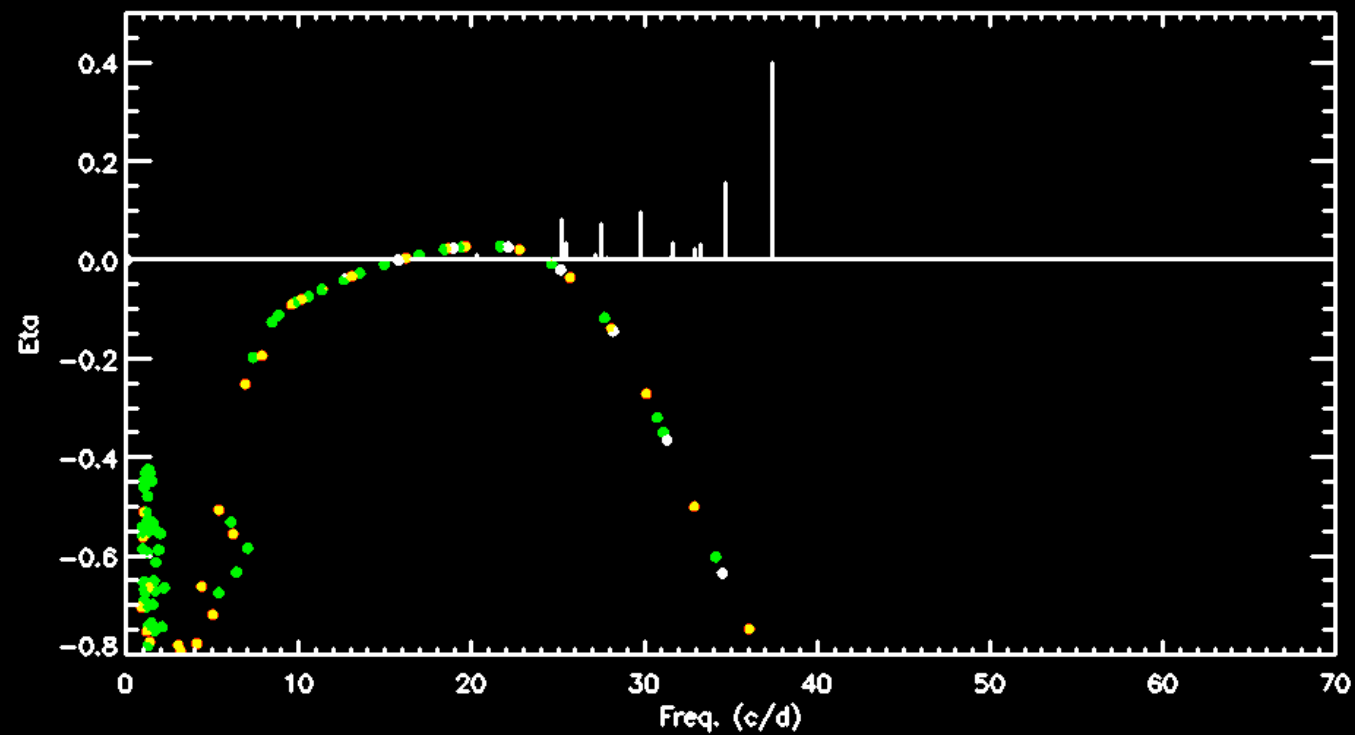


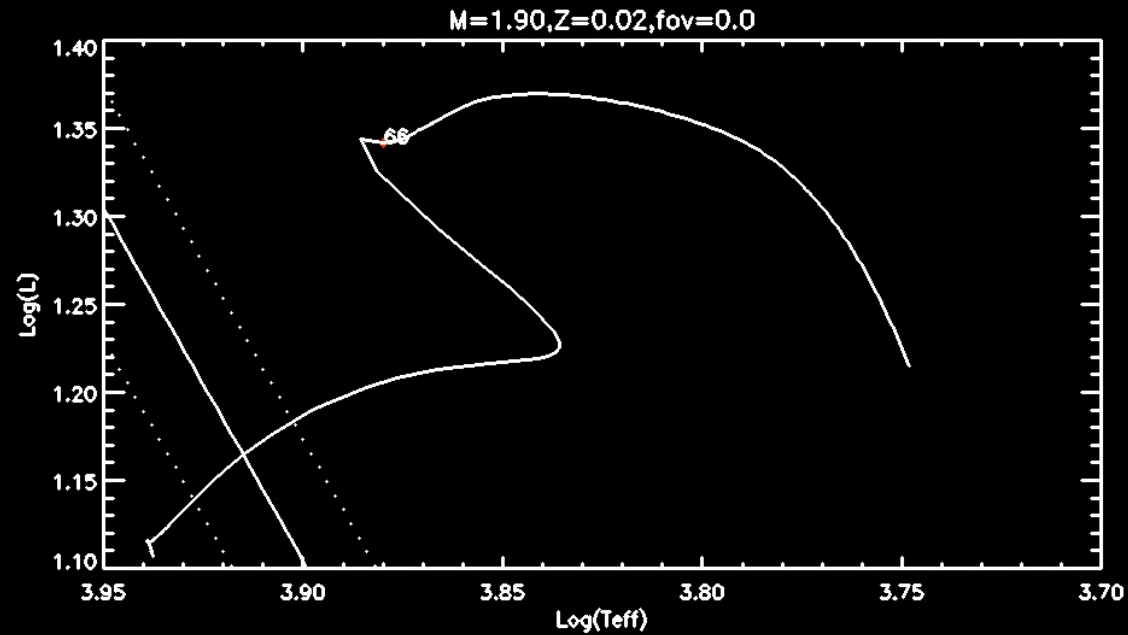
●  $L=0$   
●  $L=1$   
●  $L=2$



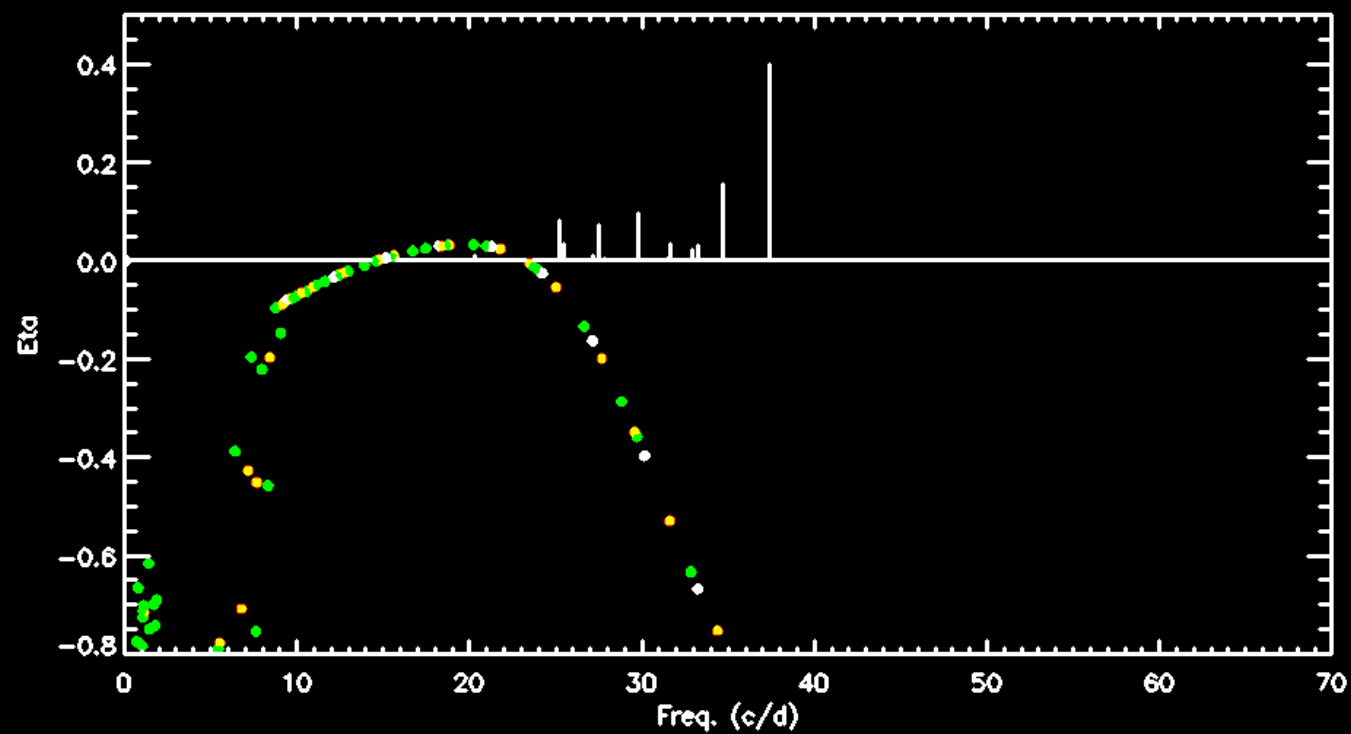


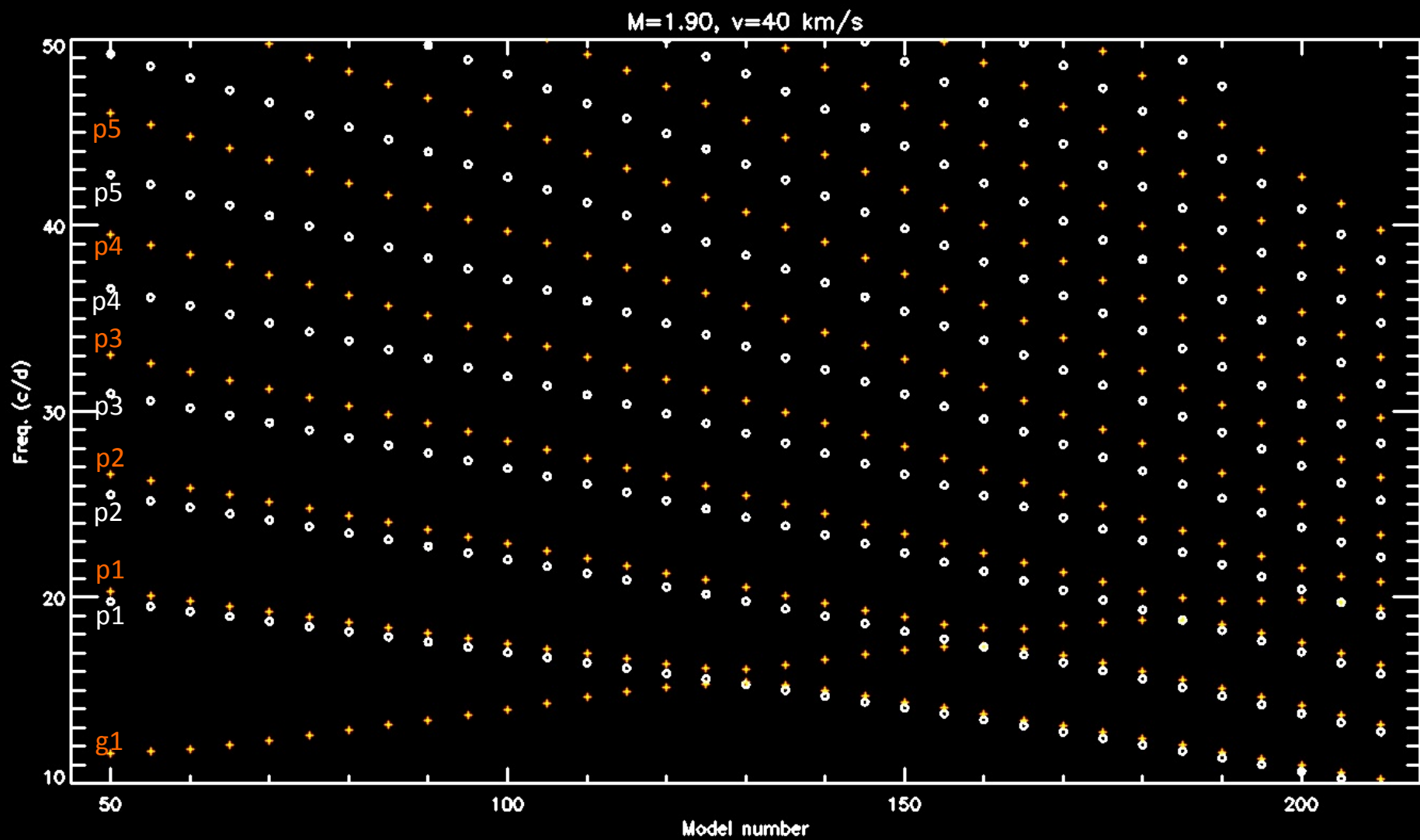
●  $L=0$   
●  $L=1$   
●  $L=2$





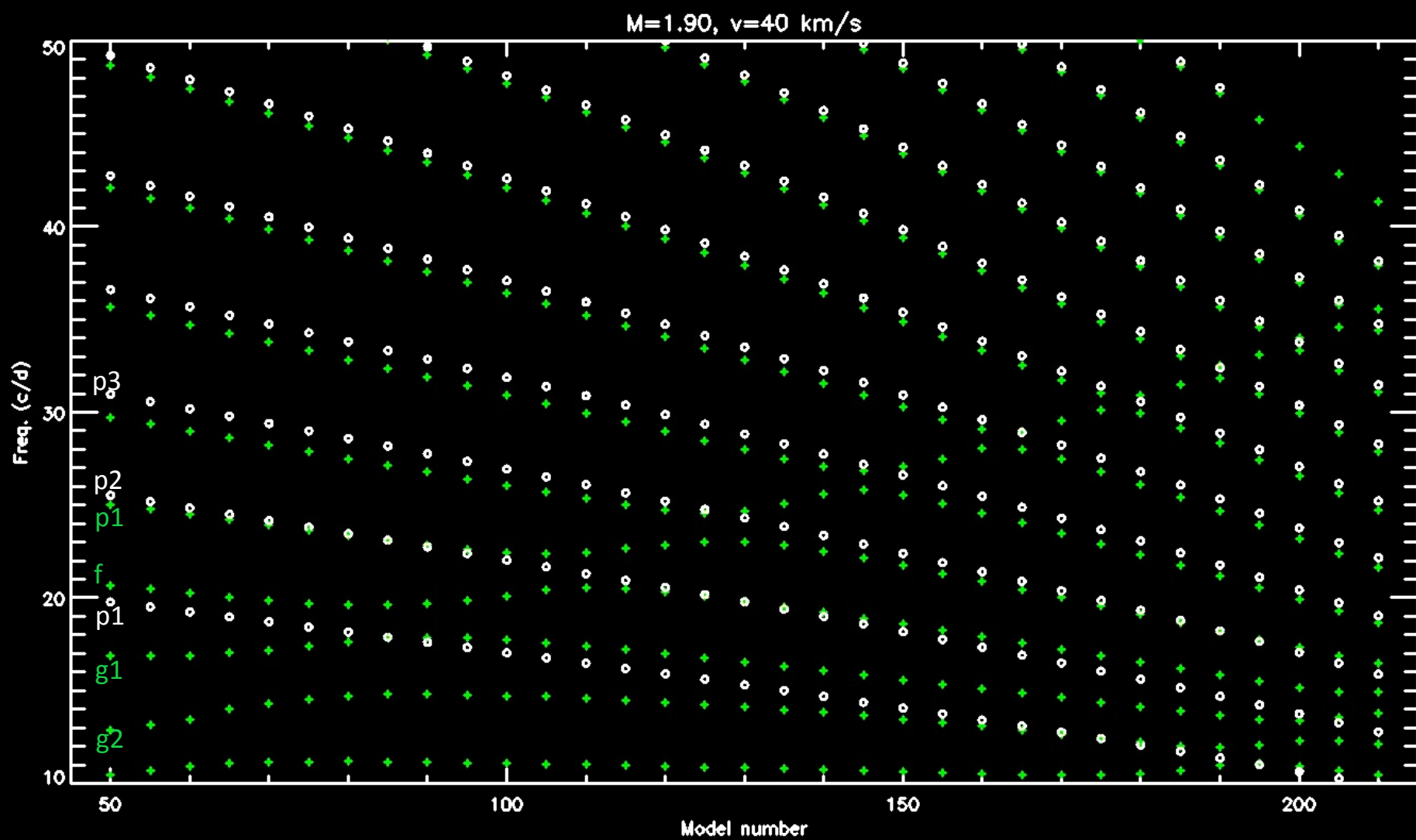
●  $L=0$   
●  $L=1$   
●  $L=2$





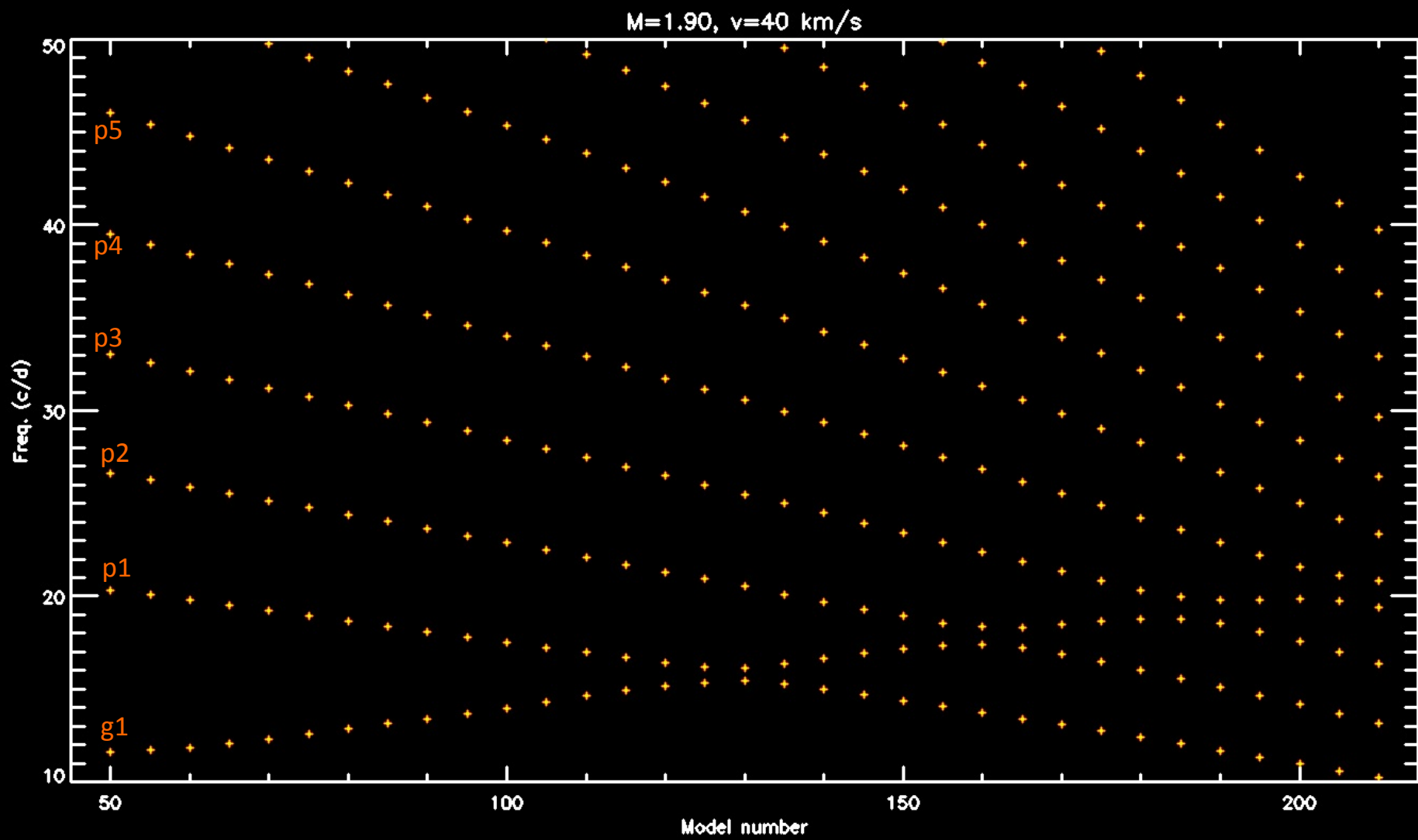
$L=0$

$L=1, m=0$



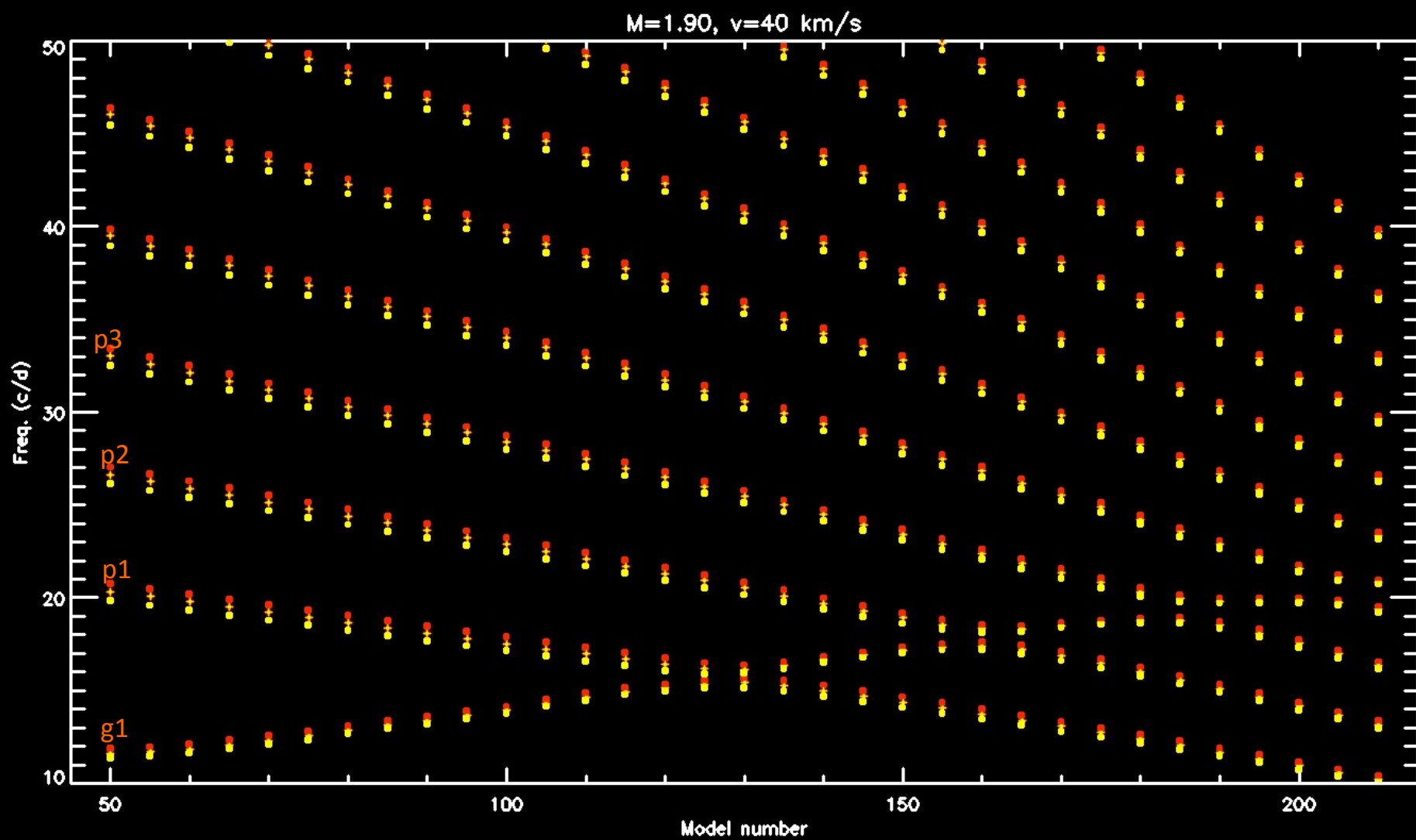
L=0

L=2, m=0

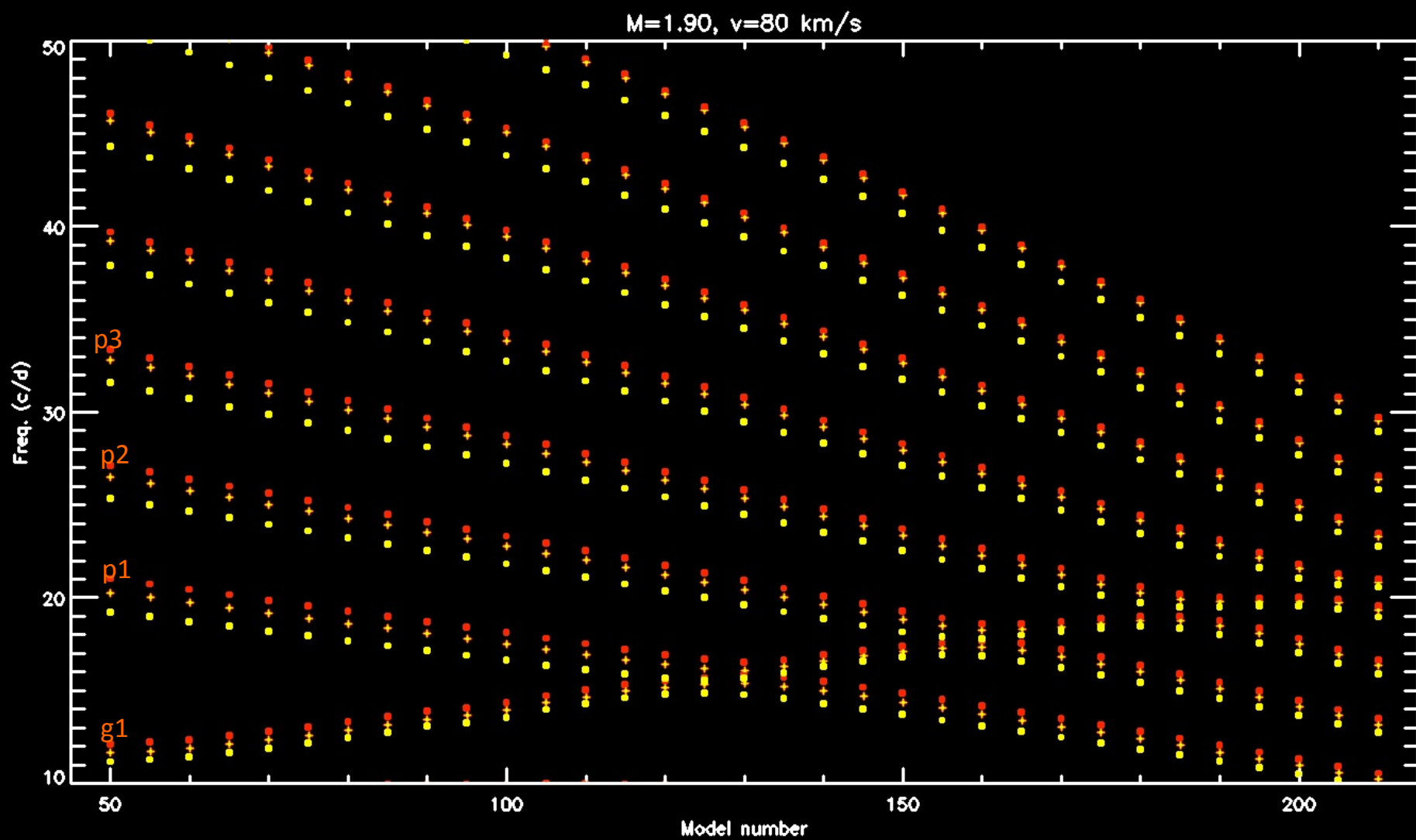


$L=1$ ,  $m=0$

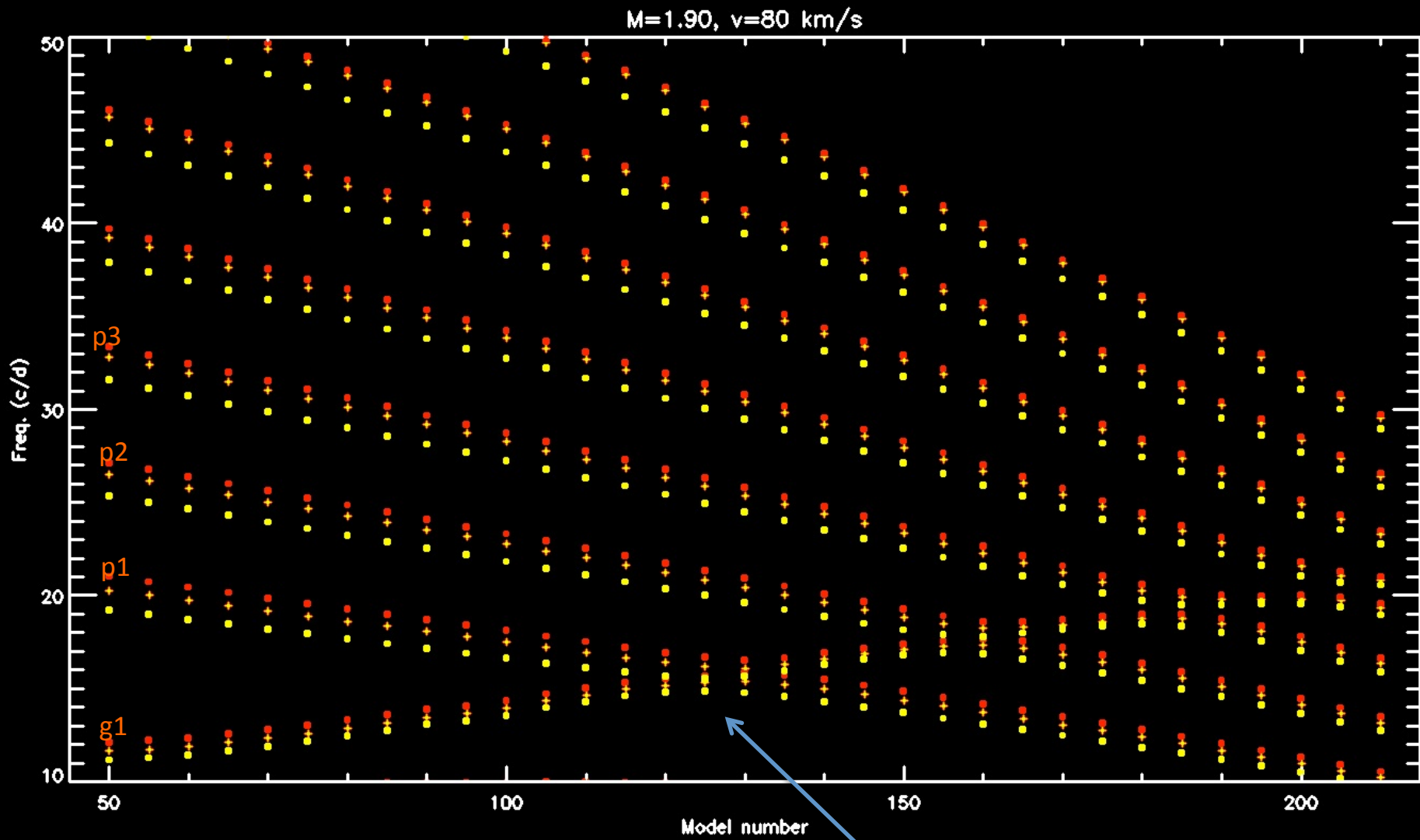




$L=1, m=0, +1, -1$

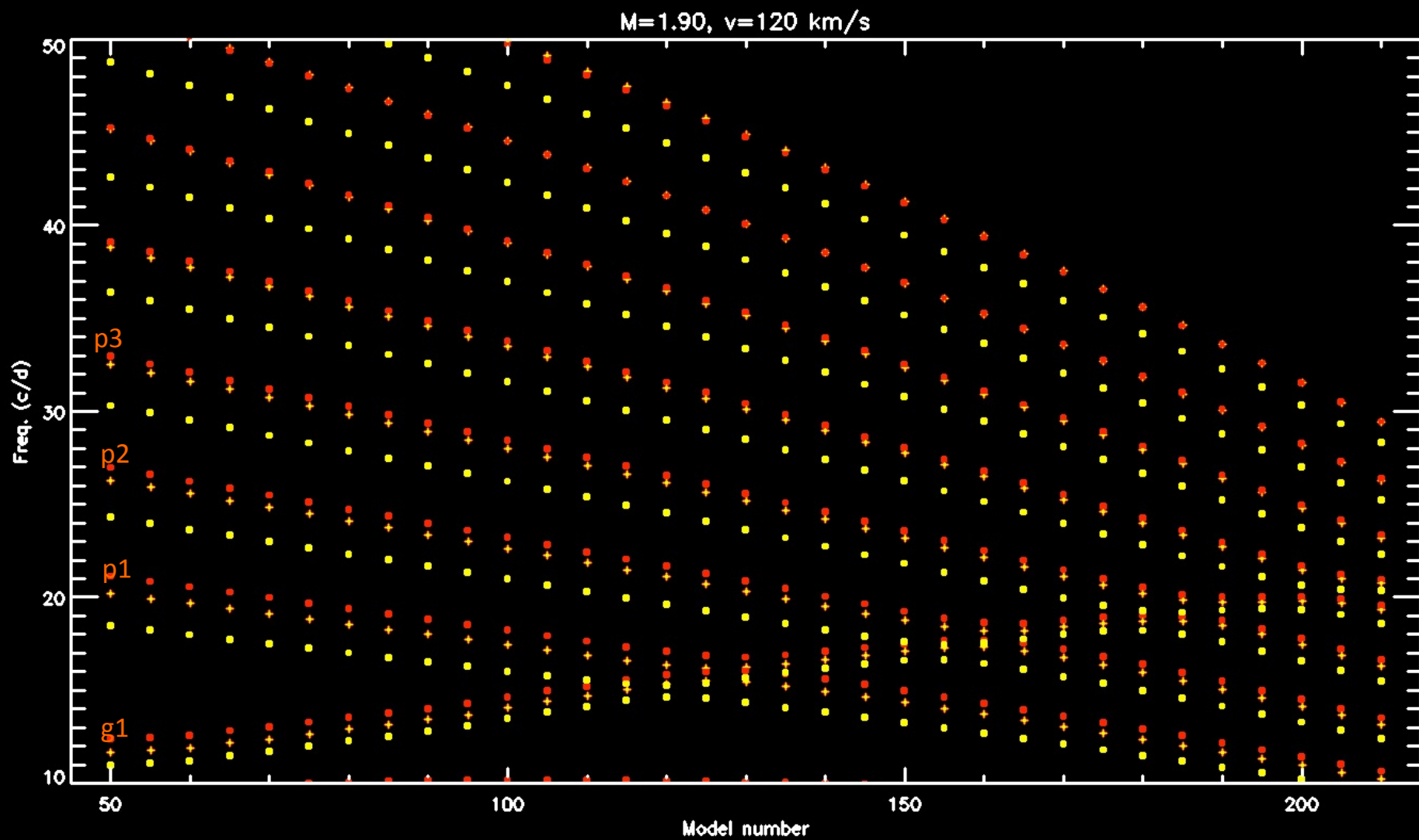


$L=1, m=0, +1, -1$

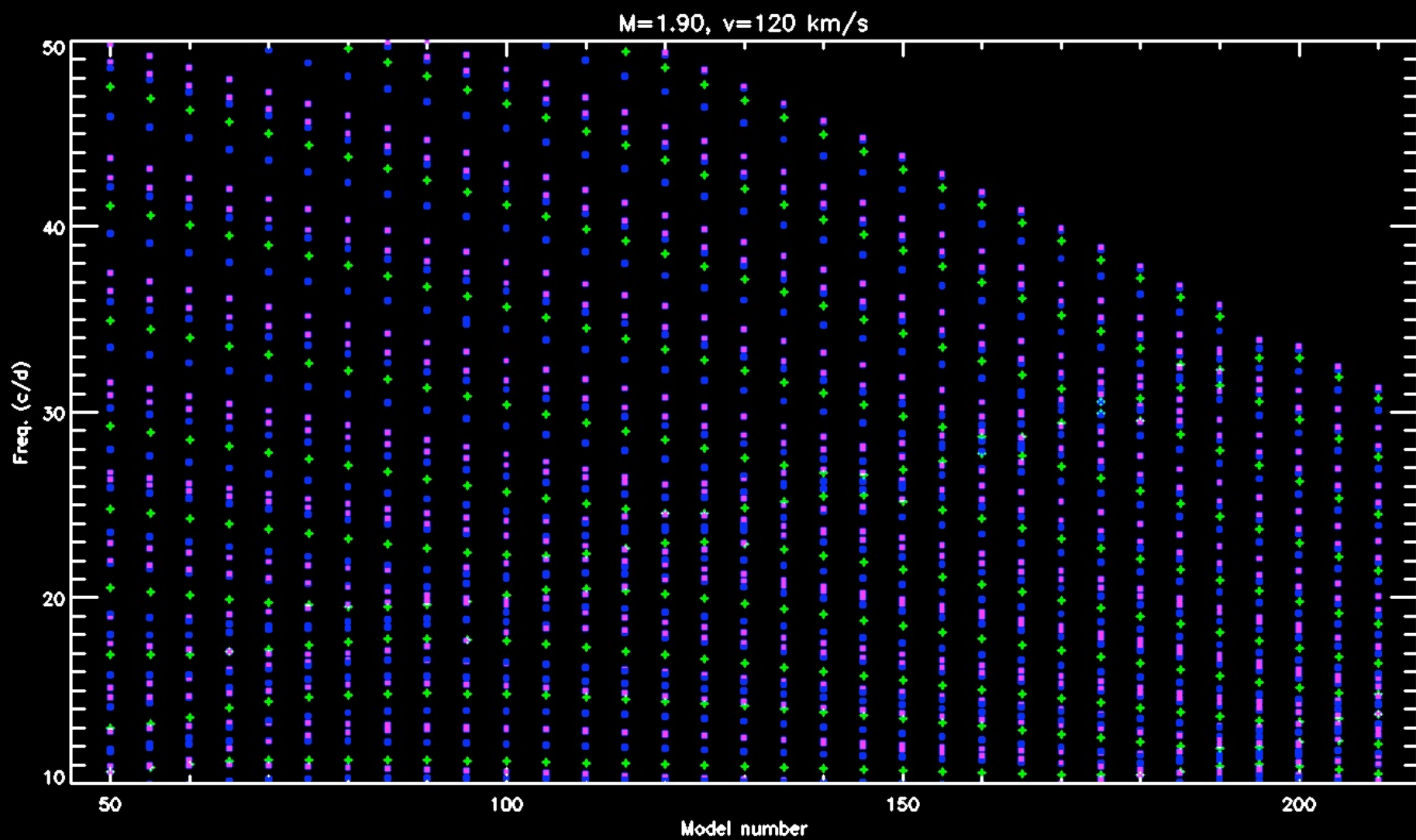


$L=1, m=0, +1, -1$

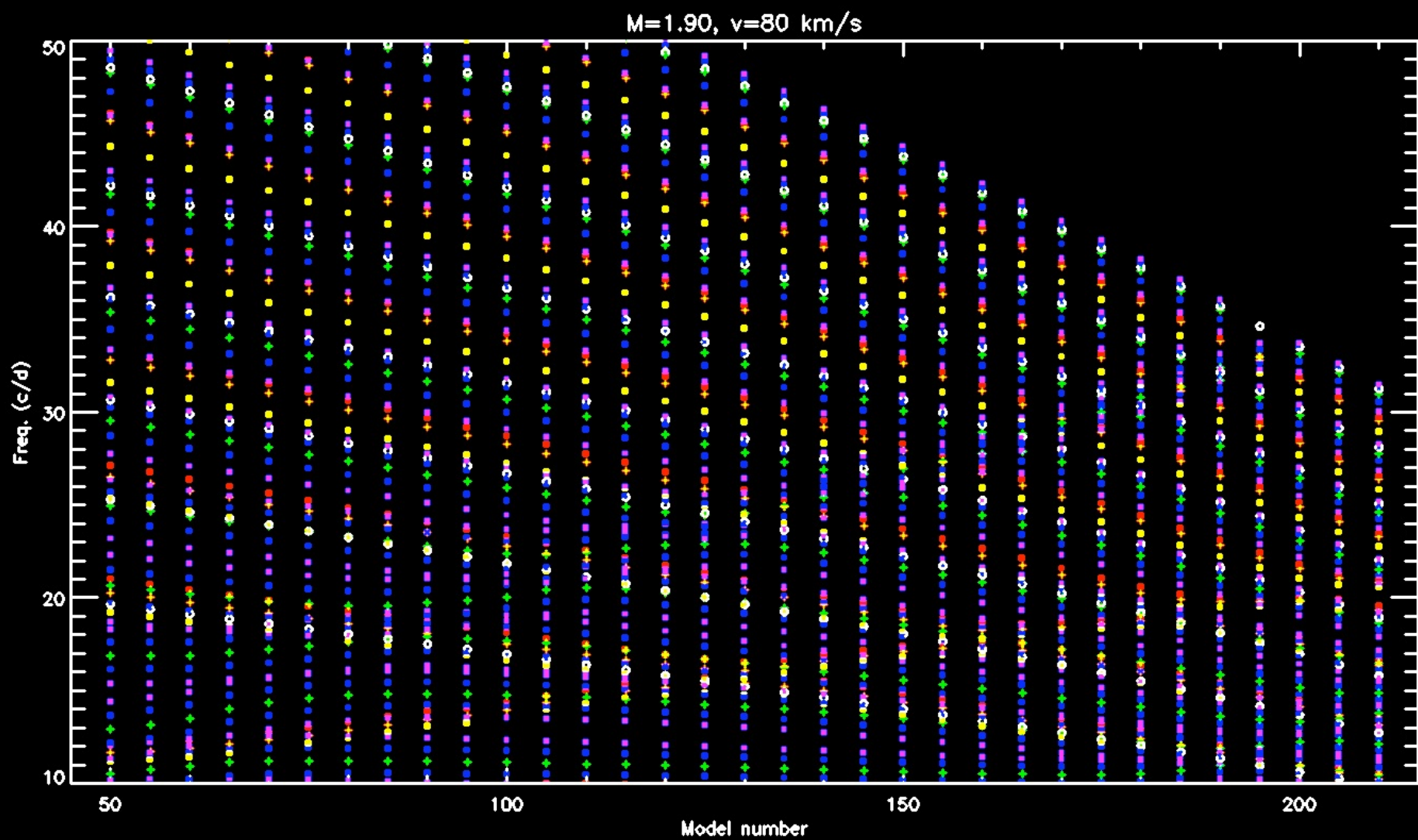
Avoided crossings  
Mode changing properties, as revealed from their  
rotational splittings

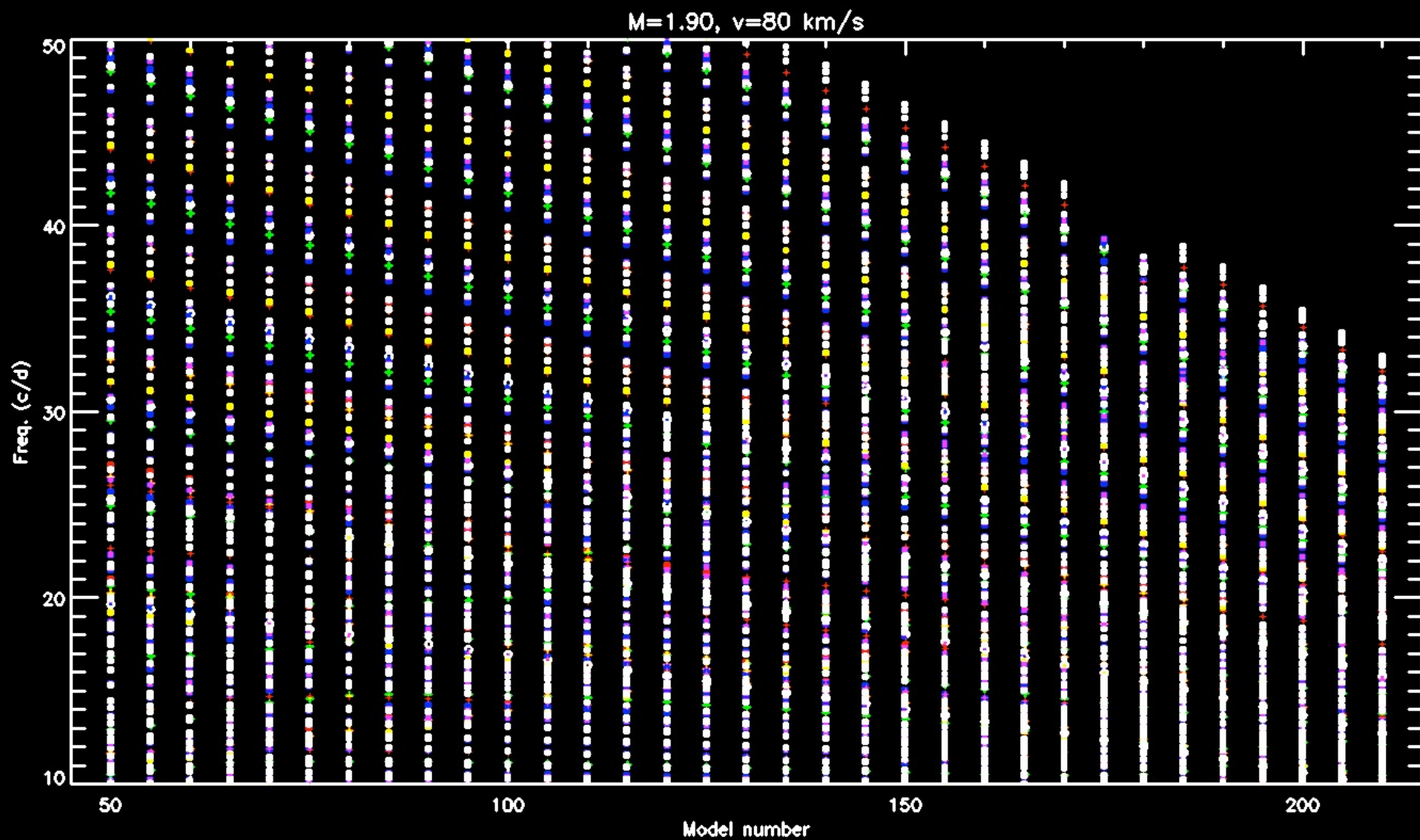


$L=1$ ,  $m=0$ ,  $+1$ ,  $-1$







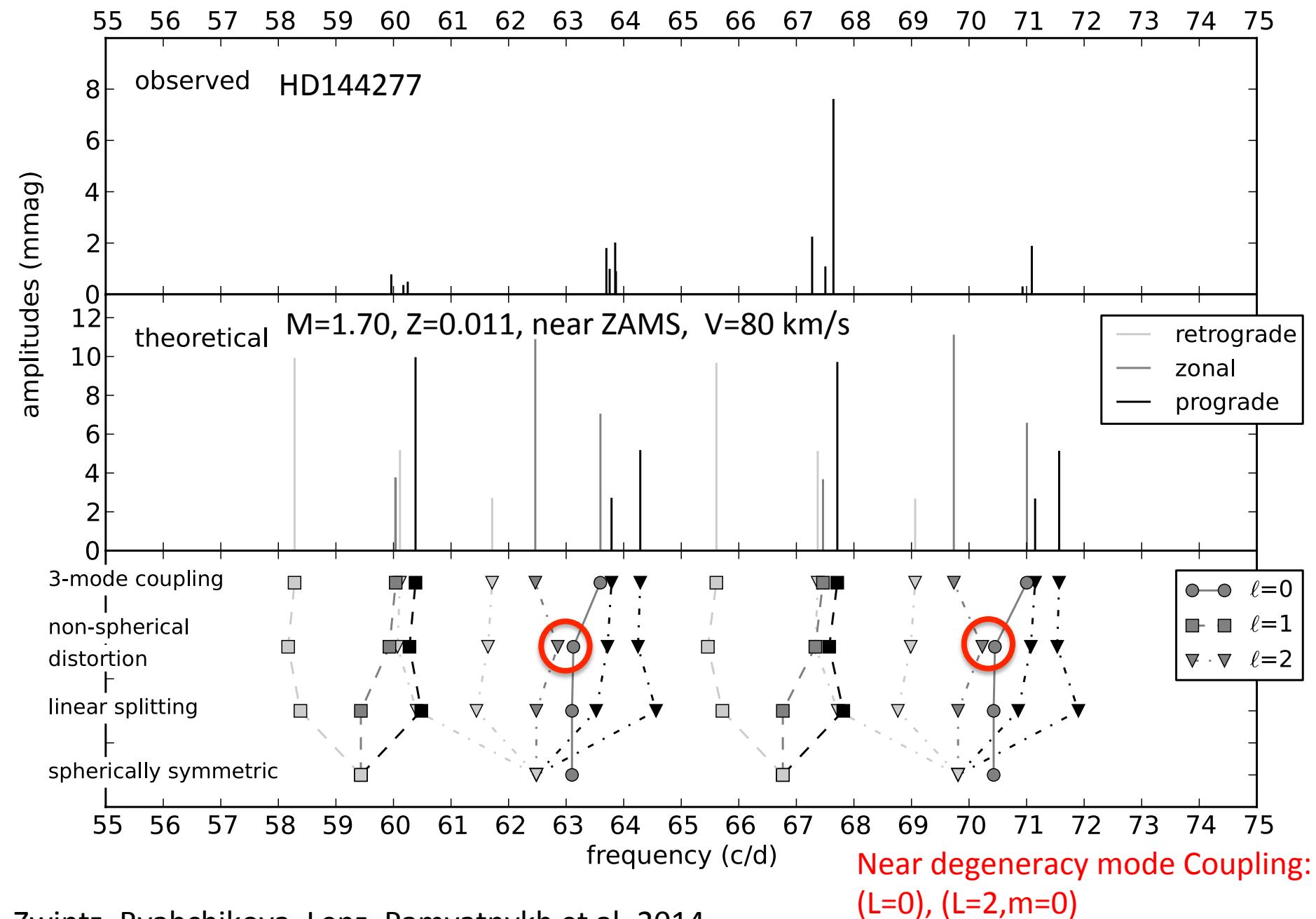


$L=0$

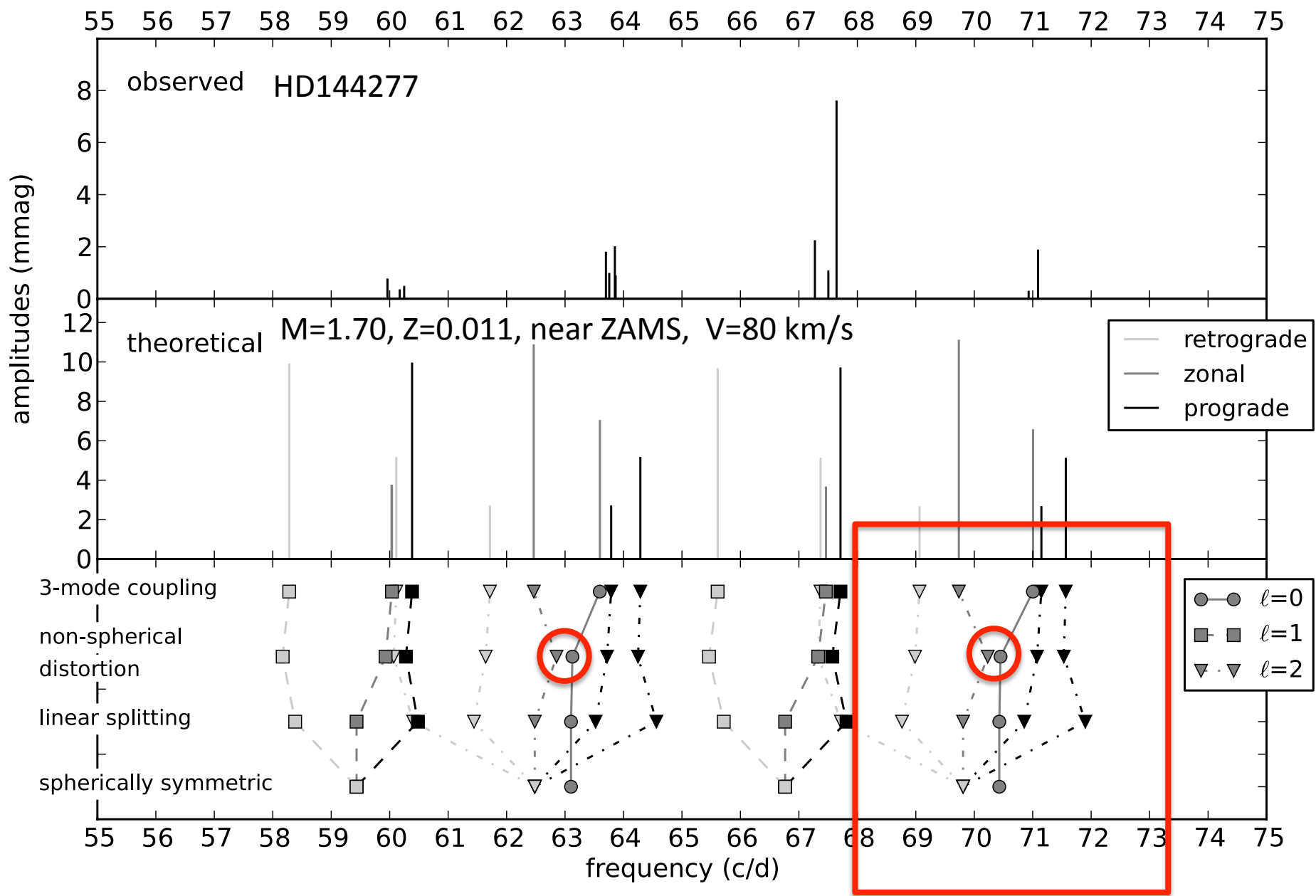
$L=1, m=0$  +1 -1

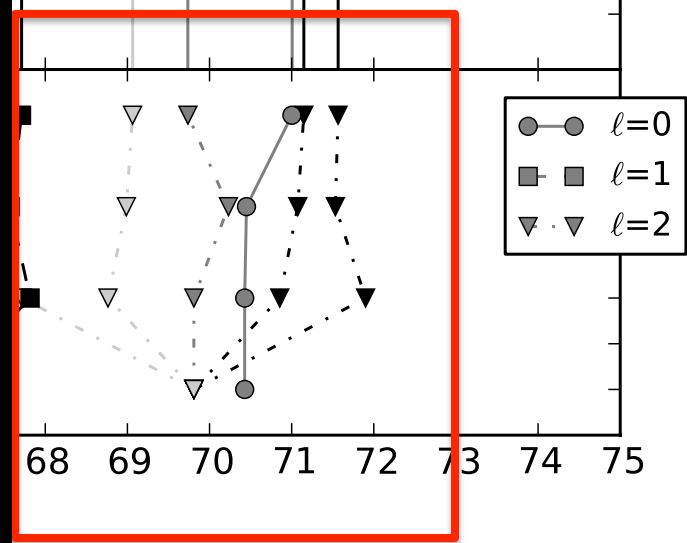
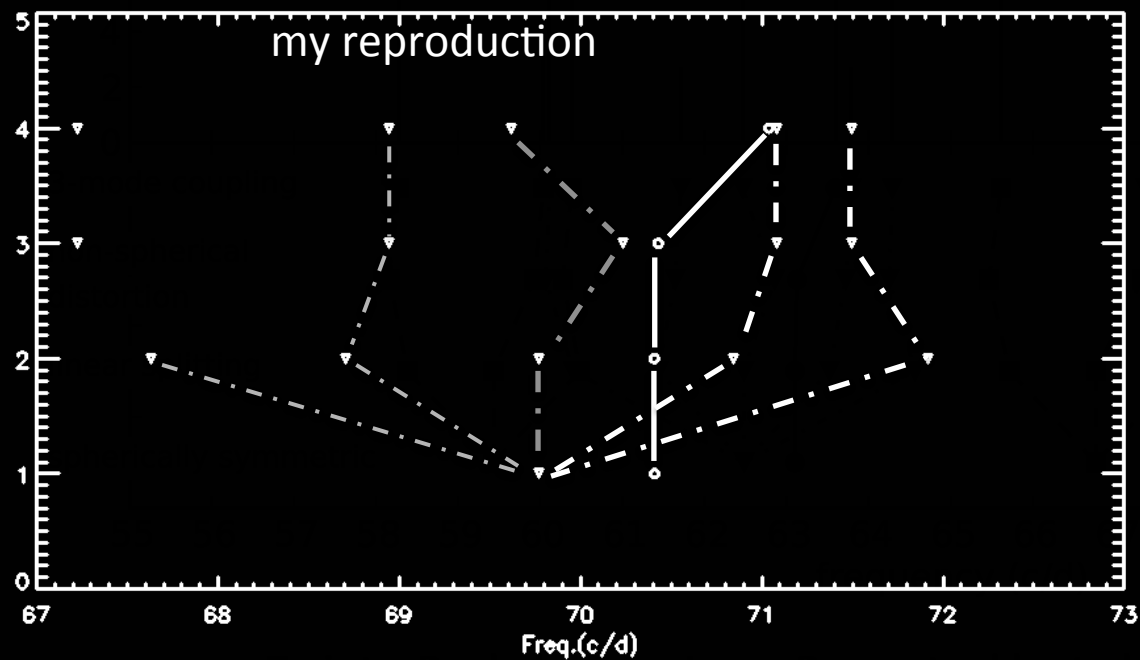
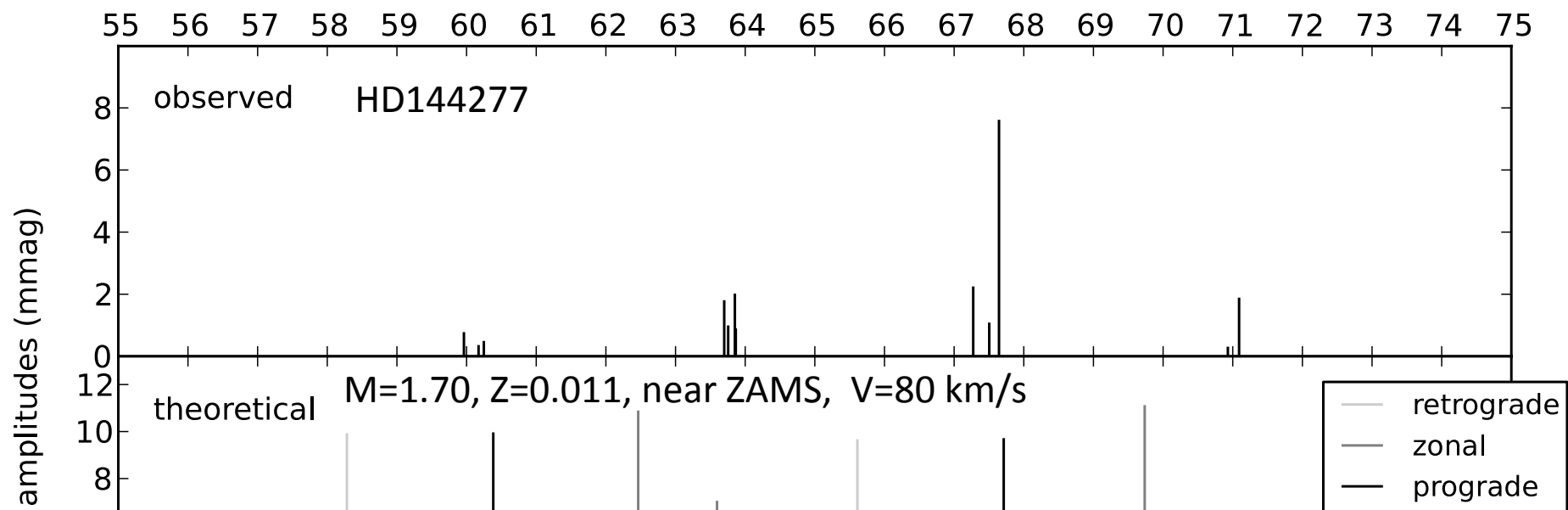
$L=2, m=0$  +1 +2 -1 -2

$L=3, m=(0, 1, 2, 3, -1, -2, -3)$









MLE

- Do you really think that ~~Chi<sup>2</sup> minimization~~ will give you the correct answer in the seismic modeling?

$$\chi^2 = \sum_{i=1}^{15} \left( \frac{v_{\text{obs}}^i - v_{\text{model}}^i}{\sigma^i} \right)^2$$

We do have some **prior knowledge**:  
mode selection, mode visibility, stellar evolution, ...

# A General Framework of Bayesian Inference

- Parameter to infer:  $\theta$
- Given observables (data):  $\mathbf{D}$
- We update our prior knowledge of  $\theta$ ,  $p(\theta)$  given  $\mathbf{D}$ , using Bayes' theorem
- posterior  $p(\theta | \mathbf{D}) = p(\theta) p(\mathbf{D} | \theta) / p(\mathbf{D})$

# $\Theta$ and $D$

## ***Isochrone fitting:***

Field stars:  $\Theta=[M, d, t]$       $D=[T_{\text{eff}}, \log g, Z]$

Star cluster:  $\Theta=[M_i, d, t, Z]$       $D=[T_{\text{eff}i}, \log g_i, Z_i]$

(Jorgensen & Lindegren 2005; Serenelli 2013)

## ***Eclipsing binaries:***

$\Theta=[M, Z, t, \dots]$       $D=[M_i, R_i, T_{\text{eff}i}, \log g_i, Z_i, \dots]$

(Prada Moroni 2012)

## ***Solar-like oscillators (SEEK package):***

$\Theta=[M, Z, t, X_0, \alpha \dots]$       $D=[T_{\text{eff}}, \log g, Z, \delta v, \Delta v, v_{\text{max}}, \dots]$

(Quirion 2010)

-> No mode ID problem

-> Individual frequencies not used

# $\Theta$ and $\mathbf{D}$ (Upper MS pulsators)

(without rotation)

- Parameters:  $\Theta = [M, Z, t, Li, n_i, f_{ov} \dots]$
- Given observables:  $\mathbf{D} = [R, T_{\text{eff}}, \log g, Z, f_i \dots]$

Turn the Prior knowledge into appropriate prior for theta  $p(\Theta)$

e.g.

$P(M)$ : initial mass function, e.g. Salpeter:  $m^{-2.35}$

$P(Z)$ : usually flat, but stars in cluster, halo? Pop I, II?

$P(t)$ : usually flat, evidence of youth? Old pop.?

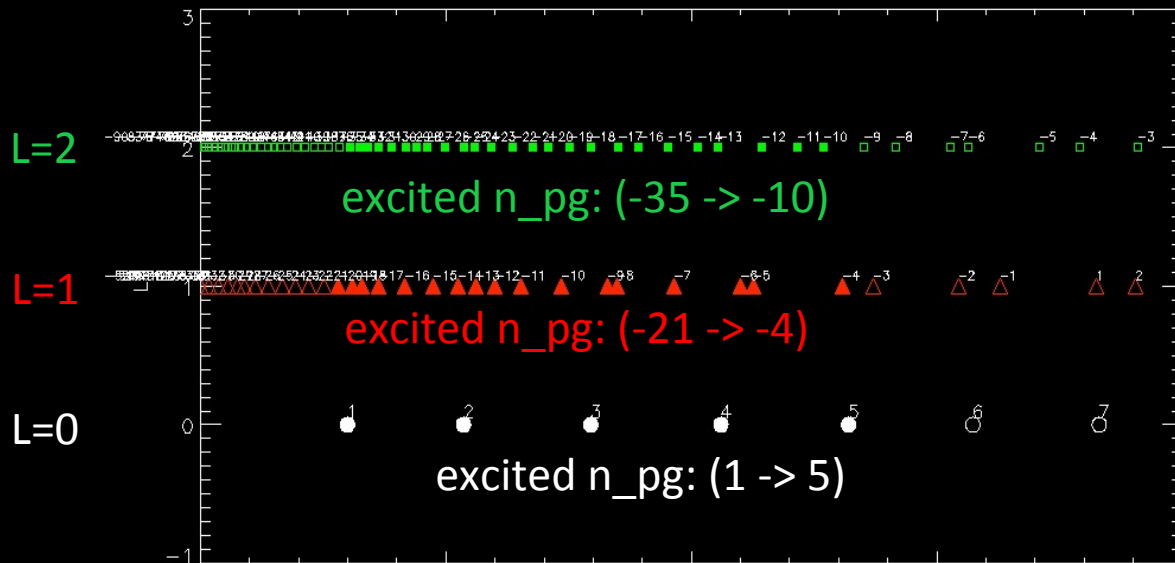
Priors on the mode degree and radial order

$P(L)$ :  $L=0,1,2$  more probable; HADs,  $L=0$ ;

$P(n)$ : excited modes  $\rightarrow$  higher probability

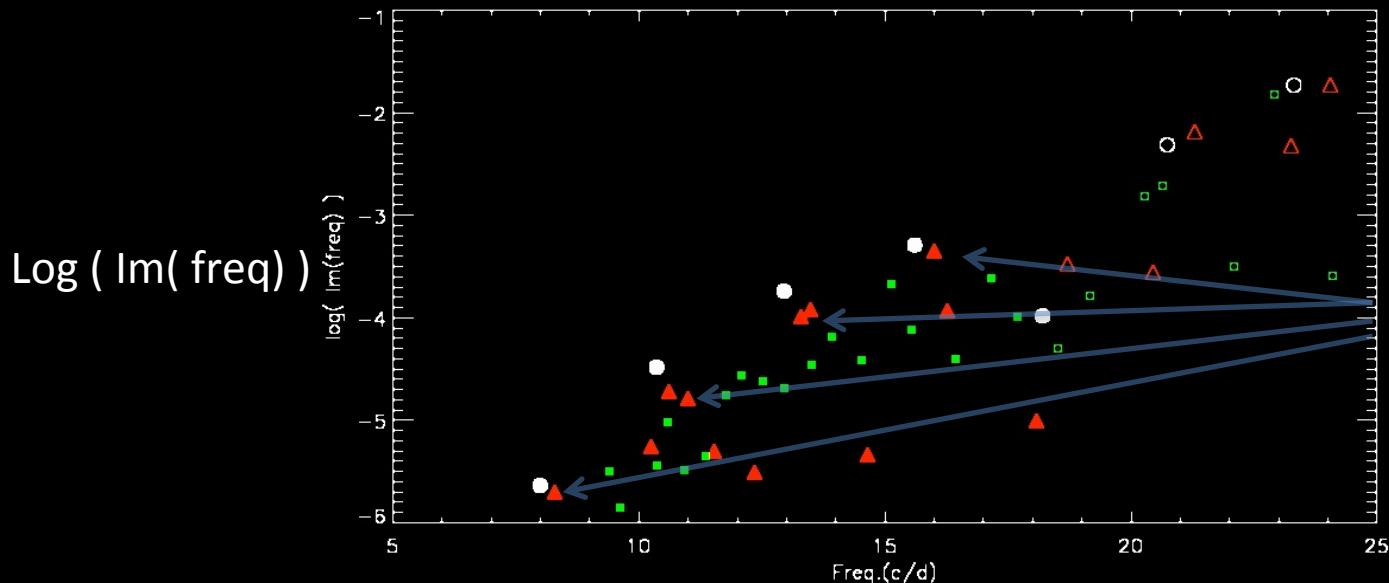
be careful, problems with excitation?

# Prior on n and L



-  $M=1.86$

$P(L)$ :  
Assign higher probability to  $L=0$  than  $L=1, 2$  ?



$P(n)$ :

Trapped L=1 modes:  
 $n_{pg} = -20, -14, -13, -9, -8, -6$

Should assign higher Probability, similar to  $L=0$  modes

# Steps: (one f)

$$\underset{\text{parameters}}{\boldsymbol{\theta}} = [M, t, l, n]$$


$$\underset{\text{observables}}{\mathbf{D}} = [M, R, T_{\text{eff}}, f]$$

Prior:

$$p(\boldsymbol{\theta}) = p(M)p(t)p(l)p(n)$$

Posterior:

$$p(\boldsymbol{\theta}|\mathbf{D}) = p([M, t, l, n]|\mathbf{D}) \propto p(M)p(t)p(l)p(n) \exp(-\chi^2/2)$$

$$\chi^2 = \sum \left[ \left( \frac{M_i - M_{\text{obs}}}{\sigma M_{\text{obs}}} \right)^2 + \left( \frac{R_{ij} - R_{\text{obs}}}{\sigma R_{\text{obs}}} \right)^2 + \left( \frac{T_{\text{eff},ij} - T_{\text{eff},\text{obs}}}{\sigma T_{\text{eff},\text{obs}}} \right)^2 + \left( \frac{f_{ij,ks} - f_{\text{obs}}}{\sigma f_{\text{obs}}} \right)^2 \right]$$


to get  $p(l|\mathbf{D})$  we marginalize over the rest parameters  $(M, t, n)$

$$p(l|\mathbf{D}) = \int p(M)p(t)p(l)p(n) \exp(-\chi^2/2) dM dt dn$$

( Posterior mode identification for L )



To evaluate:

$$p(l|\mathbf{D}) = \int p(M)p(t)p(l)p(n) \exp(-\chi^2/2) dM dt dn$$

Numerical integration:

$$p(l_k|\mathbf{D}) = \sum_i \sum_j \sum_s p(M_i)p(t_{ij})p(l_{ij,k})p(n_{ij,ks}) \exp(-\chi^2/2) \Delta M_i \Delta t_{ij} \Delta n_{ij,ks}$$

Details: a series of masses  $M_i$

for each mass  $M_i$ , there is a track, with different ages (index j)  $t_{ij}$

for each  $M_i, t_{ij}$  there are mode degrees  $l_k$  (usually  $k=0,1,2$ )

and for each  $l_k$  there are frequencies corresponding to radial orders (index s)  $n_{ks}$ .

This means  $[M, t, l, n]$  have corresponding indices of  $[i, j, k, s]$

similarly,  $p(n|\mathbf{D}) = \int p(M)p(t)p(l)p(n) \exp(-\chi^2/2) dM dt dl$

$$p(n_s|\mathbf{D}) = \sum_i \sum_j \sum_k p(M_i)p(t_{ij})p(l_{ij,k})p(n_{ij,ks}) \exp(-\chi^2/2) \Delta M_i \Delta t_{ij} \Delta l_{ij,k}$$

( *Posterior mode radial order n* )

## *Steps: (two frequencies: $f_a$ , $f_b$ )*

Let  $[M, t, la, na, lb, nb]$  have corresponding indices of  $[i, j, k, s, p, q]$ ,

$$p(la|\mathbf{D}) = \int p(M)p(t)p(na)p(lb)p(nb) \exp(-\chi^2/2) dM dt dna dlb dnb$$

$$p(la_k|\mathbf{D}) = \sum_i \sum_j \sum_s \sum_p \sum_q p(M_i)p(t_{ij})p(la_{ij,k})p(na_{ij,ks})p(lb_{ij,p})p(nb_{ij,pq}) \exp(-\chi^2/2) \\ \Delta M_i \Delta t_{ij} \Delta na_{ij,ks} \Delta lb_{ij,p} \Delta nb_{ij,pq}$$

Extend to more frequencies:

- > 15 frequencies for 44 Tau, two radial
- > 14 for 29 Cyg

# $\Theta$ and $\mathbf{D}$ (Upper MS pulsators)

(with rotation)

- Parameters:  $\Theta = [M, Z, t, L_i, n_i, m_i, f_{ov}, v, incl \dots]$
- Given observables:  $\mathbf{D} = [R, T_{eff}, \log g, Z, v \sin i, f_i, incl \dots]$
- $P(m_i)$ : depends on  $incl$ . (Gizon & Solanki 2003)  
But not entirely true for heat-driven pulsators, how to revise?
- $P(m_i)$ : some evidence of prograde mode preferred?
- $P(incl)$ : EBs? Interferometric imaging?

**CHANGING GEARS**



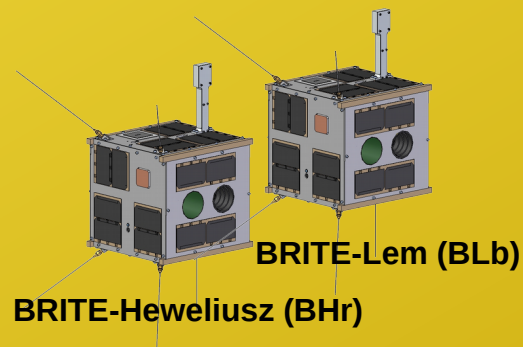
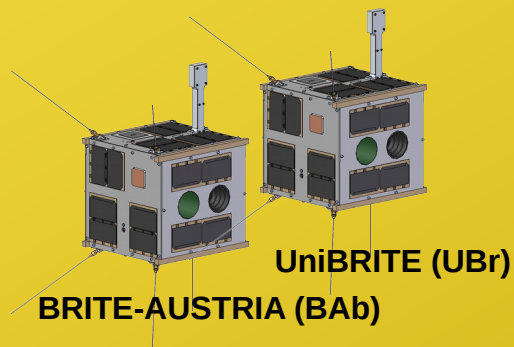
# What is BRITE?

## BRight Target Explorer

- nanosatellites 20 x 20 x 20 cm
- ca. 7 kg
- 3-cm telescope for observations of bright ( $V < 5$ ) stars
- time-resolved two-colour (B, R) photometry



## BRITE-Constellation:



# Lessons from BRITE:

(not in alphabetical order)

- Precision photometric studies with nanosatellites in low Earth orbits are possible
- gravity mode pulsation among  $\beta$  Cep stars is rather common  $\nu$  Eri,  $\alpha$  Lup, PT Pup,  $\sigma$  Sco
- interior rotation of SPB stars can be studied HD 201433
- magneto-asteroseismology is on the horizon  $\beta$  Cen,  $\epsilon$  Lup ...
- pulsation-mass loss interaction in Be stars  $\beta$  Cen, ...
- massive heartbeat stars are around and can be investigated  $\iota$  Ori
- a link between large-scale wind structures and their photospheric origin has been found

See Gerald Handler's talk at KITP

# BRITE observations so far

Field	from	to	$\Delta T$ [day]	# stars
Orion I	01.12.2013	18.03.2014	108	15
Centaurus	25.03.2014	18.08.2014	147	32
Sagittarius	29.04.2014	06.09.2014	42	19
Cygnus I	12.06.2014	25.11.2014	167	36
Perseus	02.09.2014	18.02.2015	170	37
<u>Orion II</u>	24.09.2014	17.03.2015	175	38
Vel/Pup	11.12.2014	28.05.2015	169	52
Scorpius	18.03.2015	31.08.2015	167	26
Cygnus II	01.06.2015	25.11.2015	178	27
Cas/Cep	23.08.2015	17.10.2015	55	23
CMa/Pup	18.10.2015	14.04.2016	~180	33
Cru/Car	22.01.2016	22.07.2016	183	45
<u>Cyg/Lyr</u>	05.04.2016	02.10.2016	177	20
Sgr II	21.04.2016	23.09.2016	158	17
Cas II	07.08.2016	03.02.2017	~174	18
Aur/Per	14.09.2016	07.03.2017	~171	25
Cet/Eri	06.10.2016	26.12.2016	83	11
Vel/Pic	04.11.2016	29.04.2017	173	21
Total				~410

Courtesy: Gerald Handler

*BRITE photometry Wiki page:* <http://brite.craq-astro.ca/doku.php>

# 17-CygLyr-I-2016

#	angDiam(mas)	HD	Name	V	Sp.Type	Contact PI	TNDP1)	Data avail.2)
1	3.220	172167	$\alpha$ Lyr	0.03	A0 Va	Huber	76372	PP
2	0.577	173648	$\zeta_1/\zeta_2$ Lyr	4.36/5.70	A4m	Lüftinger	90498	PP
3	0.681	174638	$\beta$ Lyr	3.45	B8 IIpe	Rucinski	91253	PP
4	12.28	175588	$\delta_2$ Lyr	4.30	M4 II	Paunzen	84634	PP
5	0.730	176437	$\gamma$ Lyr	3.24	B9 III	Paunzen	90975	PP
6	0.219	178475	$\iota$ Lyr	5.28	B7 IV	Pigulski	65810	PP
7	0.253	180163	$\eta$ Lyr	4.39	B2.5 IV	Handler	68946	PP
8	0.217	182255	3(V377)Vul	5.18	B6 III	Kallinger	49551	PP
9	0.204	182568	2 Cyg	4.97	B3 IV	Kallinger	65720	PP
10	----	183912	$\beta$ Cyg	3.08/5.16	K3 II+B9.5 V	Baade	71158	PP
11	0.658	184006	$\iota$ Cyg	3.77	A5 V	Huber	19174	PP
12	0.219	184171	8 Cyg	4.74	B3 IV	Handler	66430	PP
13	0.699	187013	17 Cyg	4.99	F5.5 IV-V	Paunzen	3267	PP
14	2.708	188947	$\eta$ Cyg	3.88	K0 III	Kallinger	15939	PP
15	0.477	189849	15(NT)Vul	4.66	A4 III	Smalley	3254	PP
16	----	191610	28(V1624)Cyg	4.93	B2.5 Ve	Baade	66181	PP
17	0.405	192640	29(V1644)Cyg	4.97	A2 V	Zwintz	65023	PP
18	----	192685	QR Vul	4.78	B3 IIIe	Baade	64650	PP
19	----	193237	34(P) Cyg	4.81	B1.5	Iabe/Richardson	65706	PP
20	2.155	197345	$\alpha$ Cyg	1.25	A2 Ia	Richardson	6752	PP

# 22 Ori-IV 2016

#	AngDiam(UD_K)	HD	Name	V	Sp.Type	Contact PI	TNDP1)	Data avail.2)
1	0.271	29248	$\nu$ Eri	3.93	B2 III	Handler	57035	PP
2	0.305	30211	$\mu$ Eri	4.02	B5 IV	Pigulski	57699	PP
3	0.508	30739	$\pi_2$ Ori	4.35	A1 Vn	Baade	27724	PP
4	0.308	30836	$\pi_4$ Ori	3.69	B2 III + B2 IV	Handler	57686	PP
5	0.286	31237	$\pi_5$ Ori	3.72	B3 III + B0 V	Handler	28337	PP
6	0.225	33328	$\lambda$ Eri	4.27	B2 IVne	Hubrig	28388	PP
7	2.690	34085	$\beta$ Ori	0.12	B8 Ia	Guinan	29482	PP
8	0.420	34503	$\tau$ Ori	3.60	B5 III	Pigulski	22175	PP
9	0.184	34816	$\lambda$ Lep	4.29	B0.5 IV	Pigulski	27865	PP
10	0.307	35411	$\eta$ Ori	3.36	B1V + B2	Pigulski	50918	PP
11	0.161	35439	$\psi_1$ Ori	4.95	B1 Vpe	Baade	28595	PP
12	0.702	35468	$\gamma$ Ori	1.64	B2 III	Handler	21863	PP
13	0.190	35715	$\psi_2$ Ori	4.59	B2 IV	Pigulski	58580	PP
14	-----	36486	$\delta$ Ori	2.23	09.5 II	Moffat	58530	PP
15	-----	36861/2	$\lambda$ Ori	3.54/6.32	08 III/B0.5 V	Moffat	29434	PP
16	0.090	37043	$\iota$ Ori	2.77	09 III	Moffat	29759	PP
17	-----	37128	$\epsilon$ Ori	1.70	B0 Ia	Moffat	51627	PP
18	0.080	37468	$\sigma$ Ori	3.81	09.5 V	Moffat	57871	PP
19	0.232	37490	$\omega$ Ori	4.57	B3 IIIe	Baade	27611	PP
20	----	37742/3	$\zeta$ Ori	1.88/3.70	09.7 Ib/B0 III	Moffat	57925	PP
21	0.547	38771	$\kappa$ Ori	2.06	B0.5 Ia	Moffat	29548	PP
22	-----	39801	$\alpha$ Ori	0.50	M1-2 Ia-Iab	Guinan	29200	PP

**Cross-match  
BRITE with  
JMMC catalog**



Iota Ori

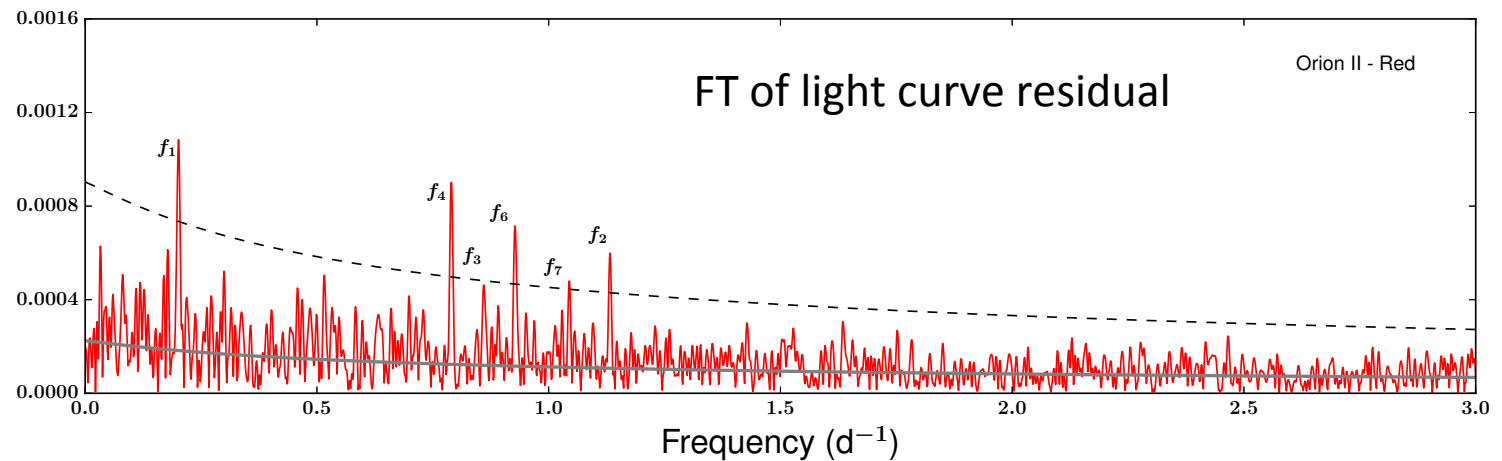
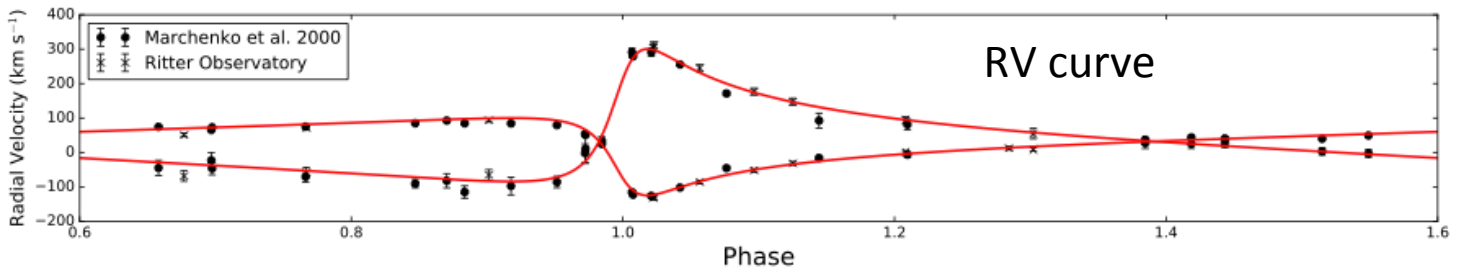
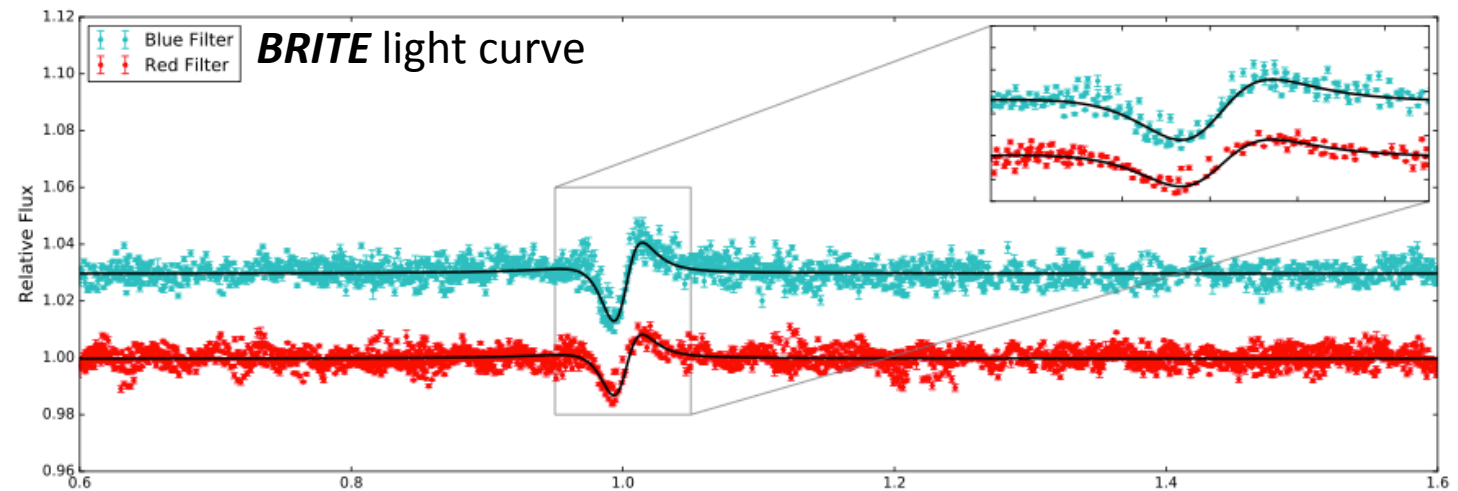
O9 III +  
B1 III/IV

$P=29$  d  
 $e=0.75$   
 $\omega = 122$

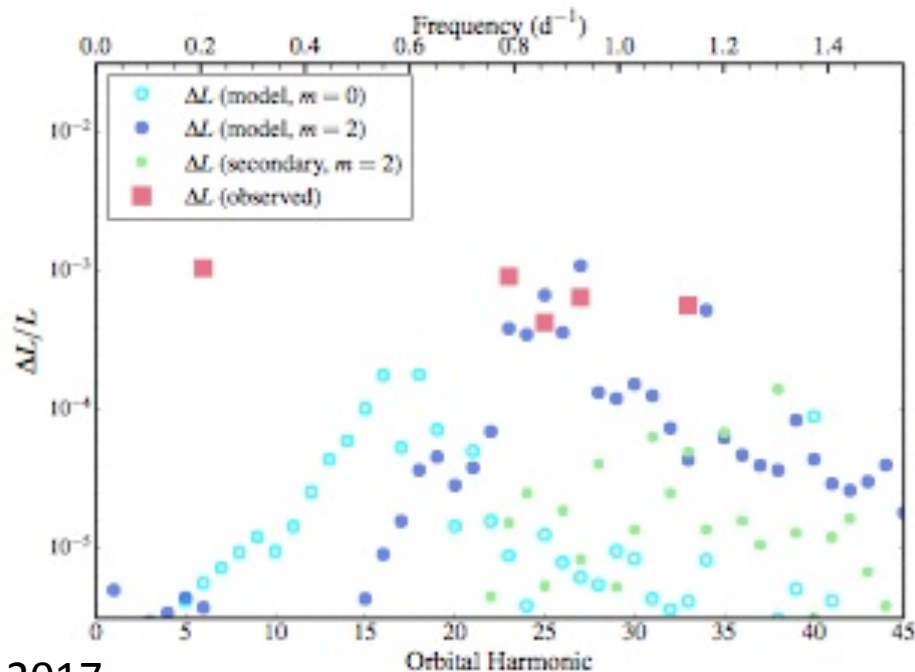
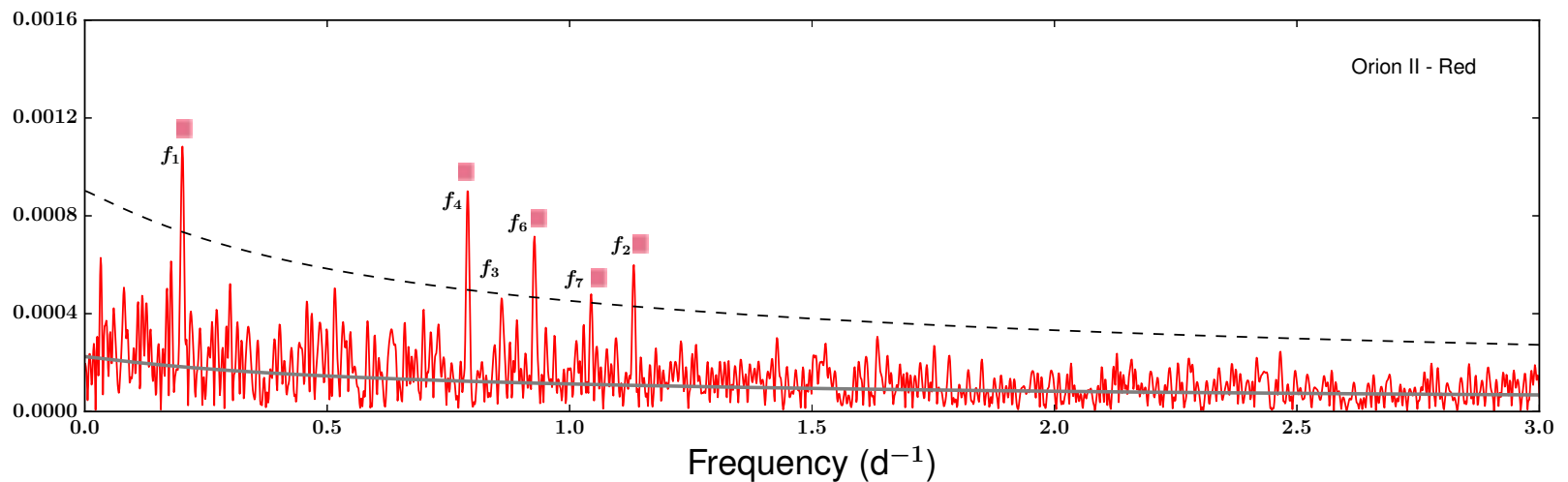
Incl. = 63

$M_1=22$ ,  
 $R_1=9.1$   
 $T_{\text{eff}1}=31000$

$M_2=13.4$ ,  
 $R_2=4.94$   
 $T_{\text{eff}2}=18319$



Pablo et al. 2017

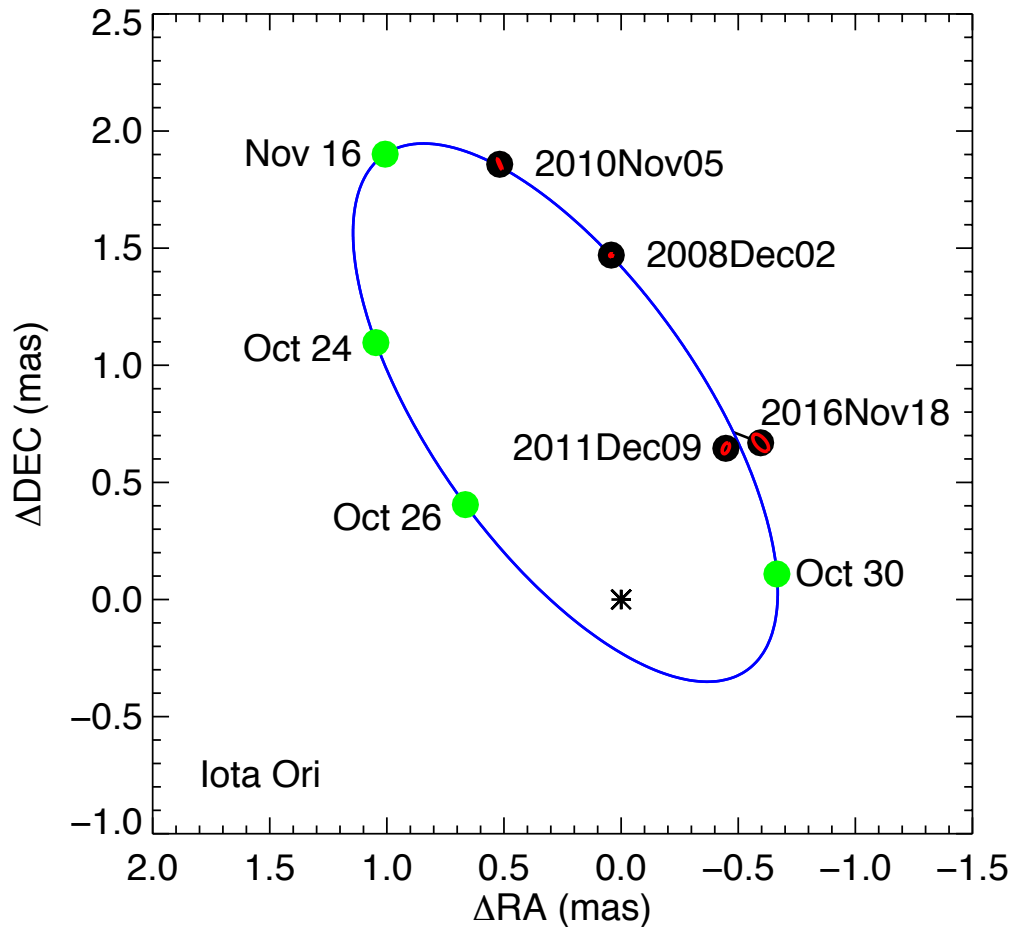


Theory works

Amplitudes agree with  
L=2 m=2 prograde  
modes

Phases: most agree with  
L=2, m=2

# Interferometric Orbit of *Iota Ori* CHARA/MIRC



Preliminary results:

$$a = 1.66 \pm 0.45 \text{ mas}$$

$$i = 65^\circ \pm 12^\circ$$

$$M1 = 22 \pm 6 M_\odot$$

$$M2 = 13 \pm 4 M_\odot$$

$$d = 363 \pm 103 \text{ pc}$$

● Scheduled observations 2017

Pablo et al. 2017

$$i = 62.86^\circ \pm 0.17^\circ$$

$$M1 = 22.2 \pm 0.6 M_\odot$$

$$M2 = 13.4 \pm 0.3 M_\odot$$



By Gail Schaefer & Doug Gies

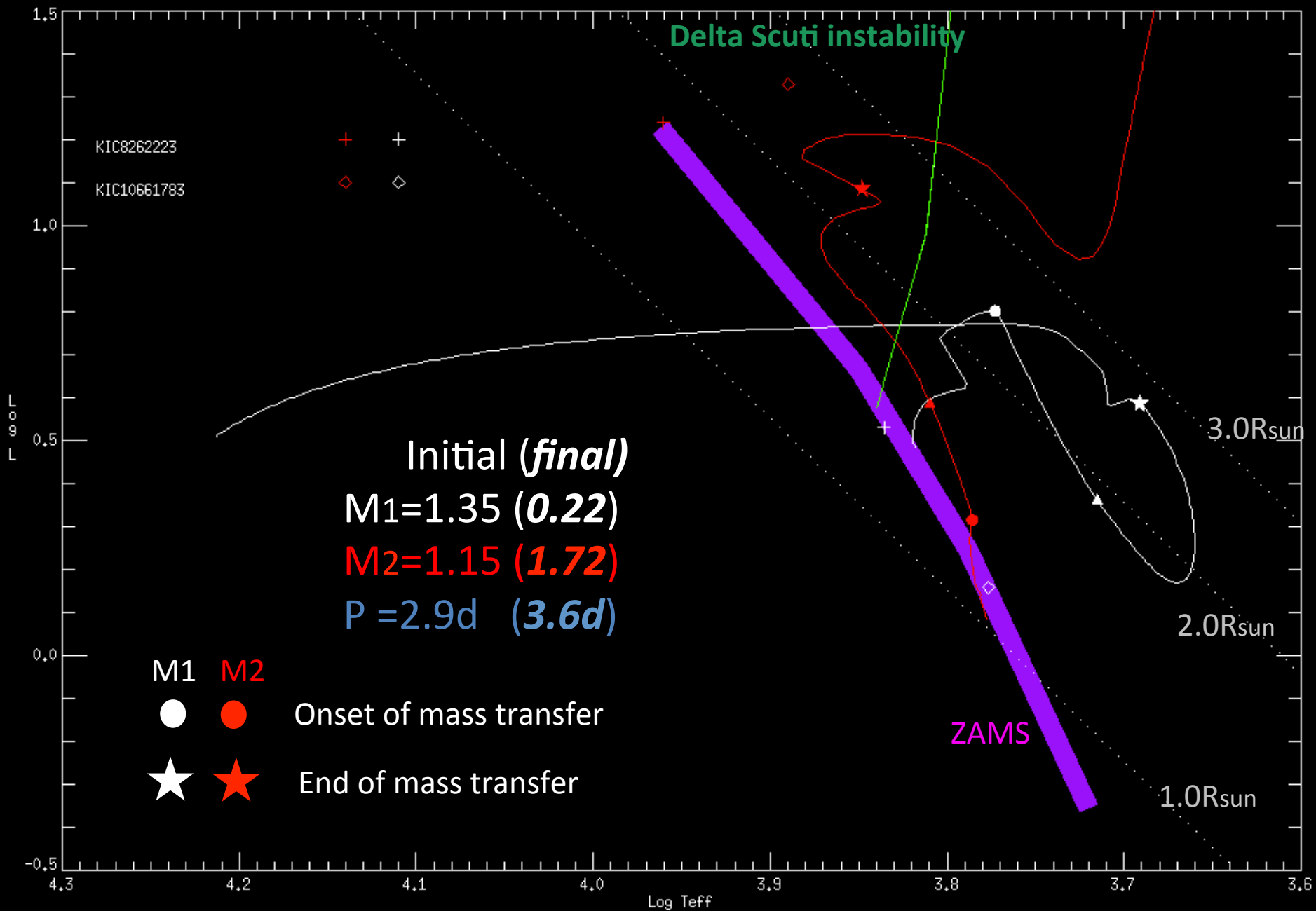
# Summary

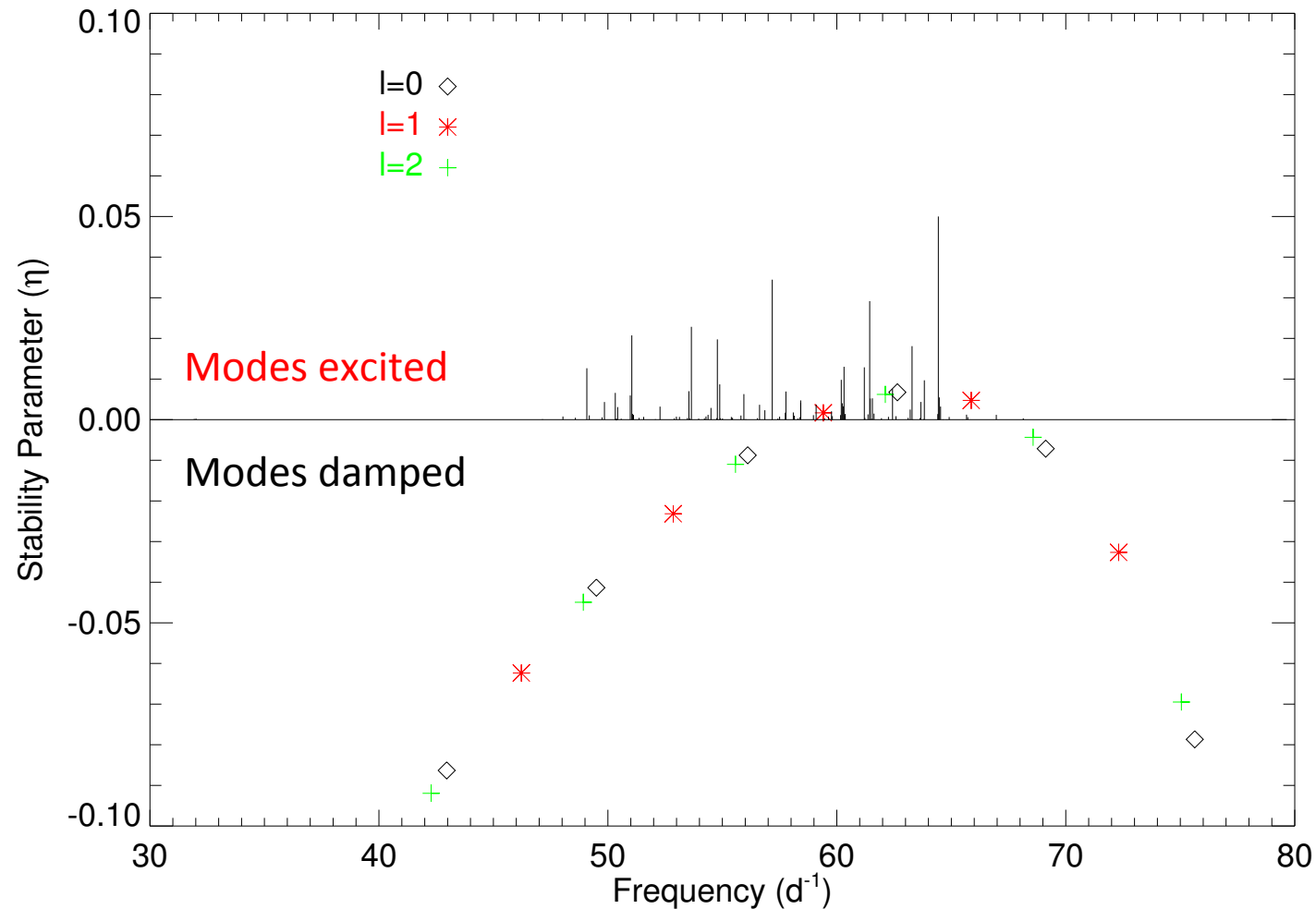
1. *Angular diameter measurements of 44 Tau and 29 Cyg*
2. *A probabilistic approach of seismic modeling of  $\delta$  Scuti stars, taking into account our prior knowledge on rotation, stellar evolution, and mode selection.*
3. *A lot of interesting asteroseismic targets from BRITE satellite, awaiting for interferometric observations*

*Thanks very much for your attention!*

## KIC8262223 Parameters

Period (days)	1.61301476 <sup>a</sup>
Time of primary minimum (HJD-2400000)	$55432.522844 \pm 0.000007$
Mass ratio $q = M_2/M_1$	$0.104 \pm 0.002$
Orbital eccentricity $e$	0.0 <sup>a</sup>
Orbital inclination $i$ (degree)	$75.203 \pm 0.007$
Semi-major axis $a$ ( $R_\odot$ )	$7.45 \pm 0.11$
$M_1$ ( $M_\odot$ )	$1.94 \pm 0.06$
$M_2$ ( $M_\odot$ )	 $0.20 \pm 0.01$
$R_1$ ( $R_\odot$ )	$1.67 \pm 0.03$
$R_2$ ( $R_\odot$ )	 $1.31 \pm 0.02$
$T_{\text{eff}1}$ (K)	9128 <sup>a</sup>
$T_{\text{eff}2}$ (K)	$6849 \pm 15$
$\log g_1$ (cgs)	$4.28 \pm 0.04$
$\log g_2$ (cgs)	$3.51 \pm 0.06$

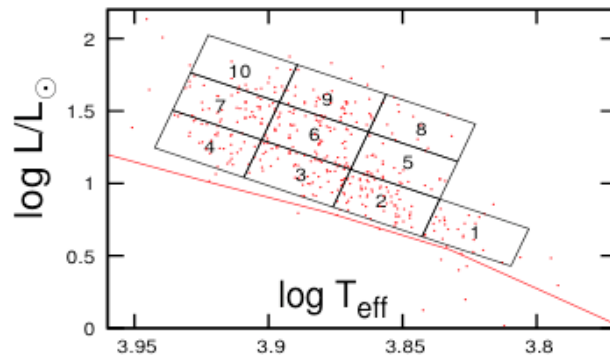




Primary  
star:

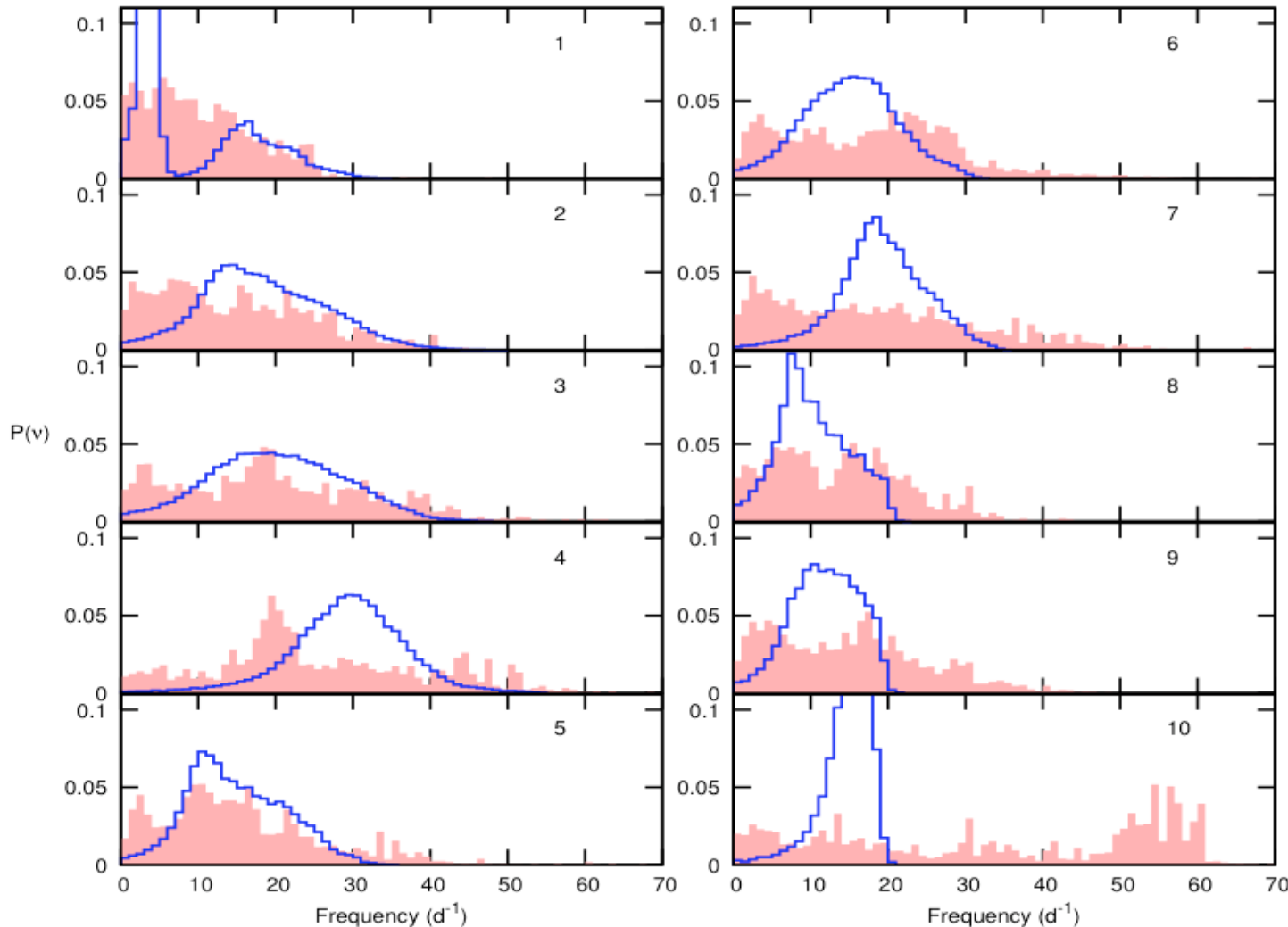
$$M_1 = 1.94M_{\odot}, R_1 = 1.67R_{\odot}, Z = 0.02, \text{ and } Y = 0.28,$$

Structure Models from single stellar evolution have some difficulties explaining the driving (unstable range) frequencies of this Post-mass transfer Delta Scuti star KIC8262223



## Frequency Distribution of Kepler Delta Scuti stars

Balona, Daszynska, Pamyatnykh (2015)



Models (blue lines)  
cannot explain  
the overabundance  
of high-frequency  
Delta Scuti stars.

***Binary  
Evolution  
?***



# Scientific results: magnetic stars

**Table 1.** Known magnetic massive pulsators, having  $N$  detected pulsation modes.

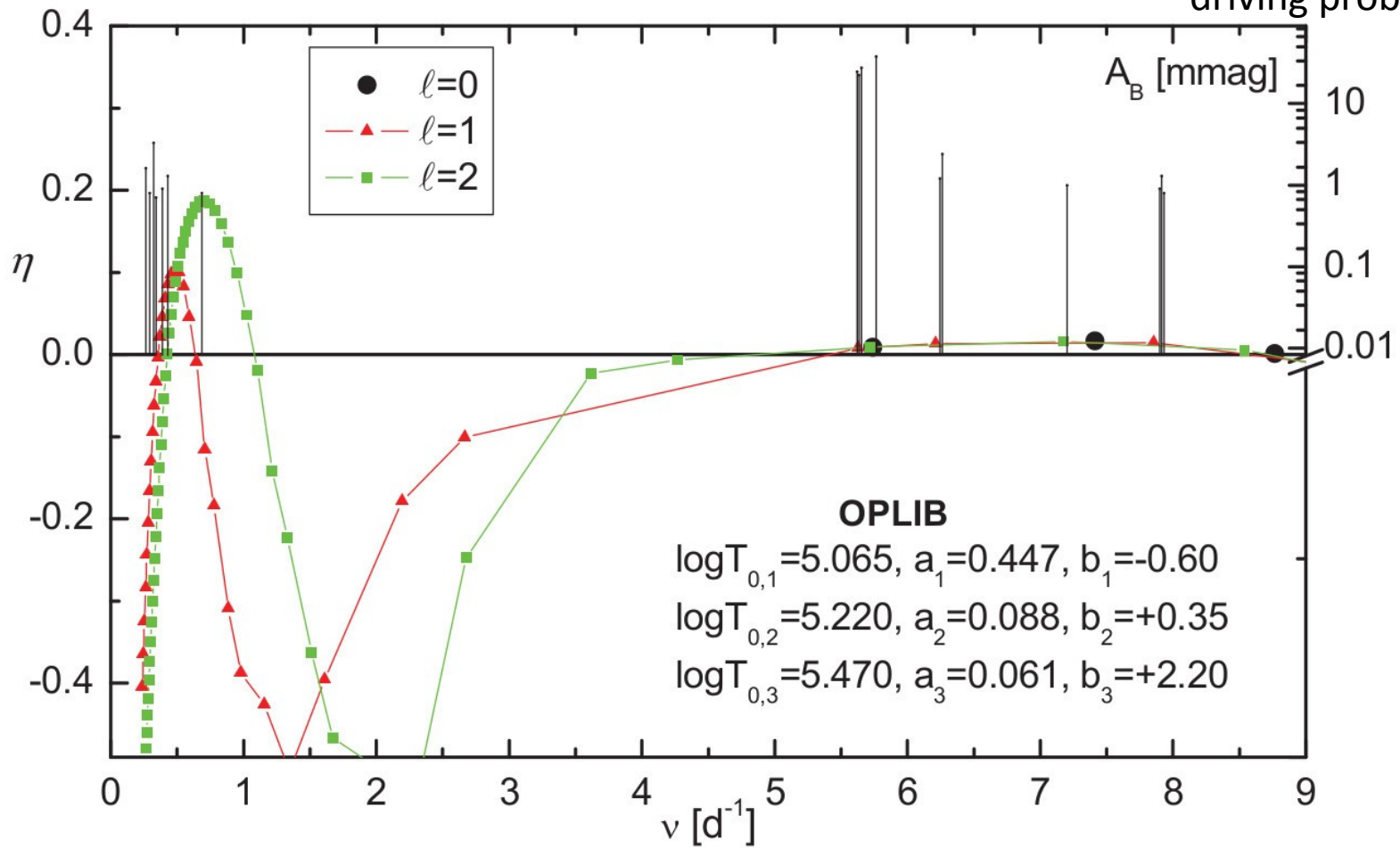
	Star	$N$	Type	$P_{\text{rot}}$ [d]	$B_{\text{pol}}$ [G]	Magnetic characterization	Binary?	SpT	References
1	HD 43317	> 100	both	0.90	$\sim 900$	dip.; $i \in [20, 50]^\circ$ ; $\beta \in [70, 86]^\circ$		B3IV	(1), (2)
2	$\beta$ Cen Ab	< 17	$\beta$ Cep		$\sim 250$		Y	+ B1III	(3), (4)
3	$\beta$ Cep	5	$\beta$ Cep	12.0	$\sim 300$	dip.; $i \sim 60^\circ$ ; $\beta \sim 95^\circ$	Y	B0III +	(5), (6)
4	V2052 Oph	3	$\beta$ Cep	3.64	$\sim 400$	dip.; $i \sim 70^\circ$ ; $\beta \sim 35^\circ$		B2IV/V	(7), (8), (9)
5	$\beta$ CMa	3	$\beta$ Cep		< 30			B1II/III	(10), (11), (12)
6	16 Peg	3	$\beta$ Cep	1.44	$\sim 500$	dip.; $i \sim 70^\circ$ ; $\beta \sim 70^\circ$		B3V	(13), (14), (15)
7	$\epsilon$ Lup A	'LPV bump'	$\beta$ Cep		$\sim 600$		Y	B2V +	(16), (17)
	$\epsilon$ Lup B	> 2	$\beta$ Cep		$\sim 300$		Y	+ B3V	(16), (18)
8	$\xi^1$ CMa	1	$\beta$ Cep	2.18	$\sim 600$			B1V	(19), (20)
9	HD 96446	1	$\beta$ Cep	23.4	$\sim 7500$			B2IIIp	(21), (22), (23)
10	$\zeta$ Cas	1?	SPB	5.37	$\sim 150$	dip.; $i \sim 30^\circ$ ; $\beta \sim 105^\circ$		B2IV/V	(24), (25)
11	$\sigma$ Lup	1?	SPB	3.09	$\sim 300$	dip.; $i \sim 60^\circ$ ; $\beta \sim 90^\circ$		B2III	(26), (14)
12	$\phi$ Cen	'LPV bump'	$\beta$ Cep	1.14	$\sim 900$			B2IV	(27), (28)

(Buysschaert, Neiner & Aerts 2017, Proc. IAUS 329, in press)

# Scientific results: asteroseismology

g modes, g modes everywhere!

Beta Cephei star  
driving problems



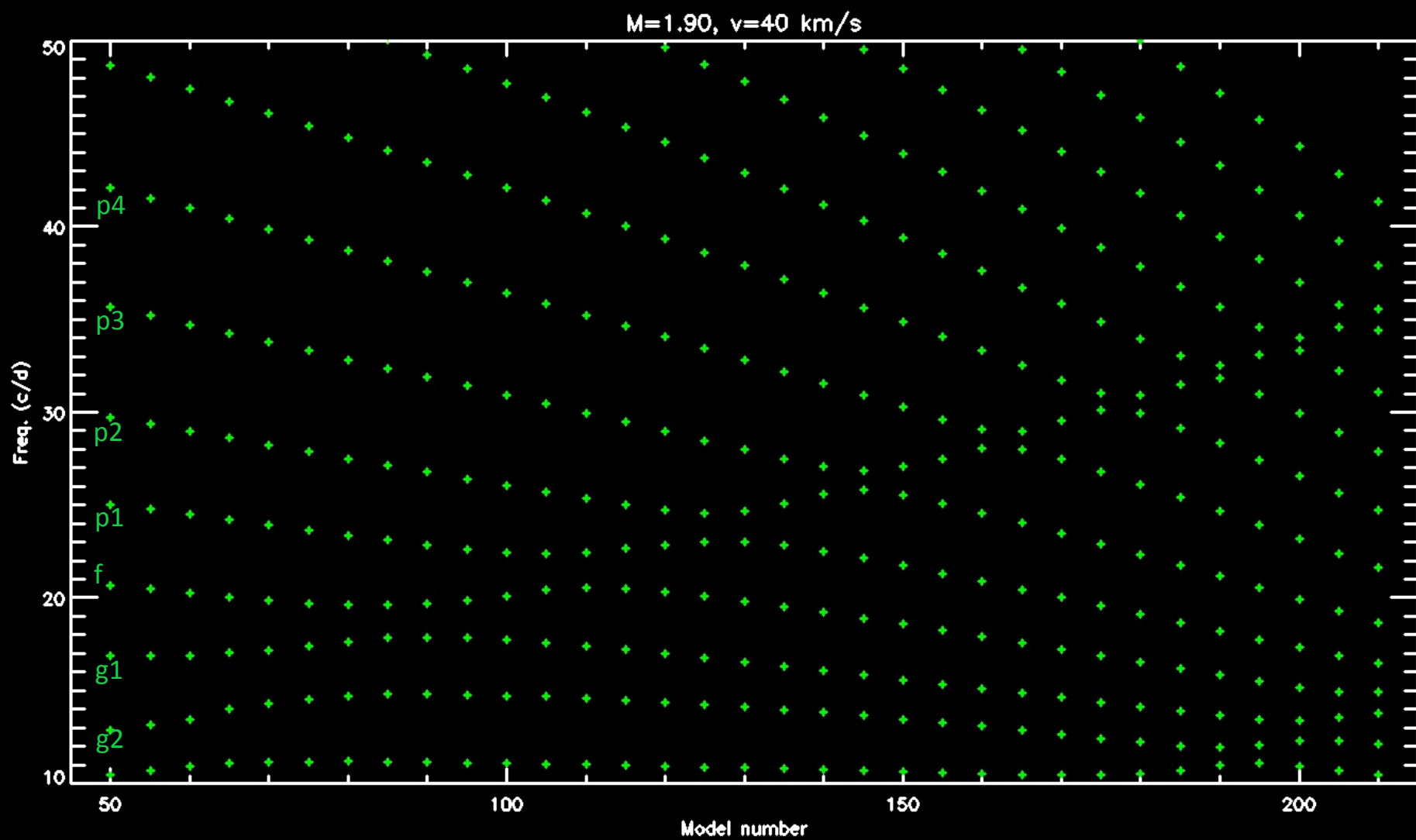
(Daszyńska-Daszkiewicz et al. 2017, MNRAS 466, 2284)

# Correct for the effect of mode densities

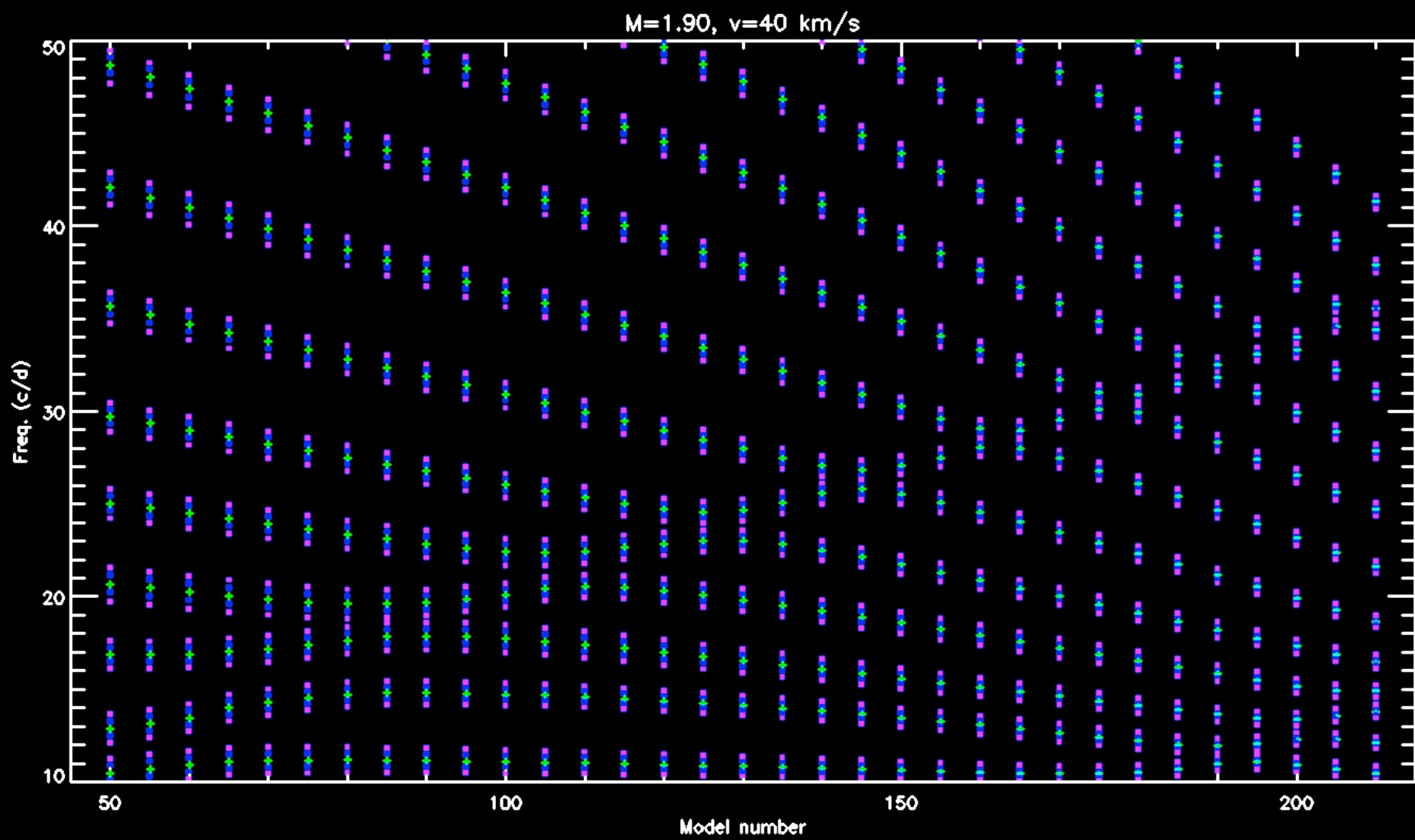
- Observable D: one frequency  $f=7.47$  c/d
- Prior:  $p(n)=1$  (if excited);  
0 (otherwise)  
 $p(L)= 1/3$  (L=0)  
1/3 (L=1)  
1/3 (L=2)

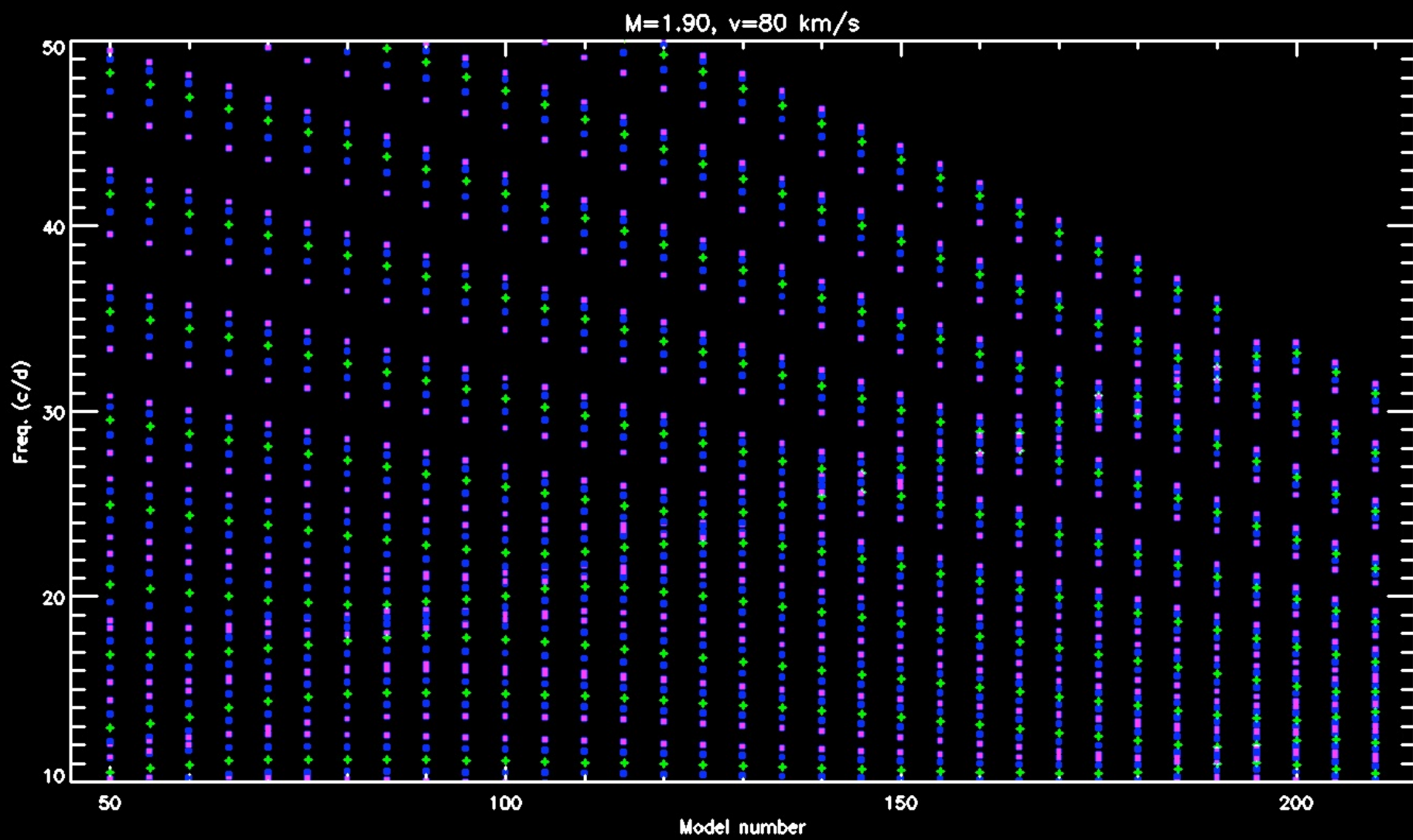
Posterior:

$$p(L|D)= \begin{array}{ll} 0.01 & (L=0) \\ 0.32 & (L=1) \\ 0.67 & (L=2) \end{array}$$



$L=2, m=0$





$L=2$ ,  $m=0$ ,  $+1$ ,  $+2$ ,  $-1$ ,  $-2$



